



**VoteBox:**

**a verifiable, tamper-evident  
electronic voting system**

**Dan S. Wallach**

Rice University



(Joint work with Daniel R. Sandler)



# Talk outline

# Talk outline

## I. Background

Trustworthiness of electronic voting machines  
Why it's worth improving them  
Related work

# Talk outline

## I. Background

Trustworthiness of electronic voting machines  
Why it's worth improving them  
Related work

## II. The design of VoteBox

Durability and audit  
Privacy and verifiability  
User interface  
Extensions

# Talk outline

## I. Background

Trustworthiness of electronic voting machines  
Why it's worth improving them  
Related work

## II. The design of VoteBox

Durability and audit  
Privacy and verifiability  
User interface  
Extensions

## III. Conclusion

# 1. Background



# **DRE** voting machines (**D**irect **R**ecording **E**lectronic)



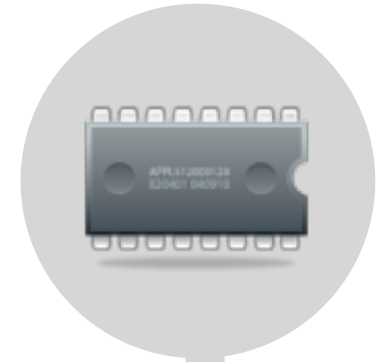


# **DRE** voting machines (**D**irect **R**ecording **E**lectronic)



touch screen / buttons  
graphical display

flash memory



# **DRE** voting machines (**D**irect **R**ecording **E**lectronic)



touch screen / buttons  
graphical display

# DREs discredited

Software bugs & design flaws  
identified by e-voting researchers



# DREs discredited

Software bugs & design flaws  
identified by e-voting researchers

## 2003 Analysis of Diebold AccuVote TS

Leaked source code analyzed [Kohno et al. 2004]

Poor software engineering, incorrect cryptography,  
vulnerable to malicious upgrades, multiple voting



# DREs discredited

Software **bugs** & design **flaws**  
identified by e-voting researchers

## 2003 Analysis of Diebold AccuVote TS

Leaked source code analyzed [Kohno et al. 2004]

Poor software engineering, incorrect cryptography,  
vulnerable to malicious upgrades, multiple voting

## 2006 “Voting-machine virus” developed

Self-propagating malicious upgrades that spread from  
machine to machine, altering votes and leaving no trace  
[Feldman et al. 2006]



# DREs discredited

Software bugs & design flaws  
identified by e-voting researchers



# DREs discredited

Software **bugs** & design **flaws**  
identified by e-voting researchers

**2007** Involvement by computer scientists  
in statewide voting systems audits

groundbreaking access to source code of commercial  
voting systems



# DREs discredited

Software **bugs** & design **flaws**  
identified by e-voting researchers

**2007** Involvement by computer scientists  
in statewide voting systems audits

groundbreaking access to source code of commercial  
voting systems

## **Top-To-Bottom Review (California)**

- ▶ All machines certified for use in CA found to have serious bugs & be vulnerable to attack
- ▶ Viral-style attacks found in all systems





# DREs discredited

Software **bugs** & design **flaws**  
identified by e-voting researchers

**2007** Involvement by computer scientists  
in statewide voting systems audits

groundbreaking access to source code of commercial  
voting systems

## **Top-To-Bottom Review (California)**

- ▶ All machines certified for use in CA found to have serious bugs & be vulnerable to attack
- ▶ Viral-style attacks found in all systems

## **EVEREST study (Ohio)**

- ▶ All machines certified in OH found vulnerable (validating CA-TTBR)
- ▶ Showed that hundreds of votes were lost in 2004



**Result:**  
**undermined trust  
in elections**







Trash

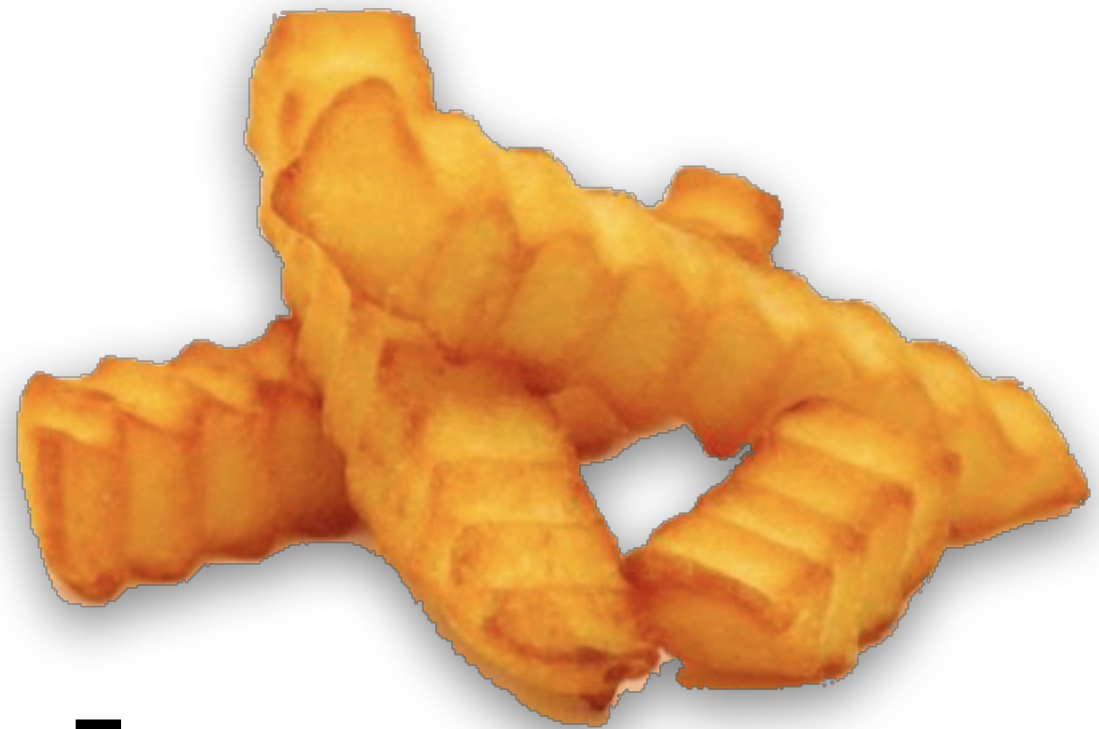
?

**voters**  
**prefer**  
**electronic**  
**voting**

# voters prefer electronic voting

S. P. Everett, K. K. Greene, M. D. Byrne, D. S. Wallach, K. Derr, **D. R. Sandler**, and T. Torous.  
*Electronic voting machines versus traditional methods: Improved preference, similar performance.*  
In CHI 2008.

# voters prefer electronic voting

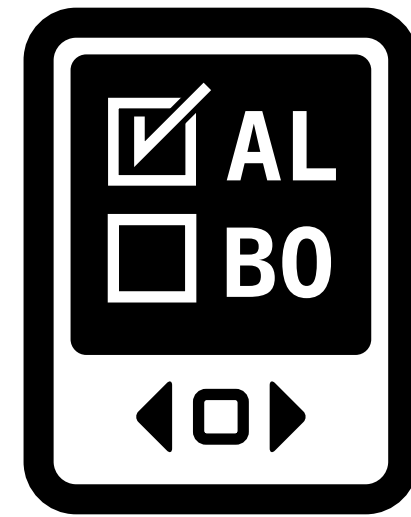


S. P. Everett, K. K. Greene, M. D. Byrne, D. S. Wallach, K. Derr, **D. R. Sandler**, and T. Torous.  
*Electronic voting machines versus traditional methods: Improved preference, similar performance.*  
In CHI 2008.



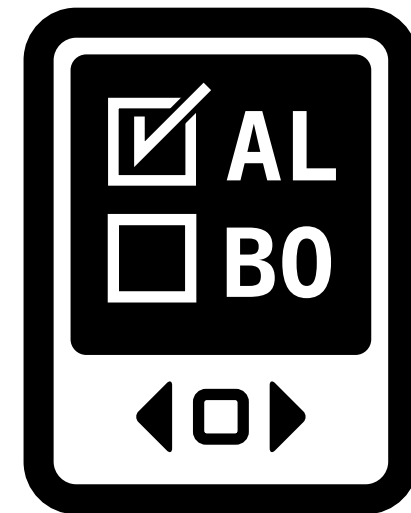


# legitimate benefits



# legitimate benefits

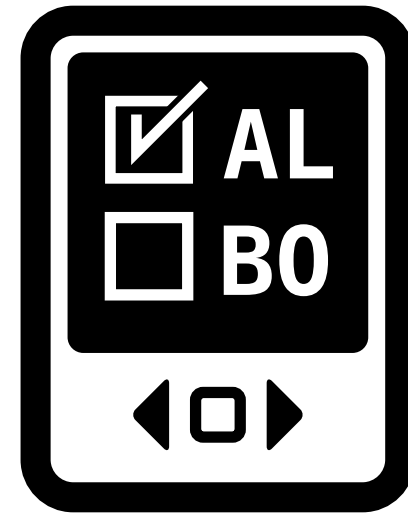
accessibility



# legitimate benefits

accessibility

feedback

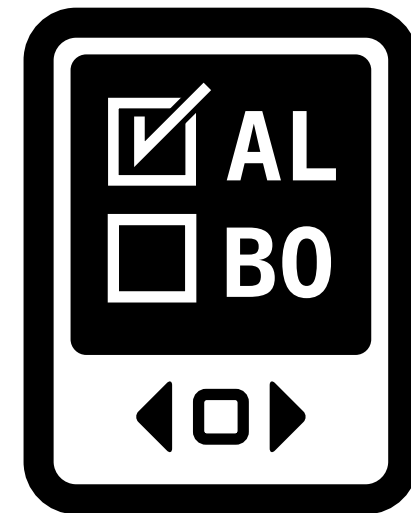


# legitimate benefits

accessibility

feedback

flexibility



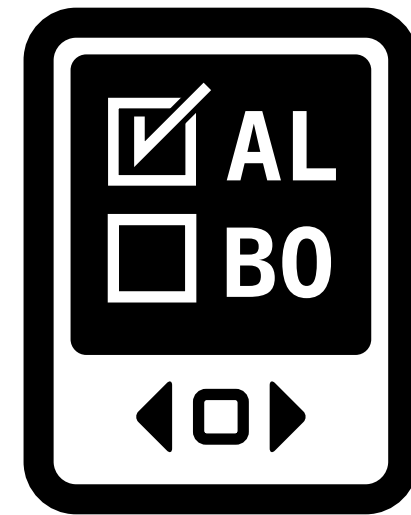
# legitimate benefits

accessibility

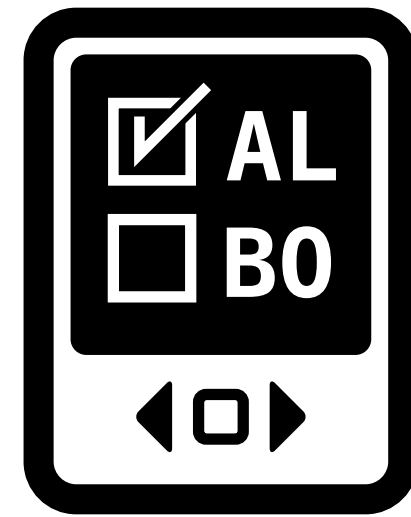
feedback

flexibility

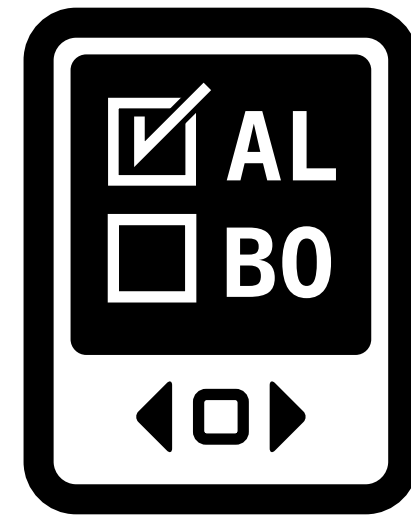
satisfaction



can we  
design a  
better DRE?



can we  
design a  
better DRE?



“better” = ?

# goals

## **1. resistance to failure & tampering**

essential vote data should survive  
hardware failure, poll worker mistakes,  
attempts to attack the system



# goals

## **2. tamper-evidence**

if we are unable to prevent data loss,  
we must always be able to detect the  
failure

# goals

## 3. verifiability

two useful properties:

### cast-as-intended

“Was my vote recorded faithfully?”  
very, very hard for DREs to satisfy

### counted-as-cast

“Has my vote been tallied correctly?”  
can be somewhat addressed with recounts

# goals

## **resistance to failure & tampering**

prevent or minimize data loss

## **tamper-evidence**

if resistance is futile

## **verifiability**

cast-as-intended; counted-as-cast

## **DRE user experience**

## **smaller codebase**

# a computer science problem

**resistance to failure & tampering**

replication; gossip

**tamper-evidence**

secure logs

**verifiability**

cryptography

**DRE user experience**

**smaller codebase**

# a computer science problem

**resistance to failure & tampering**

replication; gossip

**tamper-evidence**

secure logs

**verifiability**

cryptography

**DRE user experience**

**smaller codebase**

# a computer science problem

**resistance to failure & tampering**

replication; gossip

**tamper-evidence**

secure logs

**Auditorium**

**verifiability**

cryptography

**DRE user experience**

**smaller codebase**

# a computer science problem

**resistance to failure & tampering**

replication; gossip

**tamper-evidence**

secure logs

**Auditorium**

**verifiability**

cryptography

**DRE user experience**

**smaller codebase**

# a computer science problem

**resistance to failure & tampering**

replication; gossip

**tamper-evidence**

secure logs

**Auditorium**

**verifiability**

cryptography

**Ballot challenge**

**DRE user experience**

**smaller codebase**



# a computer science problem

**resistance to failure & tampering**

replication; gossip

**tamper-evidence**

secure logs

**Auditorium**

**verifiability**

cryptography

**Ballot challenge**

**DRE user experience**

**smaller codebase**

# a computer science problem

**resistance to failure & tampering**

replication; gossip

**tamper-evidence**

secure logs

**Auditorium**

**verifiability**

cryptography

**Ballot challenge**

**DRE user experience**

**smaller codebase**

**PRUI**

# other research voting systems

## **Mixnets**

Chaum '81

Neff '01

Chaum '04 (visual crypto)

Prêt-à-voter: Chaum, Ryan,  
Schneider '05

## **Blind signatures**

FOO: Fujioka, Okamoto, Ohta '92

EVOX: Herschberg '97

Sensus: Cranor, Cytron '97

## **Storage**

Molnar, Kohno, Sastry, Wagner '06

Bethencourt, Boneh, Waters '07

## **Homomorphic crypto and NIZKs**

Benaloh '87

Adder: Kiayias, Korman, Walluck '06

Moran, Naor '06

Benaloh '07

Helios: Adida '08

Civitas: Clarkson, Chong, Myers '08

## **TCB reduction**

Pvote: Yee '06, '07

Sastry, Kohno, Wagner '06

## **Paper**

Punchscan: Chaum '05

ThreeBallot: Rivest '06

Scantegrity: Chaum '07

# other research voting systems

## Mixnets

Chaum '81

Neff '01

Chaum '04 (visual crypto)

Prêt-à-voter: Chaum, Ryan,  
Schneider '05

## Blind signatures

FOO: Fujioka, Okamoto, Ohta '92

EVOX: Herschberg '97

Sensus: Cranor, Cytron '97

## Storage

Molnar, Kohno, Sastry, Wagner '06

Bethencourt, Boneh, Waters '07

## Homomorphic crypto and NIZKs

Benaloh '87

Adder: Kiayias, Korman, Walluck '06

Moran, Naor '06

Benaloh '07

Helios: Adida '08

Civitas: Clarkson, Chong, Myers '08

## TCB reduction

Pvote: Yee '06, '07

Sastry, Kohno, Wagner '06

## Paper

Punchscan: Chaum '05

ThreeBallot: Rivest '06

Scantegrity: Chaum '07

**“The Auditorium”**

**“The Auditorium”**

# Auditorium's approach

**D. Sandler** and D. S. Wallach. **Casting Votes in the Auditorium.** In Proceedings of the 2nd USENIX/ACCURATE Electronic Voting Technology Workshop (EVT'07).

# Auditorium's approach

**Store everything everywhere**

Massive **redundancy**

Stop trusting DREs to keep their own audit data

**D. Sandler** and D. S. Wallach. **Casting Votes in the Auditorium**. In Proceedings of the 2nd USENIX/ACCURATE Electronic Voting Technology Workshop (EVT'07).



# Auditorium's approach

## Store everything everywhere

Massive **redundancy**

Stop trusting DREs to keep their own audit data

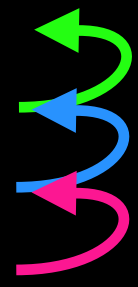
## Link all votes, events together

Create a **secure timeline** of election events

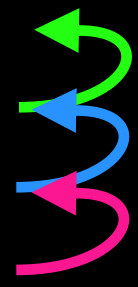
Tamper-evident proof of each vote's legitimacy

**D. Sandler** and D. S. Wallach. **Casting Votes in the Auditorium**. In Proceedings of the 2nd USENIX/ACCURATE Electronic Voting Technology Workshop (EVT'07).

# Ingredient: **hash chains**

	"Machine turned on"	(HASH = 0x1234)	
"Cast a vote after event"	0x1234	(HASH = 0xABCD)	
"Cast a vote after event"	0xABCD	(HASH = 0xBEEF)	
"Turned off after event"	0xBEEF	(HASH = 0x4242)	

# Ingredient: **hash chains**

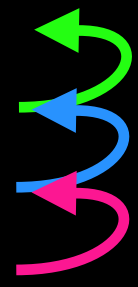
	"Machine turned on"	(HASH = 0x1234)	
"Cast a vote after event"	0x1234	(HASH = 0xABCD)	
"Cast a vote after event"	0xABCD	(HASH = 0xBEEF)	
"Turned off after event"	0xBEEF	(HASH = 0x4242)	

## A hash-chained **secure log**

Every event includes the cryptographic hash (e.g. SHA1) of a previous event

[Schneier & Kelsey '99]

# Ingredient: hash chains

	"Machine turned on"	(HASH = 0x1234)	
"Cast a vote after event 0x1234"	(HASH = 0xABCD)		
"Cast a vote after event 0xABCD"	(HASH = 0xBEEF)		
"Turned off after event 0xBEEF"	(HASH = 0x4242)		

## A hash-chained secure log

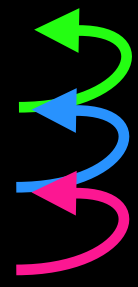
Every event includes the cryptographic hash (e.g. SHA1) of a previous event

[Schneier & Kelsey '99]

## Result: provable order

If **Y** includes  $H(\mathbf{X})$ , then **Y** must have happened after **X**

# Ingredient: **hash chains**

	"Machine turned on"	(HASH = 0x1234)	
"Cast a vote after event"	0x1234	(HASH = 0xABCD)	
"Cast a vote after event"	0xABCD	(HASH = 0xBEEF)	
"Turned off after event"	0xBEEF	(HASH = 0x4242)	

## A hash-chained **secure log**

Every event includes the cryptographic hash (e.g. SHA1) of a previous event

[Schneier & Kelsey '99]

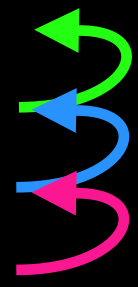
## Result: **provable order**

If **Y** includes  $H(\mathbf{X})$ , then **Y** must have happened after **X**

## Any **attempted change** to the log

invalidates all later hashes (breaks the chain)

# Ingredient: **hash chains**

	"Machine turned on"	(HASH = 0x1234)	
"Cast a vote after event"	0x1234	(HASH = 0xABCD)	
"Cast a vote after event"	0xABCD	(HASH = 0xBEEF)	
"Turned off after event"	0xBEEF	(HASH = 0x4242)	

## A hash-chained **secure log**

Every event includes the cryptographic hash (e.g. SHA1) of a previous event

[Schneier & Kelsey '99]

## Result: **provable order**

If **Y** includes  $H(\mathbf{X})$ , then **Y** must have happened after **X**

## Any **attempted change** to the log

invalidates all later hashes (breaks the chain)

## To **alter, insert, or delete** a single record

you must alter every subsequent event as well!

**Ingredient: timeline entanglement**

# Ingredient: timeline entanglement

Entanglement = “chain with hashes from others”

Result: event ordering **between** participants

[Maniatis & Baker '02]





# Ingredient: **timeline entanglement**

Entanglement = “chain with hashes from others”

Result: event ordering **between** participants

[Maniatis & Baker '02]



**Malicious machines can't retroactively alter their own logs**

it would violate commitments they have already exchanged with others

# Ingredient: timeline entanglement

Entanglement = “chain with hashes from others”

Result: event ordering **between** participants

[Maniatis & Baker '02]



Malicious machines can't retroactively alter their own logs

it would violate commitments they have already exchanged with others

**So with whom should a VoteBox entangle?**

**Ingredient: broadcast**

# Ingredient: **broadcast**

## **All-to-all communication**

All messages signed & distributed to every VoteBox

Each machine records each message independently

# Ingredient: **broadcast**

## **All-to-all communication**

All messages signed & distributed to every VoteBox

Each machine records each message independently

## **result: massive replication**

$O(N^2)$ , but  $N$  is small in a polling place

# Ingredient: **broadcast**

## **All-to-all communication**

All messages signed & distributed to every VoteBox

Each machine records each message independently

## **result: massive replication**

$O(N^2)$ , but  $N$  is small in a polling place

## **Mechanism for entanglement**

each log fills up with local and remote messages

when sending new messages, include recent hashes  
(regardless of origin)

**Broadcast entanglement =  
Auditorium**

# Unusual prior art



## The Papal Conclave

Proceedings **closed** to outsiders

All ballots cast **in plain view**

All ballots **secret**

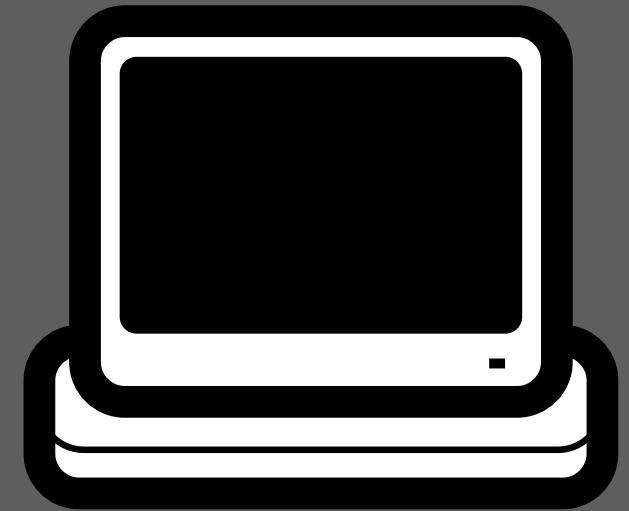


# A pragmatic benefit

# A pragmatic benefit

The **supervisor console**

Assistance for poll workers



# A pragmatic benefit

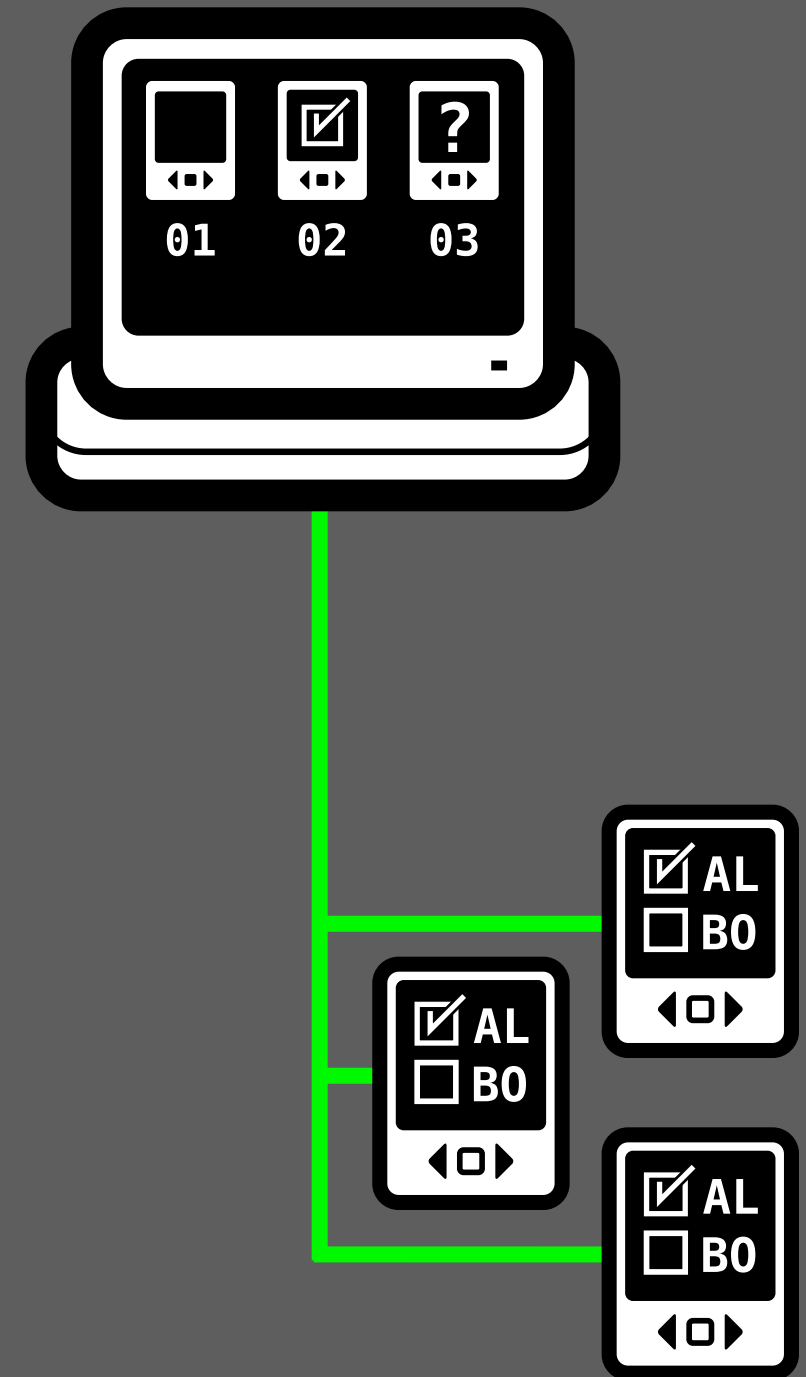
## The **supervisor console**

Assistance for poll workers

## Helps conduct the election

Open/close polls, authorize machines to cast ballots

Less opportunity for poll-worker error



# A pragmatic benefit

## The **supervisor console**

Assistance for poll workers

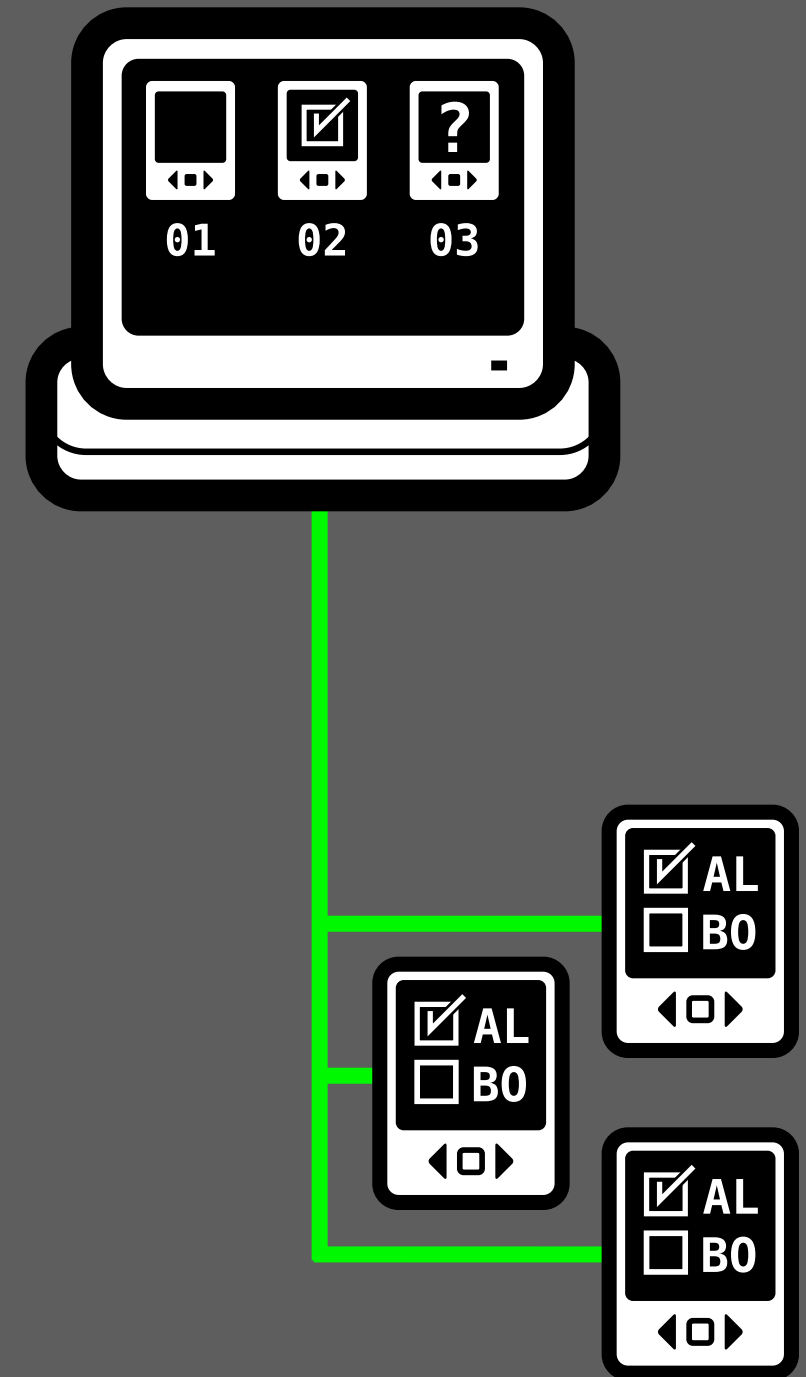
## Helps conduct the election

Open/close polls, authorize machines to cast ballots

Less opportunity for poll-worker error

## Ballots distributed over the network

Booths are **stateless**, interchangeable  
(Supervisor can have a spare as well)



# A pragmatic benefit

## The **supervisor console**

Assistance for poll workers

## Helps conduct the election

Open/close polls, authorize machines to cast ballots

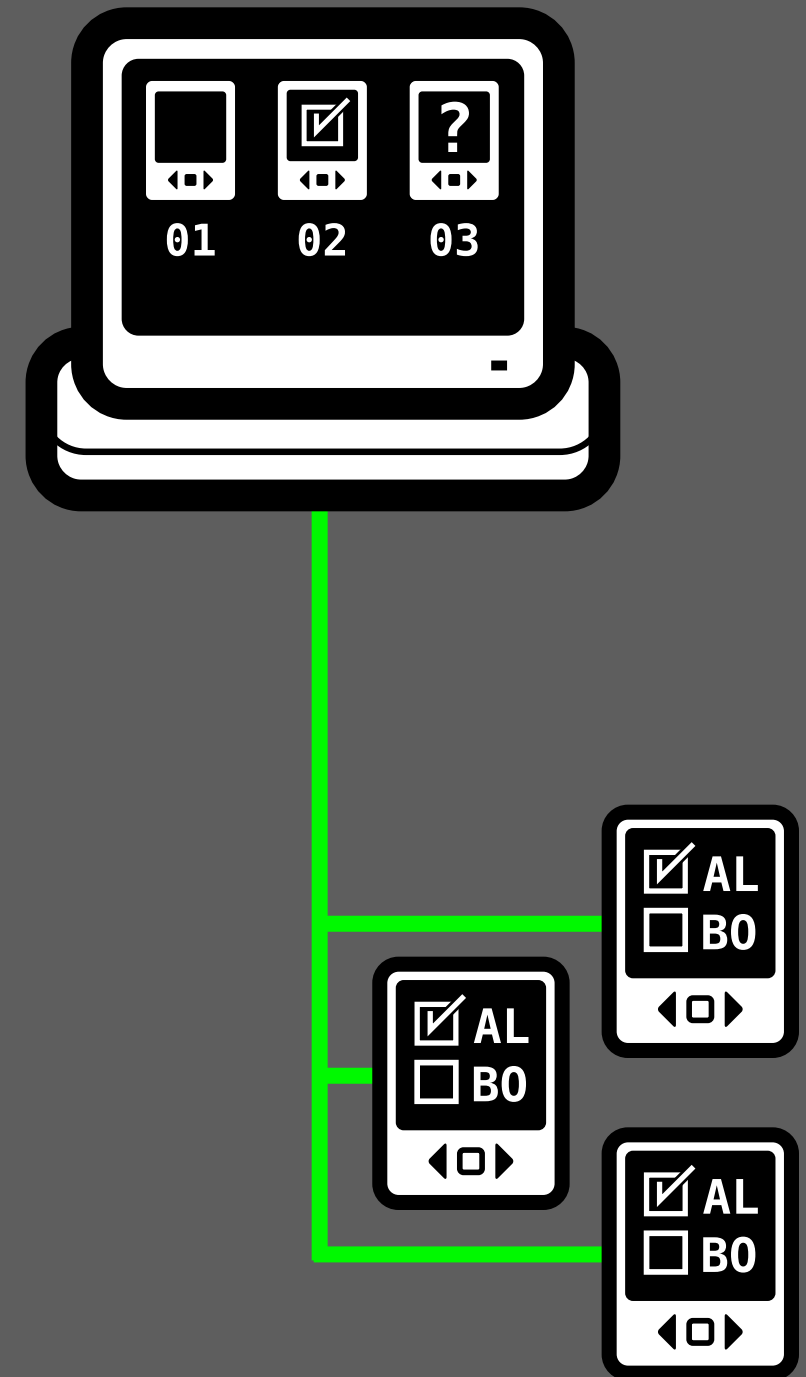
Less opportunity for poll-worker error

## Ballots distributed over the network

Booths are **stateless**, interchangeable  
(Supervisor can have a spare as well)

## Shows status of all machines

Votes cast, battery running low, etc.



# How do you audit a secure log?

# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

## Where is that program?



# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

## Where is that program?

“suspicious” is domain-specific

# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

## Where is that program?

“suspicious” is domain-specific

**QUERIFIER:** an audit log analysis tool

# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

## Where is that program?

“suspicious” is domain-specific

**QUERIFIER:** an audit log analysis tool

Predicate logic for expressing rules over secure logs

# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

## Where is that program?

“suspicious” is domain-specific

**QUERIFIER:** an audit log analysis tool

Predicate logic for expressing rules over secure logs

Key predicate: “precedes” — requires graph search

# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

## Where is that program?

“suspicious” is domain-specific

## **QUERIFIER:** an audit log analysis tool

Predicate logic for expressing rules over secure logs

Key predicate: “precedes” — requires graph search

Querifier runs on a complete log (“OK” / “Violation”)

# How do you audit a secure log?

*“Audit logs are useless unless someone reads them. Hence, we first assume that there is a software program whose job it is to scan all audit logs and look for suspicious entries.”*

—Schneier & Kelsey '99

## Where is that program?

“suspicious” is domain-specific

## **QUERIFIER:** an audit log analysis tool

Predicate logic for expressing rules over secure logs

Key predicate: “precedes” — requires graph search

Querifier runs on a complete log (“OK” / “Violation”)

or iteratively on a growing log (“OK so far” / “Violation”)

**D. Sandler**, K. Derr, S. Crosby, and D. S. Wallach. **Finding the evidence in tamper-evident logs.** In Proceedings of the 3rd International Workshop on Systematic Approaches to Digital Forensic Engineering (SADFE'08).

**Ballots.**

# Privacy



# Privacy

**Secure log of votes could be a problem**

When decrypted for tallying, votes are exposed in **order**

An observer could match them with voters

Loss of privacy → bribery & coercion\*

# Privacy

**Secure log of votes could be a problem**

When decrypted for tallying, votes are exposed in **order**

An observer could match them with voters

Loss of privacy → bribery & coercion\*

**Anonymity through clever ballot ordering**

re-encryption mixnets

lexicographic sorting

# Privacy

**Secure log of votes could be a problem**

When decrypted for tallying, votes are exposed in **order**

An observer could match them with voters

Loss of privacy → bribery & coercion\*

**Anonymity through clever ballot ordering**

re-encryption mixnets

lexicographic sorting

**These would still require the ballots to be removed from the ordered audit logs**

# Ballots in VoteBox

# Ballots in VoteBox

**logically, a cast ballot is a vector of counters**  
one per *candidate*

# Ballots in VoteBox

**logically, a cast ballot is a vector of counters**  
one per *candidate*

**e.g., for one race with three candidates:**

$$\text{ballot} = (a, b, c) \qquad a, b, c \in \{0, 1\}$$

# Ballots in VoteBox

**logically, a cast ballot is a vector of counters**  
one per *candidate*

**e.g., for one race with three candidates:**

$$\text{ballot} = (a, b, c) \qquad a, b, c \in \{0, 1\}$$

**ballots may therefore be summed**

$$\text{tally} = \sum \text{ballot}_i = (\sum a_i, \sum b_i, \sum c_i)$$

# Encryption



# Encryption

## **Ballots should be sealed**

protected from prying eyes

once cast, they should be readable only by the parties  
trusted to count them

# Encryption

## **Ballots should be sealed**

protected from prying eyes

once cast, they should be readable only by the parties  
trusted to count them

## **But how do we count them?**

Remember, we don't want to decrypt them in order

# Diffie-Hellman (1976)

Alice : *random*  $a \in \mathbb{Z}_p^*$

Bob : *random*  $b \in \mathbb{Z}_p^*$

Public : *generator*  $g \in \mathbb{Z}_p^*$

$A \rightarrow B$  :  $g^a$

$B \rightarrow A$  :  $g^b$

Alice : computes  $(g^b)^a = g^{ab}$

Bob : computes  $(g^a)^b = g^{ab}$

Eve : knows  $g^a, g^b$ , cannot compute  $g^{ab}$

# Elgamal encryption (1984)

Non-deterministic cryptosystem (different  $r$  every time)

$$E(g^a, r, M) = \langle g^r, (g^a)^r M \rangle$$

$$D(g^r, g^{ar} M) = \frac{g^{ar} M}{(g^r)^a} = M$$

$g$	group generator
$M$	plaintext (message)
$r$	random (chosen at encryption time)
$a$	(private) decryption key
$g^a$	(public) encryption key

# Homomorphic property

Anybody can combine two ciphertexts to get a new one.

$$\begin{aligned} E(M_1) \oplus E(M_2) &= \langle g^{r_1}, (g^a)^{r_1} M_1 \rangle \oplus \langle g^{r_2}, (g^a)^{r_2} M_2 \rangle \\ &= \langle g^{r_1} g^{r_2}, (g^a)^{r_1} M_1 (g^a)^{r_2} M_2 \rangle \\ &= \langle g^{r_1+r_2}, g^{a(r_1+r_2)} M_1 M_2 \rangle \\ &= E(M_1 M_2) \end{aligned}$$

$g$	group generator
$M$	plaintext (message)
$r$	random (chosen at encryption time)
$a$	(private) decryption key
$g^a$	(public) encryption key

# Homomorphic vote tallying

Change messages to counters, additive in exponent of  $g$ .

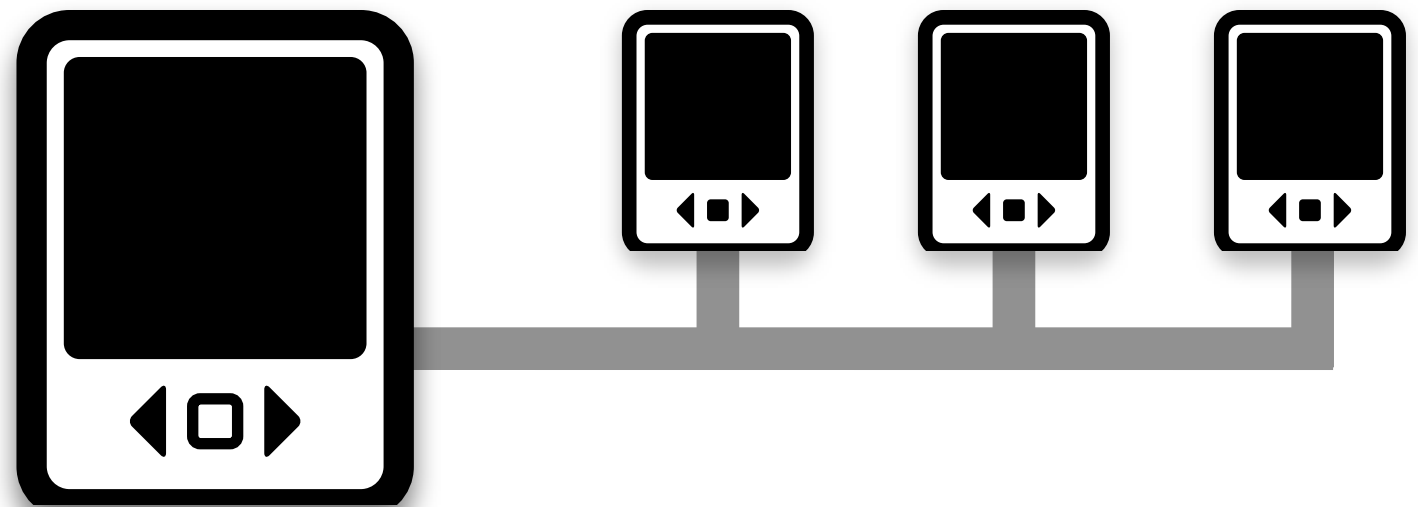
“Exponential Elgamal”

$$\begin{aligned} E(v_1) \oplus E(v_2) &= \langle g^{r_1}, (g^a)^{r_1} g^{v_1} \rangle \oplus \langle g^{r_2}, (g^a)^{r_2} g^{v_2} \rangle \\ &= \langle g^{r_1+r_2}, g^{a(r_1+r_2)} g^{v_1+v_2} \rangle \\ &= E(v_1 + v_2) \end{aligned}$$

$g$	group generator
$v$	plaintext (counters)
$r$	random (chosen at encryption time)
$a$	(private) decryption key
$g^a$	(public) encryption key

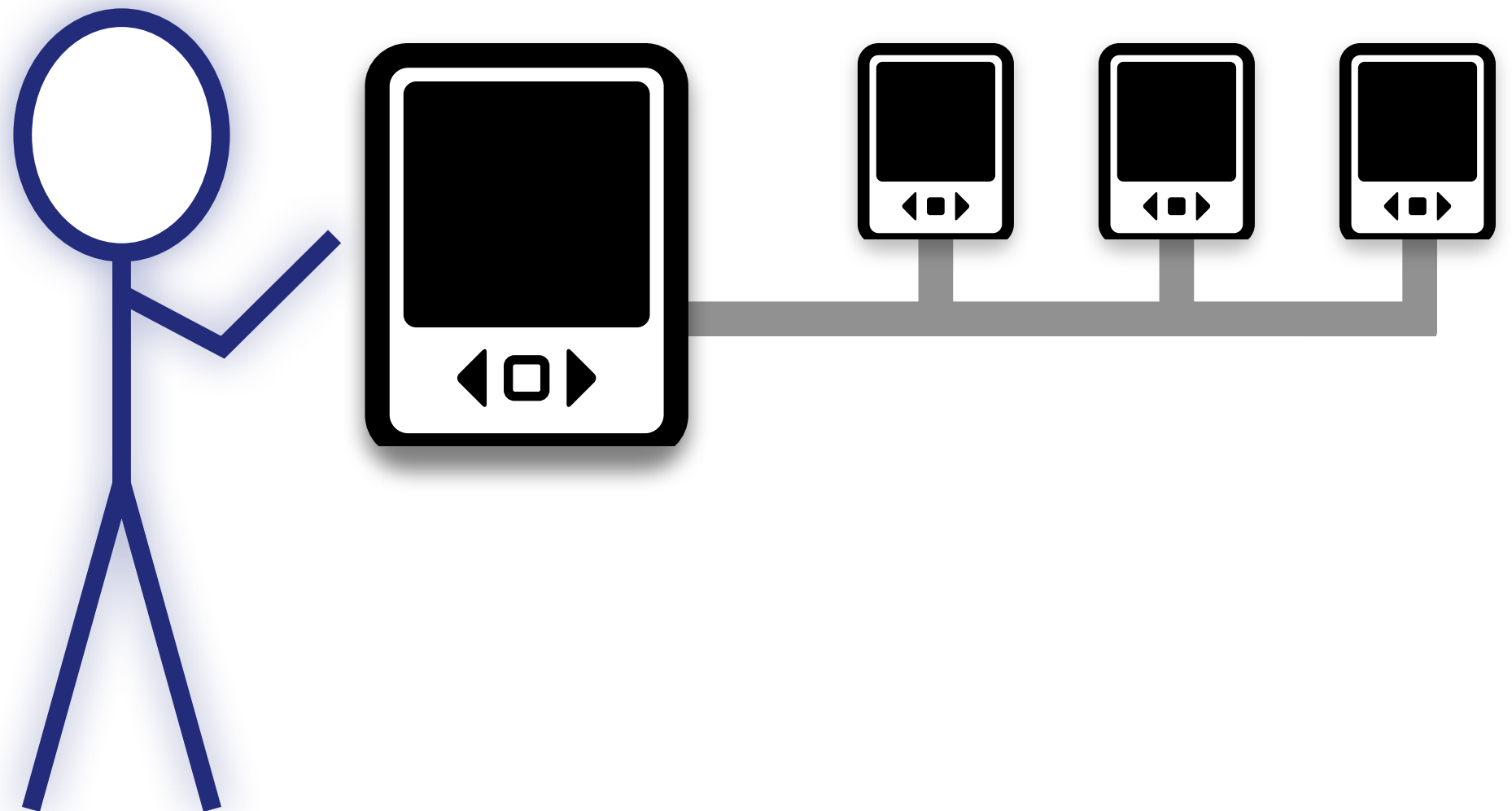
**How can I be sure my  
vote is faithfully captured  
by the voting machine?**

polling place

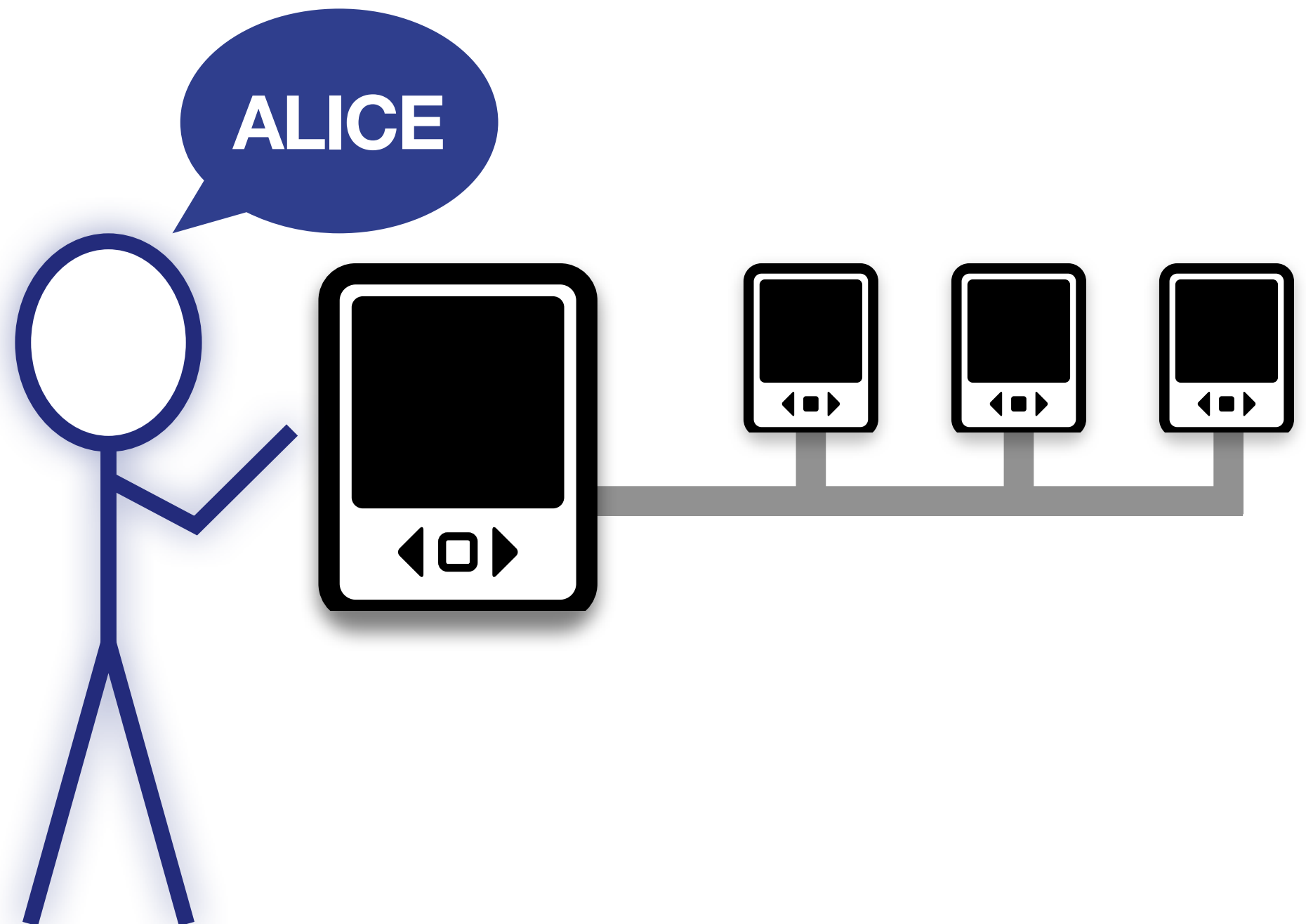




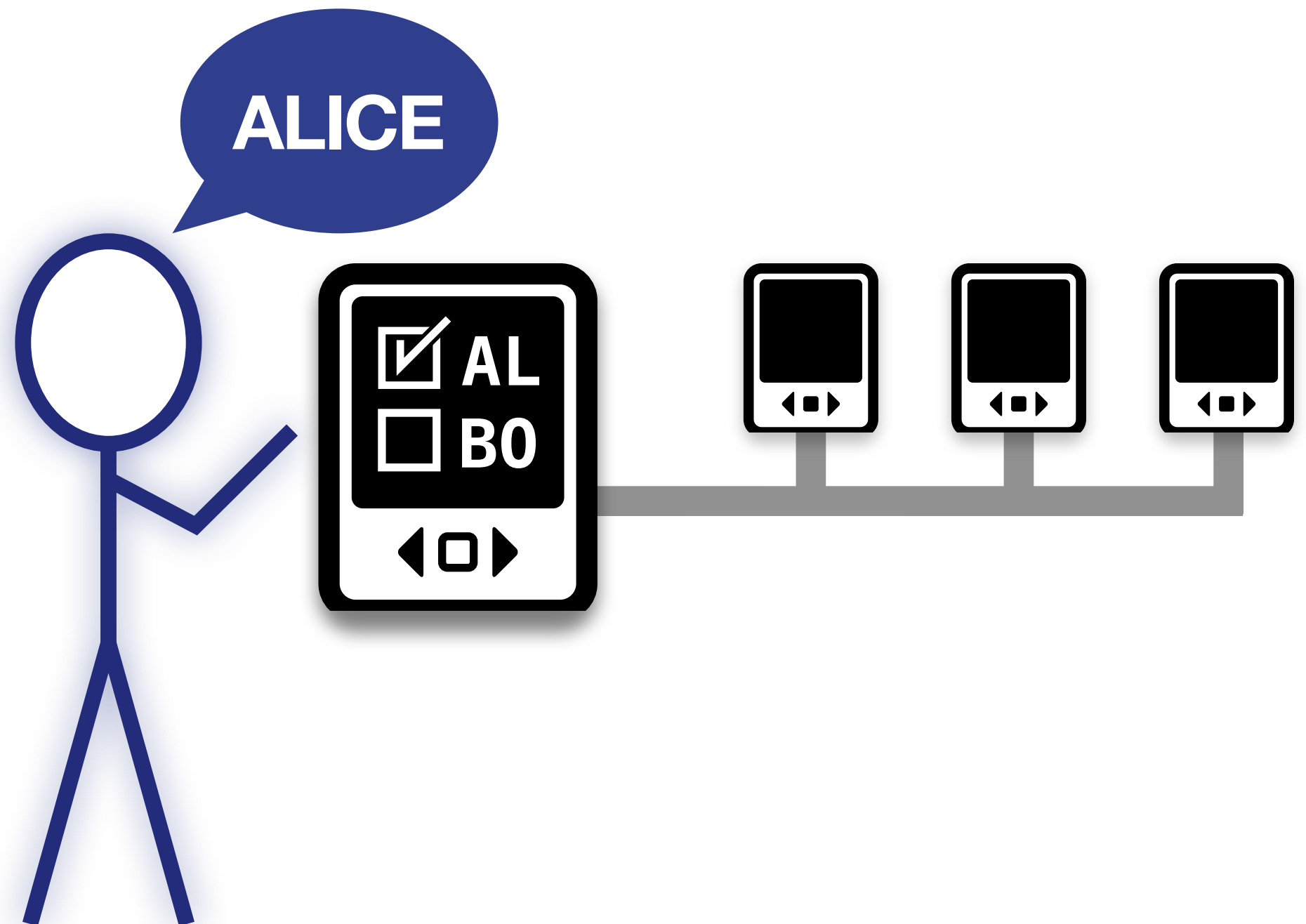
polling place



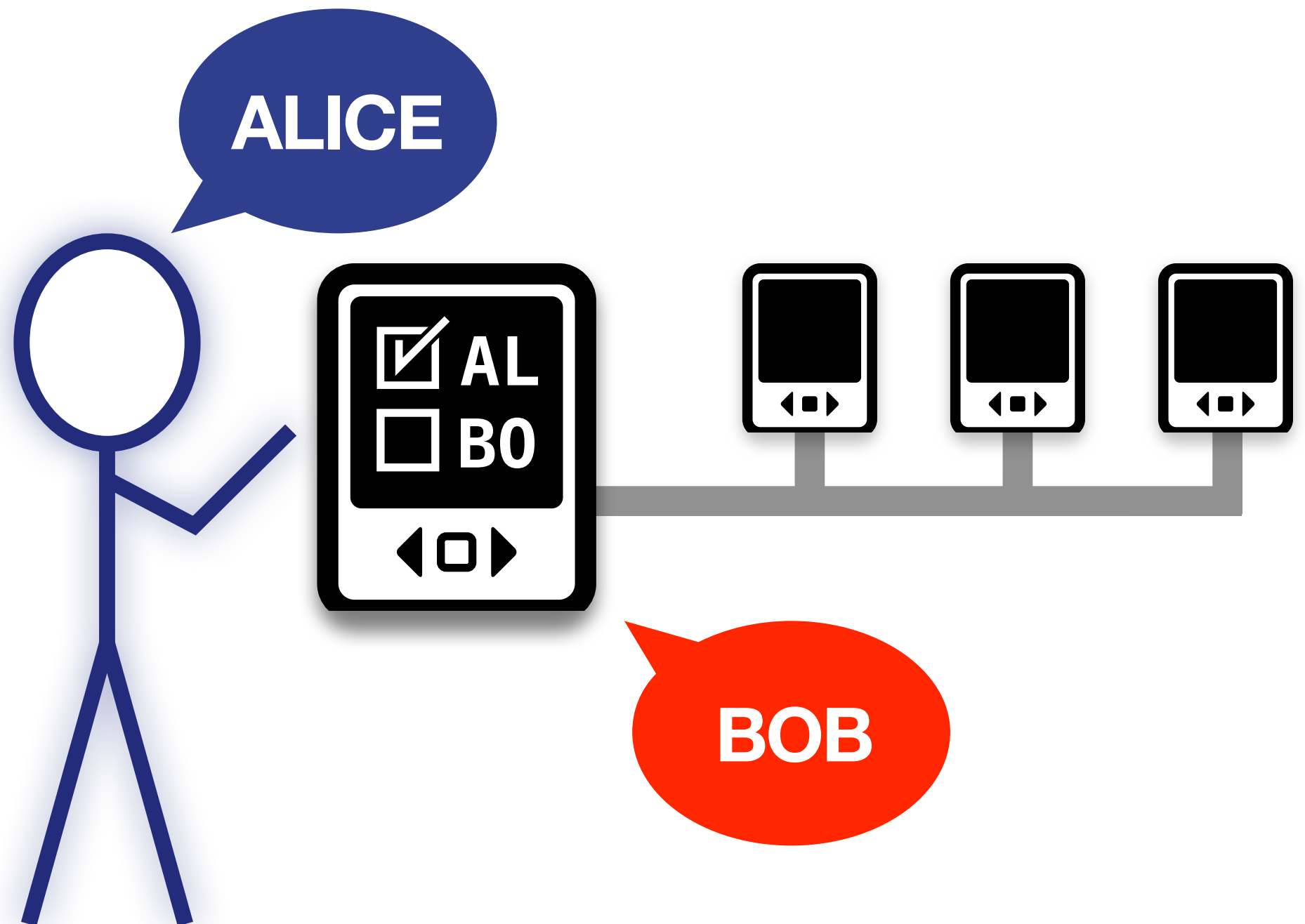
polling place



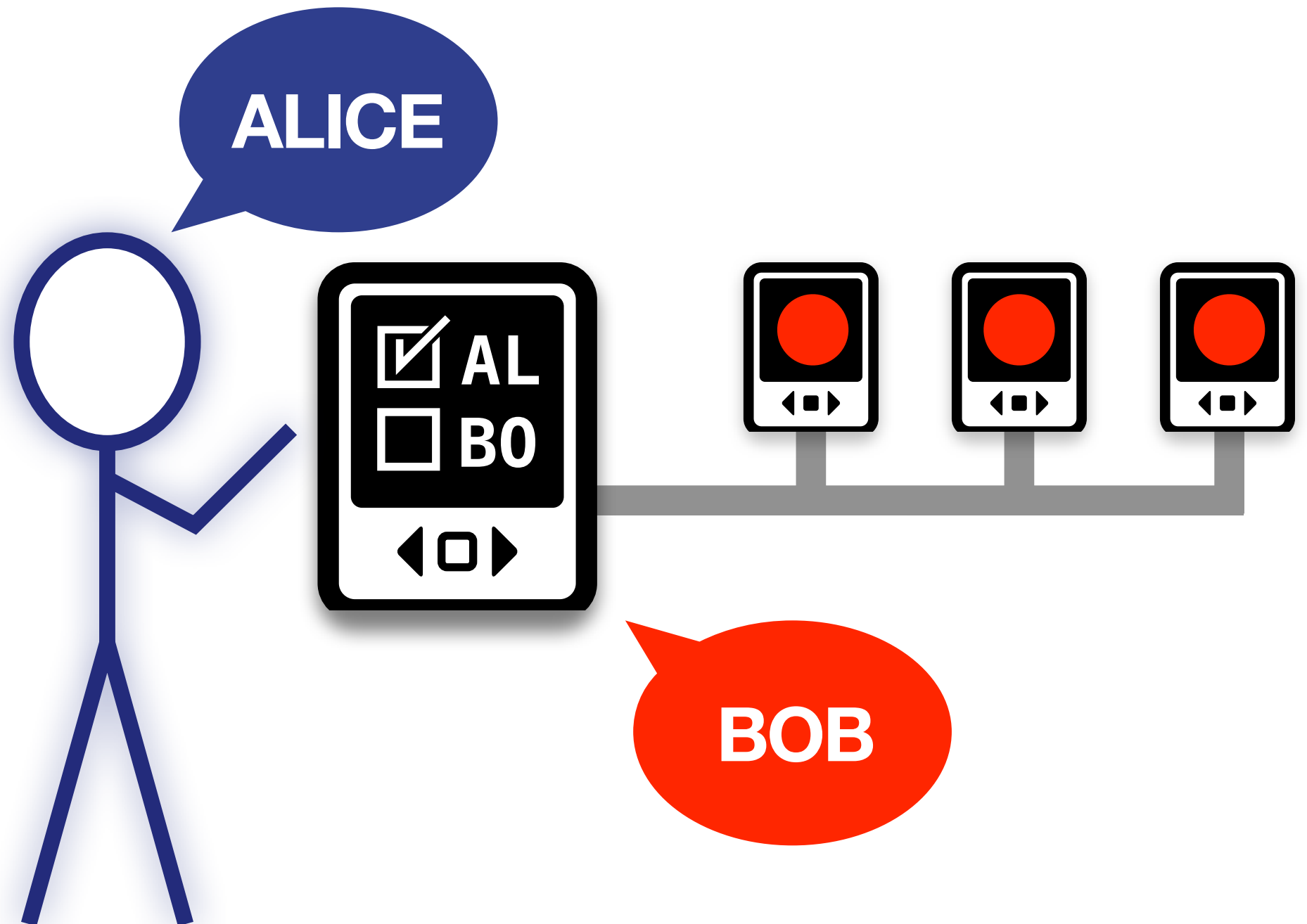
polling place



polling place



polling place



this doesn't work:

**“logic &  
accuracy testing”**

**VoteBox's approach:**  
**ballot challenge**

# ballot challenge



# ballot challenge

a technique due to [Benaloh '07]

# ballot challenge

a technique due to [Benaloh '07]

**at the end, instead of casting your ballot:**

force the machine to **show it to you**

# ballot challenge

a technique due to [Benaloh '07]

**at the end, instead of casting your ballot:**

force the machine to **show it to you**

**this happens on election day**

no artificial testing conditions (viz., “L&A tests”)

the voting machine cannot distinguish this from a real vote until the challenge

# ballot challenge

# ballot challenge

**voter makes  
selections**

# ballot challenge

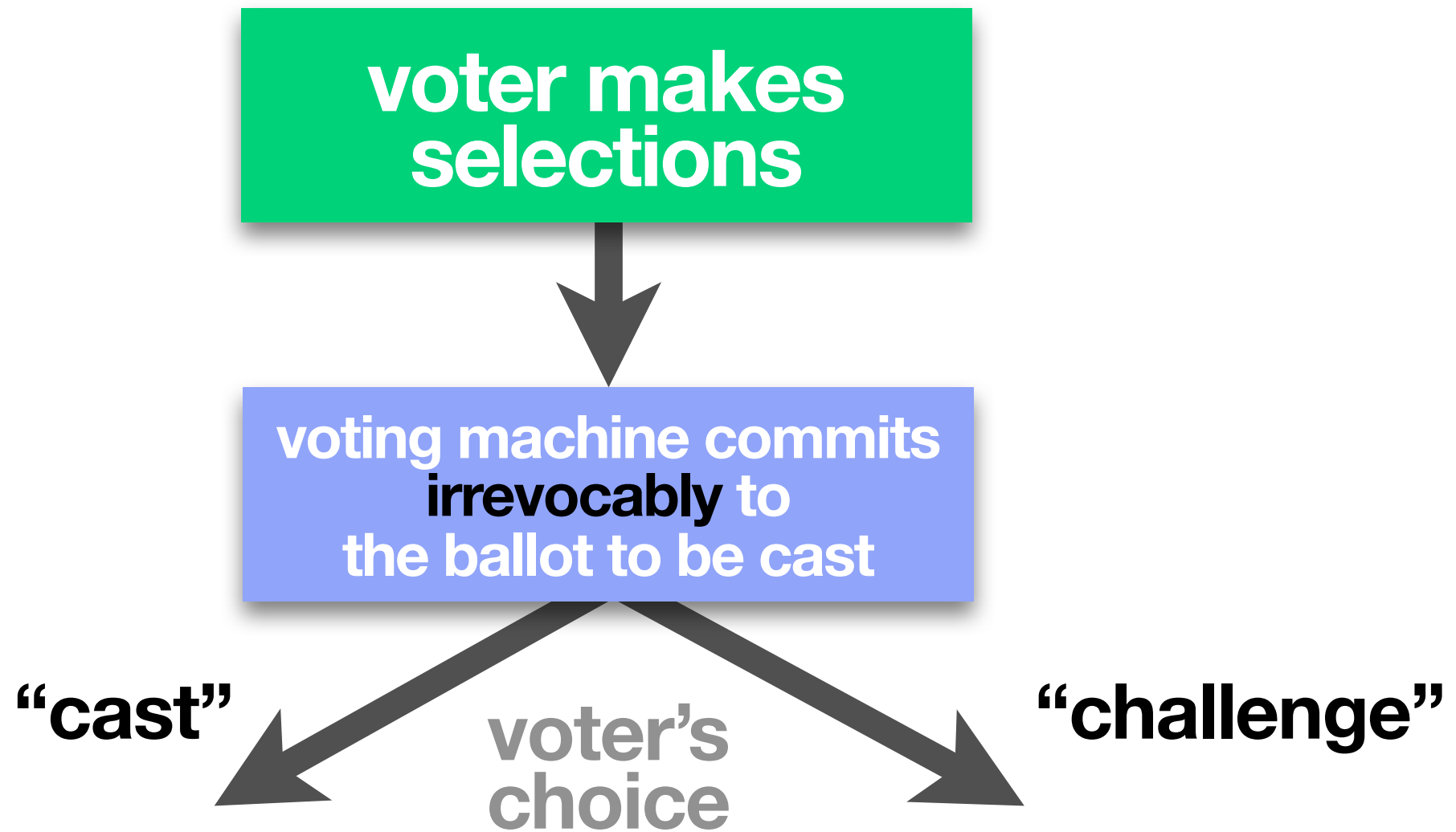
voter makes  
selections



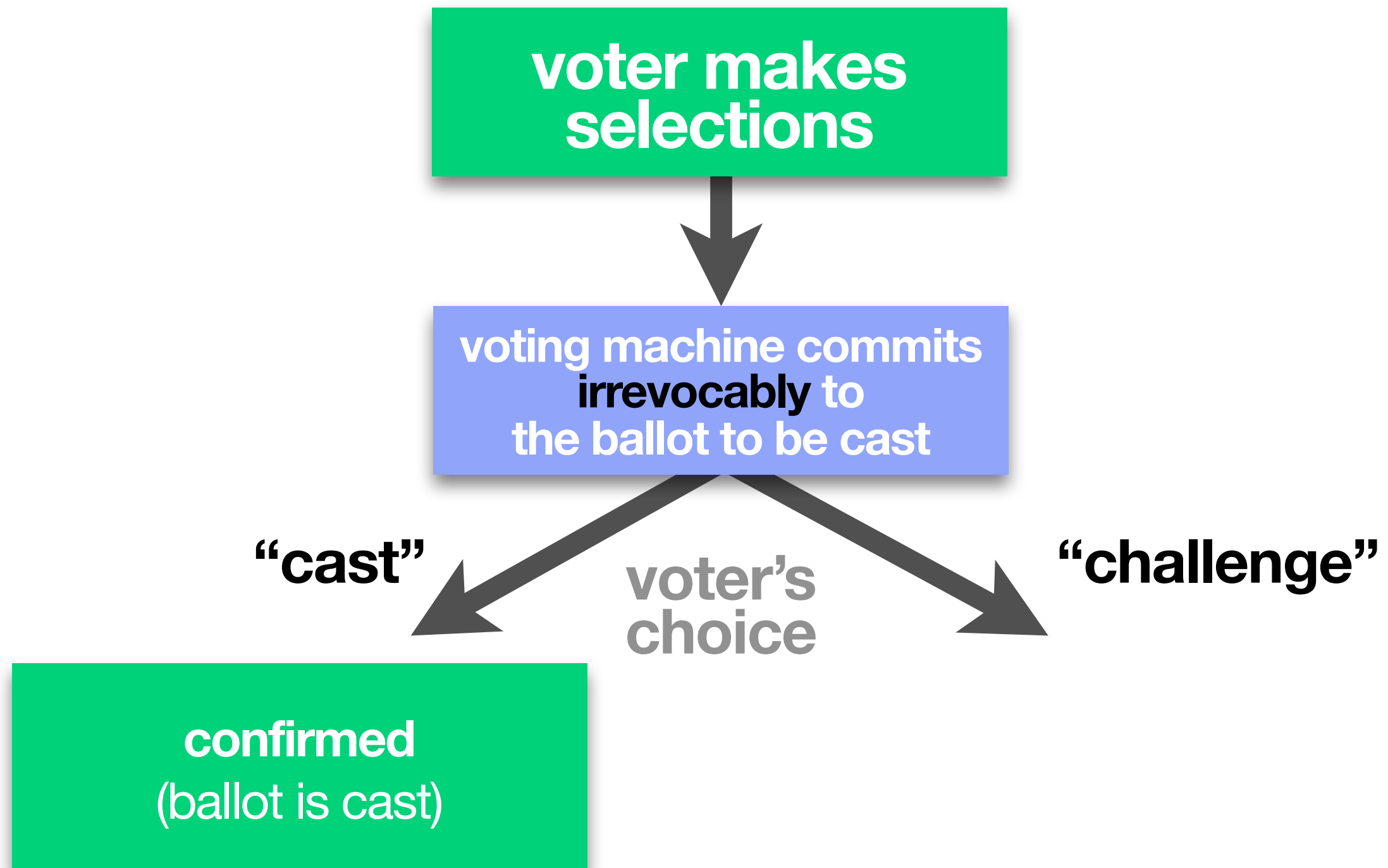
```
graph TD; A[voter makes selections] --> B[voting machine commits irrevocably to the ballot to be cast]
```

voting machine commits  
**irrevocably** to  
the ballot to be cast

# ballot challenge

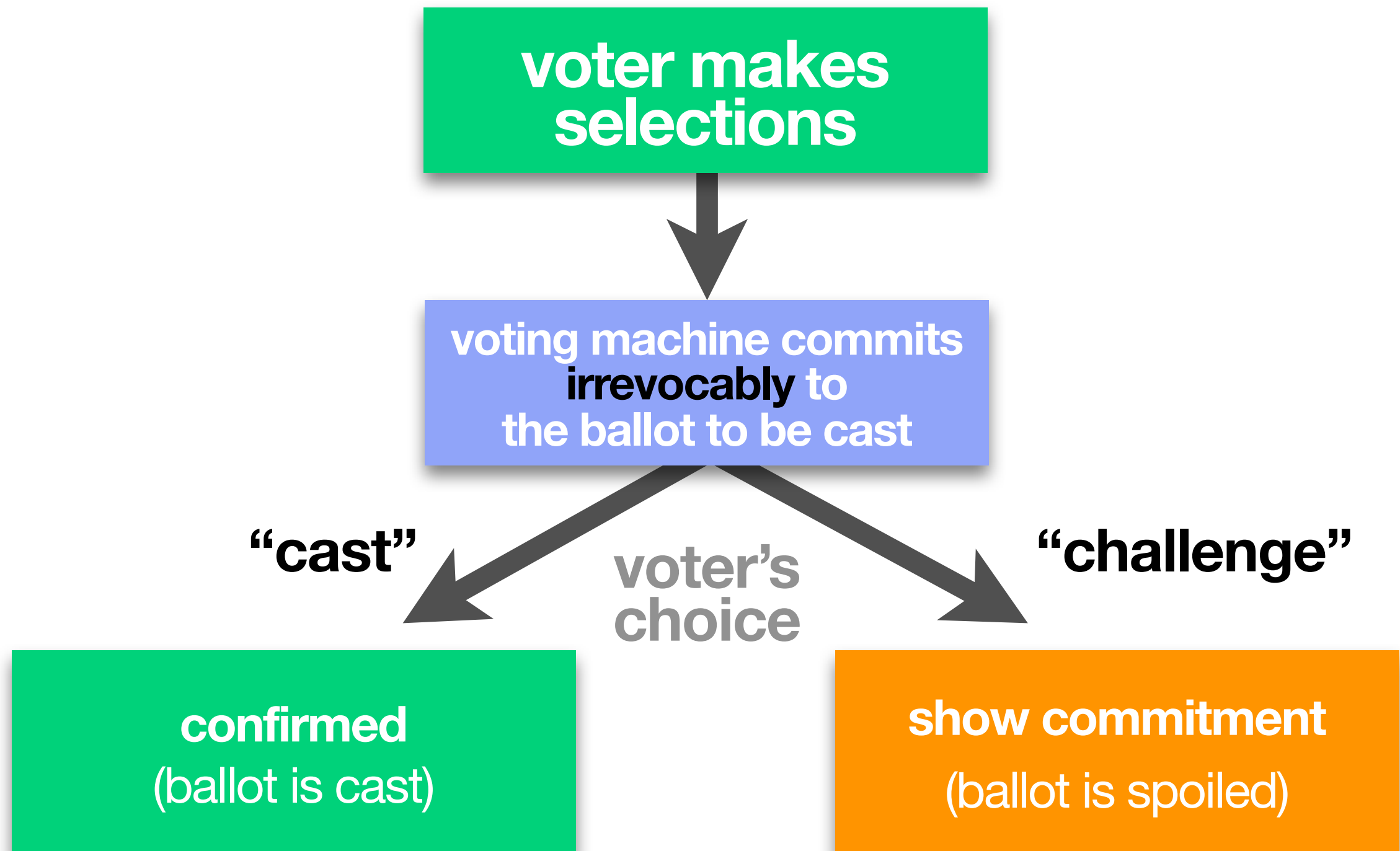


# ballot challenge





# ballot challenge



# ballot commitment

# ballot commitment

## **What is the commitment?**

How do we force the machine to produce proof of what it's about to cast on the voter's behalf?

# ballot commitment

## **What is the commitment?**

How do we force the machine to produce proof of what it's about to cast on the voter's behalf?

## **Benaloh's proposal**

print the encrypted ballot behind an opaque shield

You can't see the contents, but you can see the page

the computer cannot "un-print" the ballot

# ballot commitment

## **What is the commitment?**

How do we force the machine to produce proof of what it's about to cast on the voter's behalf?

## **Benaloh's proposal**

print the encrypted ballot behind an opaque shield

You can't see the contents, but you can see the page

the computer cannot "un-print" the ballot

## **How do you test the commitment?**

# ballot commitment

## What is the commitment?

How do we force the machine to produce proof of what it's about to cast on the voter's behalf?

## Benaloh's proposal

print the encrypted ballot behind an opaque shield

You can't see the contents, but you can see the page

the computer cannot "un-print" the ballot

## How do you test the commitment?

**Decrypt it.**

But decryption requires the private key for tabulating the whole election!

# Elgamal reminder

Two ways to decrypt:

$$E(g^a, r, M) = \langle g^r, (g^a)^r M \rangle$$

$$D(g^r, g^{ar} M, a) = \frac{g^{ar} M}{(g^r)^a}$$

$$D(g^r, g^{ar} M, r) = \frac{g^{ar} M}{(g^a)^r}$$

$$= M$$

$g$	group generator
$M$	plaintext (message)
$r$	random (chosen at encryption time)
$a$	(private) decryption key
$g^a$	(public) encryption key

# challenging the machine



# challenging the machine

**When challenged, the machine must reveal  $r$**

We can then decrypt this ballot (only) and see if it's what we expected to see

**In Benaloh, the encrypted ballot is on paper**

An **irrevocable** output medium

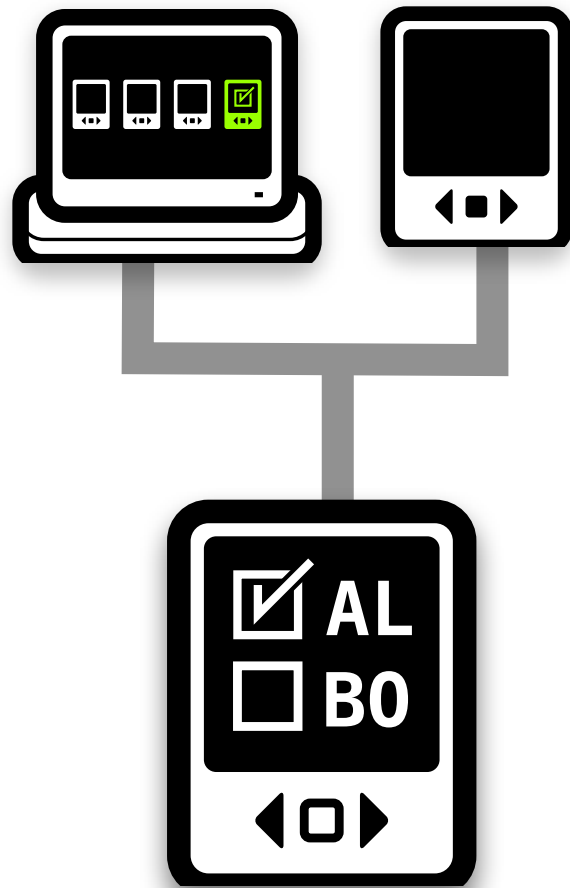
decrypting requires additional equipment

**VoteBox happens to have its own irrevocable publishing system**

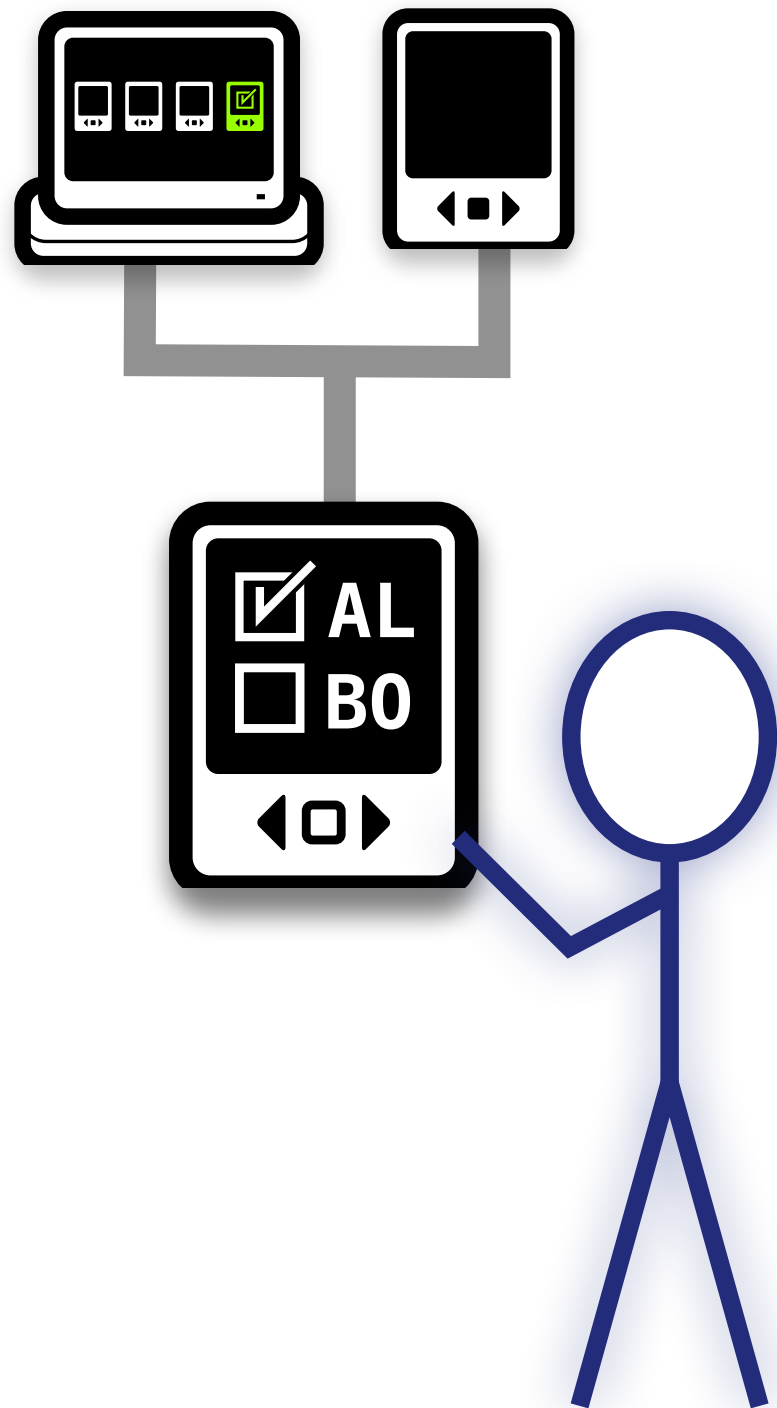
One that doesn't run out of ink or paper

**Auditorium.**

# polling place

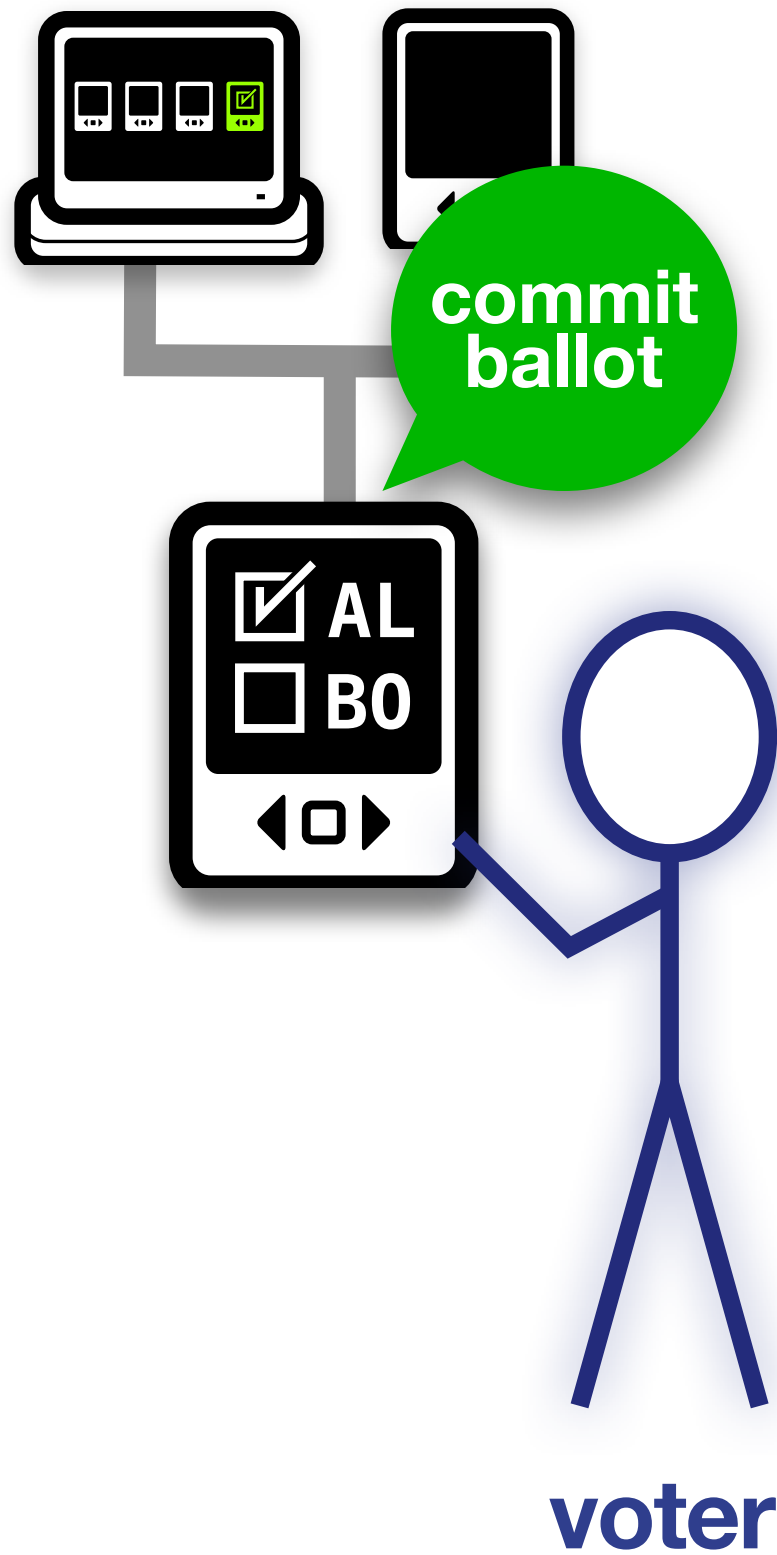


# polling place

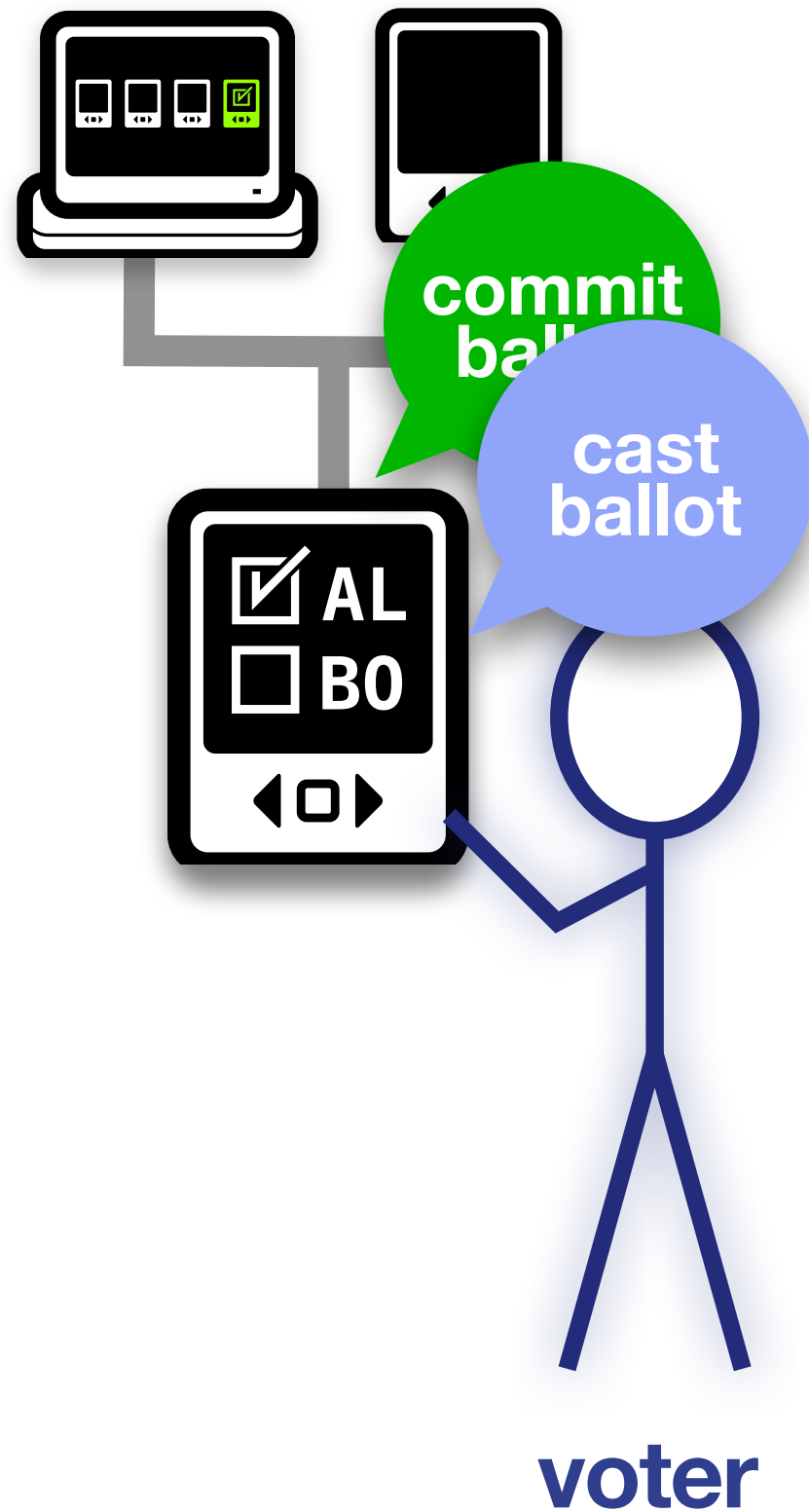


voter

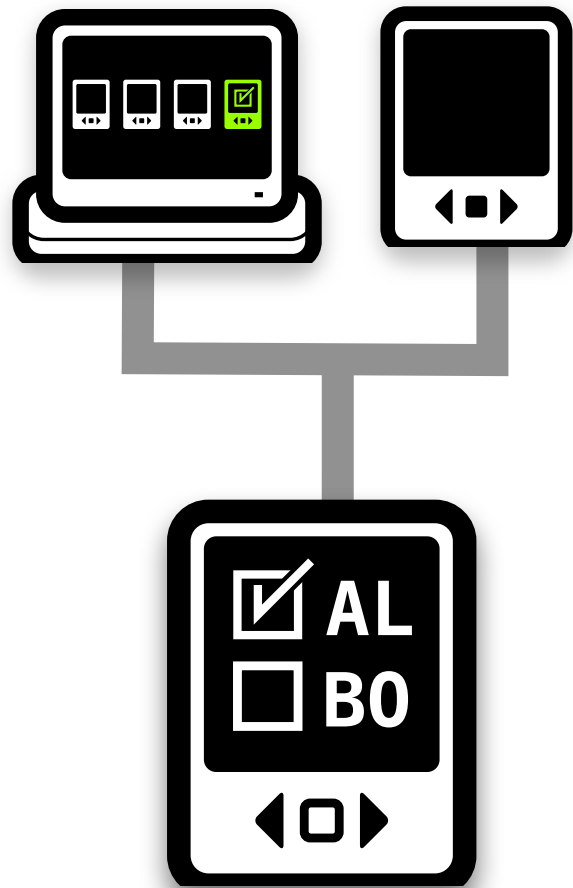
# polling place



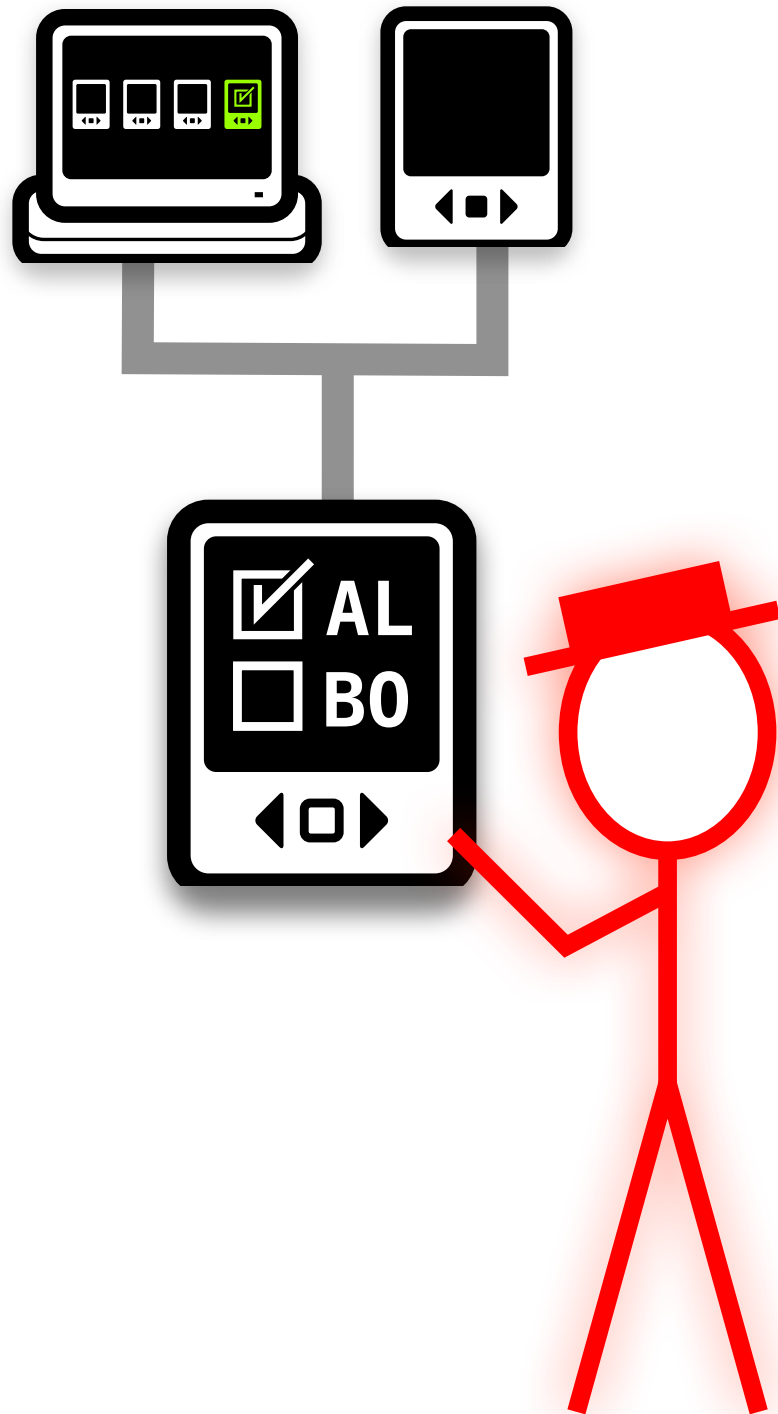
# polling place



# polling place

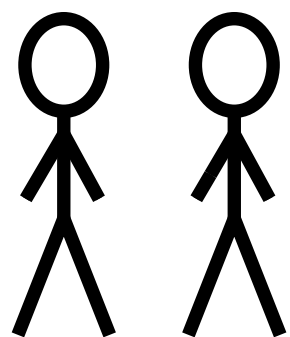
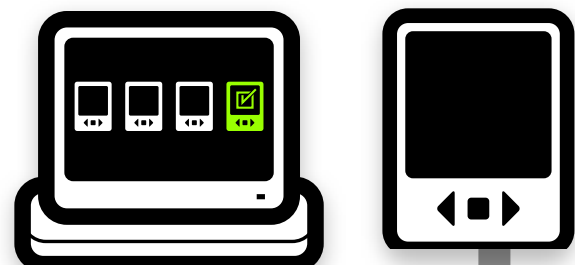


polling place



challenger

# polling place

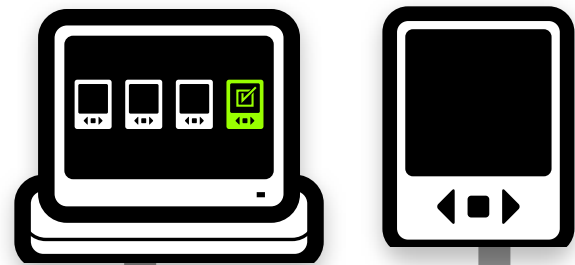


observers

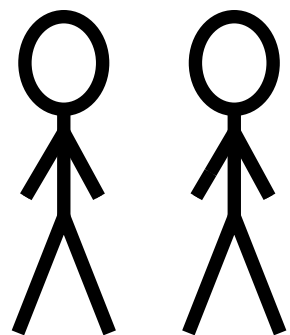
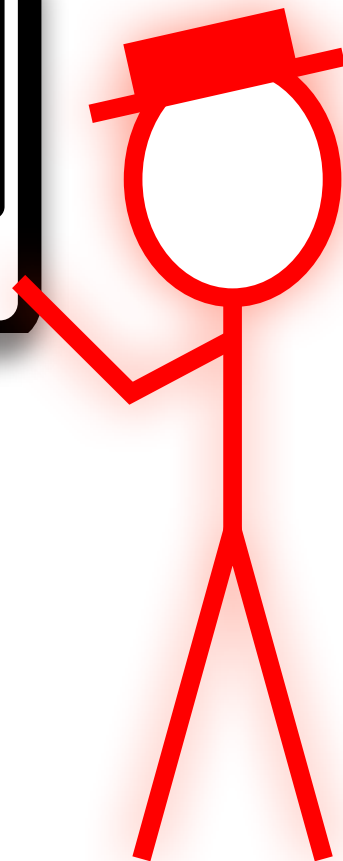
**challenger**



# polling place



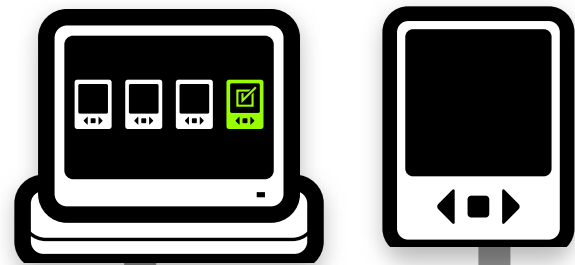
commit  
ballot



observers

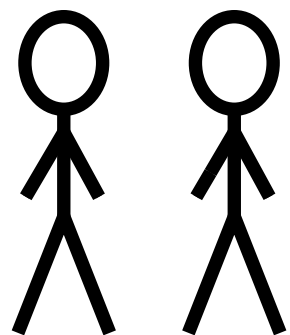
challenger

# polling place



commit  
ballot

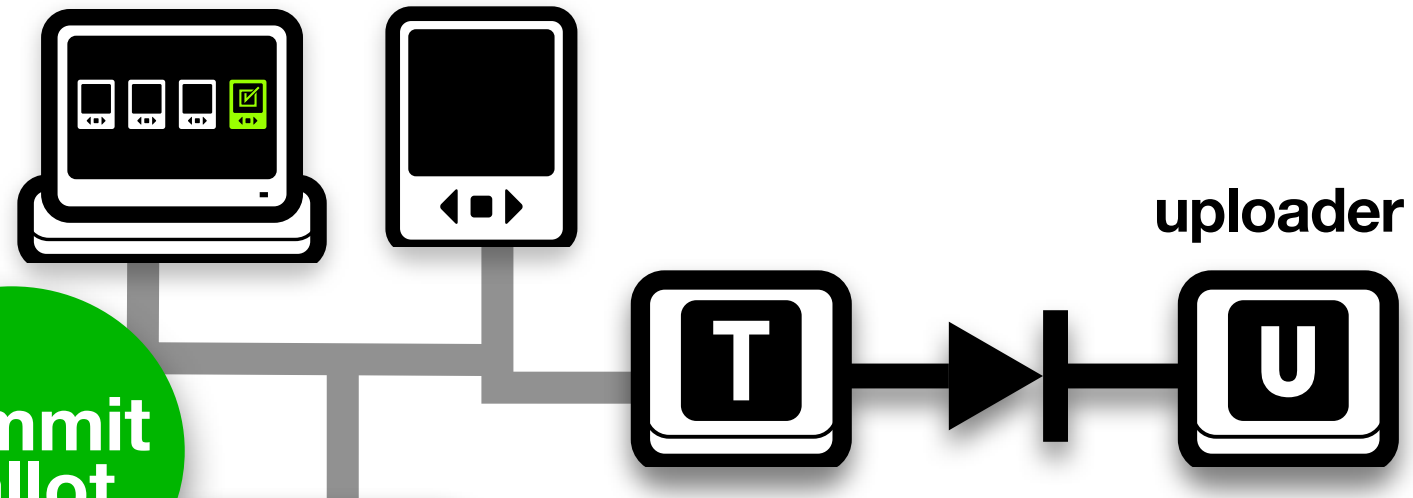
challenge  
response



observers

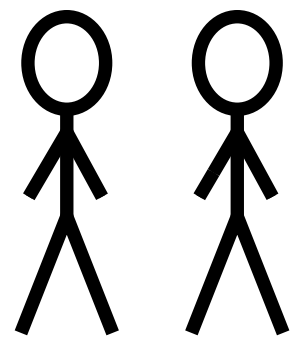
challenger

# polling place



commit  
ballot

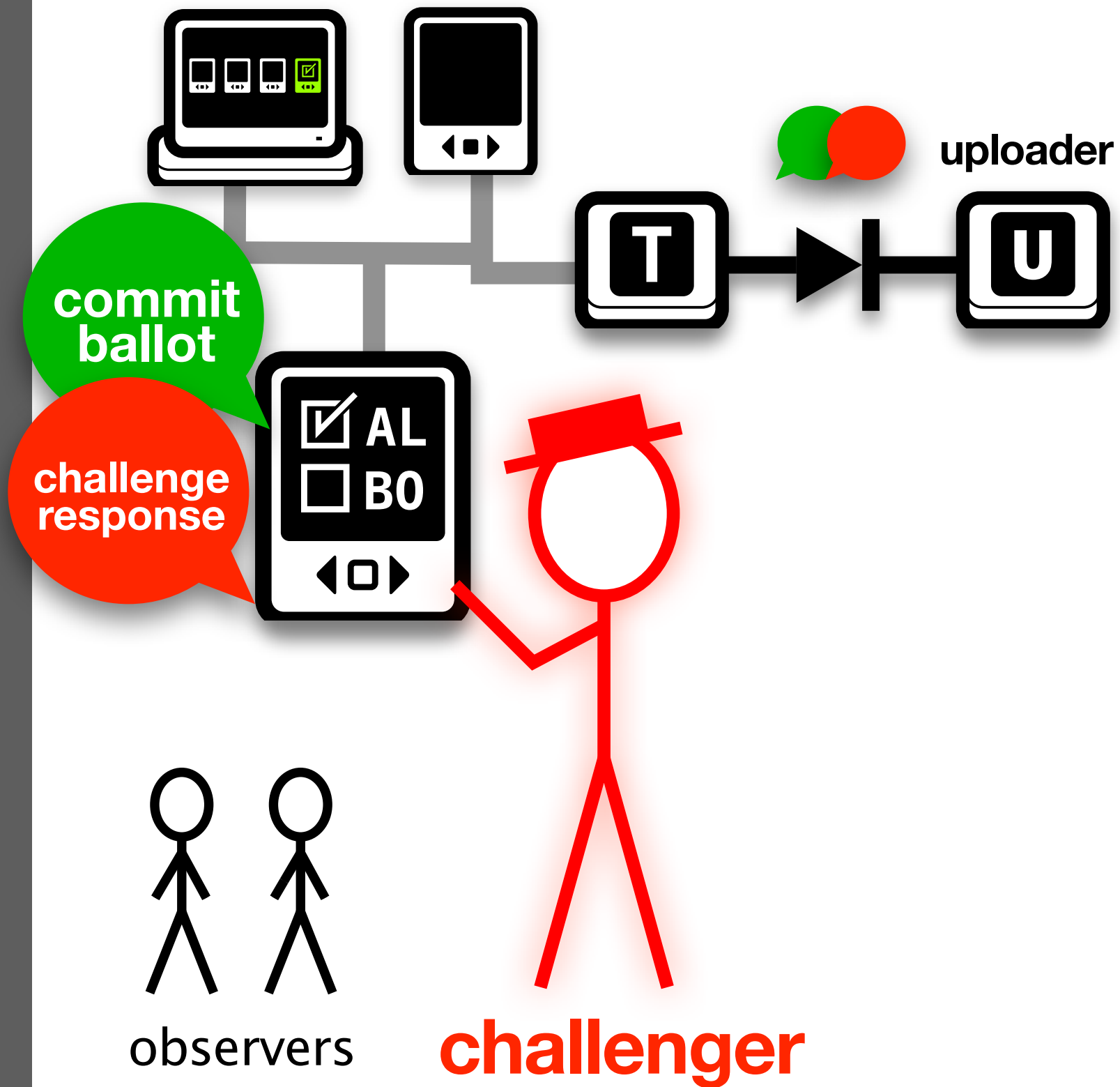
challenge  
response



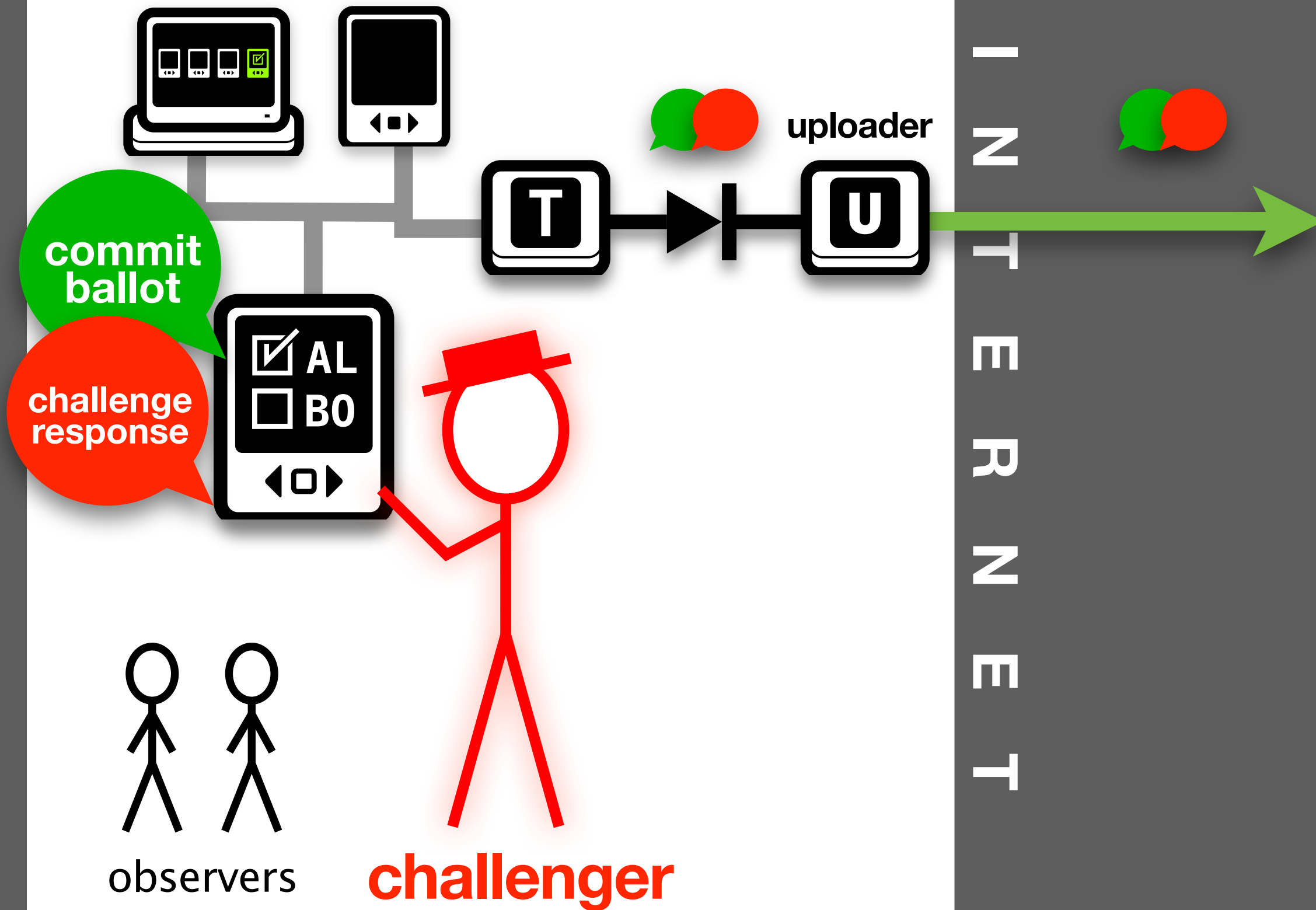
observers

challenger

# polling place

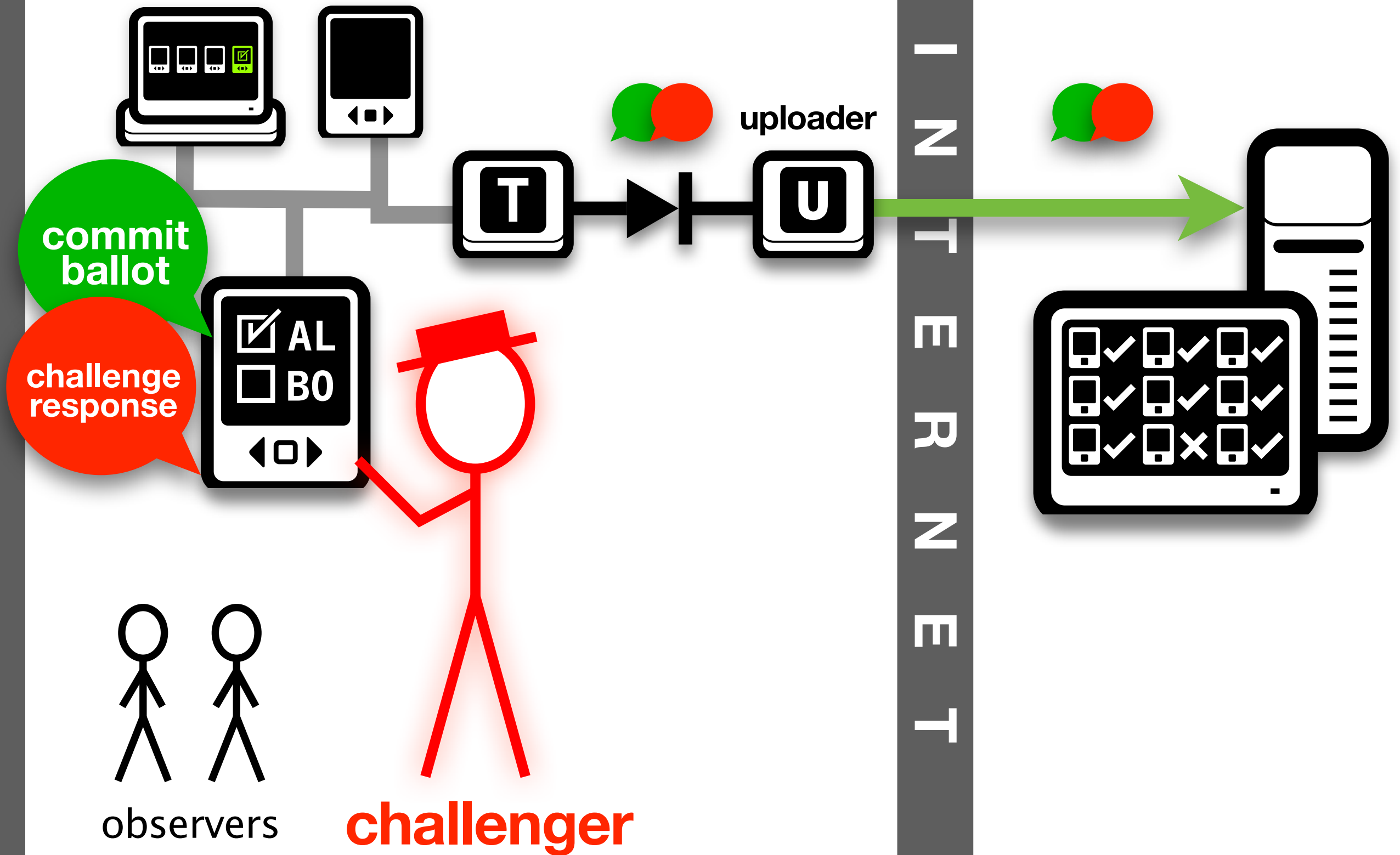


# polling place



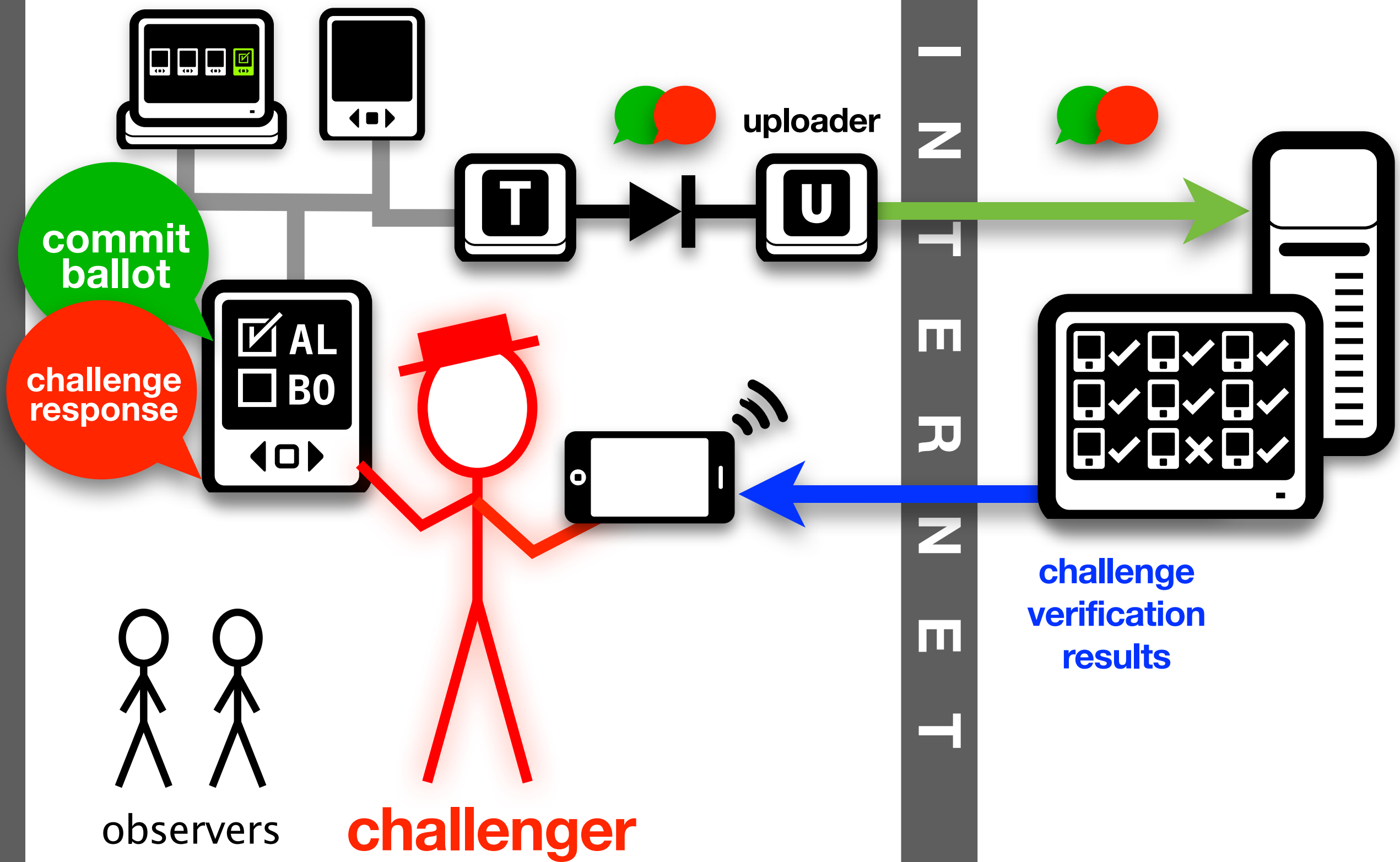
## polling place

## challenge center



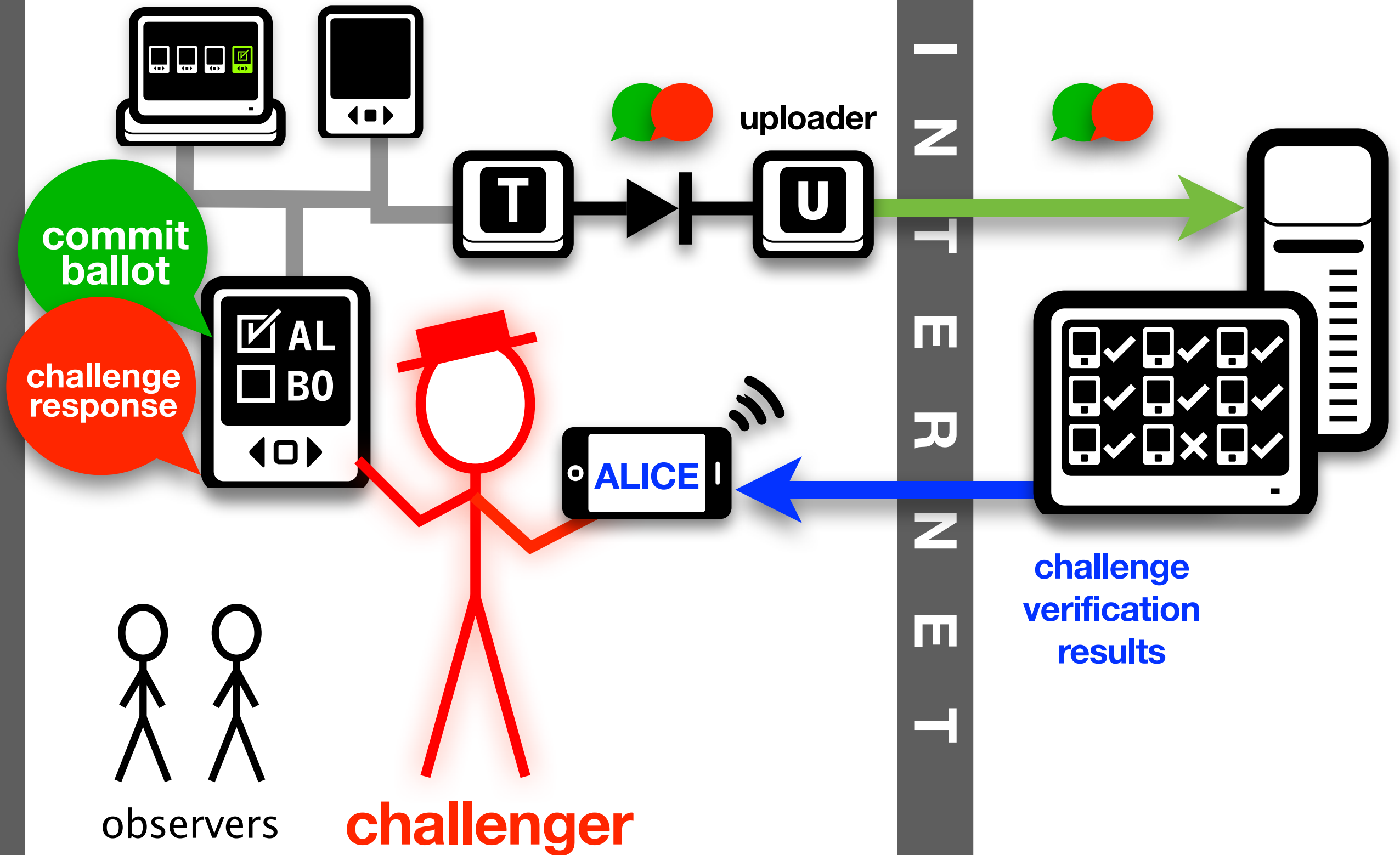
# polling place

# challenge center



## polling place

## challenge center





# Challenges in Auditorium

# Challenges in Auditorium

**When challenged,**

# Challenges in Auditorium

**When challenged,**

a VoteBox must **announce  $r$  on the network**

# Challenges in Auditorium

**When challenged,**

a VoteBox must **announce  $r$  on the network**

Irrevocable thanks to the properties of Auditorium

# Challenges in Auditorium

**When challenged,**

a VoteBox must **announce  $r$  on the network**

Irrevocable thanks to the properties of Auditorium

We still need help decrypting the commitment, even given  **$r$**

# Challenges in Auditorium

**When challenged,**

a VoteBox must **announce  $r$  on the network**

Irrevocable thanks to the properties of Auditorium

We still need help decrypting the commitment, even given  $r$

**If we are careful, we can send challenges offsite**

# Challenges in Auditorium

**When challenged,**

a VoteBox must **announce  $r$  on the network**

Irrevocable thanks to the properties of Auditorium

We still need help decrypting the commitment, even given  $r$

**If we are careful, we can send challenges offsite**

Allow a third party to assist in verifying the challenge

# Challenges in Auditorium

**When challenged,**

a VoteBox must **announce  $r$  on the network**

Irrevocable thanks to the properties of Auditorium

We still need help decrypting the commitment, even given  $r$

**If we are careful, we can send challenges offsite**

Allow a third party to assist in verifying the challenge

Trusted by the challenger!





# **Ballot challenges:**

**Ballot challenges:**  
**cast-as-intended verification**

**Ballot challenges:**  
**cast-as-intended verification**  
**preserving privacy**

**Ballot challenges:**  
cast-as-intended verification  
preserving privacy  
without artificial test conditions.

UI.

# pre-rendered user interfaces

# pre-rendered user interfaces

**very restricted UI functions**



# pre-rendered user interfaces

**very restricted UI functions**

**next\_event ( )** → keyboard or (x, y) input



# pre-rendered user interfaces

**very restricted UI functions**

**next\_event()** → keyboard or (x, y) input

**blit**(bitmap, x, y)



# pre-rendered user interfaces

**very restricted UI functions**

**next\_event()** → keyboard or (x, y) input

**blit**(bitmap, x, y)

**what's not here?**



# pre-rendered user interfaces

**very restricted UI functions**

**next\_event()** → keyboard or (x, y) input

**blit**(bitmap, x, y)



**what's not here?**

windowing system; widgets; fonts & text rendering

# pre-rendered user interfaces

**very restricted UI functions**

**next\_event()** → keyboard or (x, y) input

**blit**(bitmap, x, y)



**what's not here?**

windowing system; widgets; fonts & text rendering

**result**

# pre-rendered user interfaces

**very restricted UI functions**

**next\_event()** → keyboard or (x, y) input

**blit**(bitmap, x, y)



**what's not here?**

windowing system; widgets; fonts & text rendering

**result**

less code to inspect, certify, and trust

# pre-rendered user interfaces

**very restricted UI functions**

**next\_event()** → keyboard or (x, y) input

**blit**(bitmap, x, y)



**what's not here?**

windowing system; widgets; fonts & text rendering

**result**

less code to inspect, certify, and trust

**inspiration: Pvote**

pioneering work on PRUI in e-voting

[Yee, EVT '06 & '07]

**President and Vice President of the United States**  
*Race 1 of 27*

To make your choice, click on the candidate's name or on the box next to his/her name. A green checkmark will appear next to your choice. If you want to change your choice, just click on a different candidate or box.

<b>President and Vice President of the United States</b> <i>(You may vote for one)</i>		
<input type="checkbox"/>	Gordon Bearce Nathan Maclean	REP
<input type="checkbox"/>	Vernon Stanley Albury Richard Rigby	DEM
<input checked="" type="checkbox"/>	Janette Froman Chris Aponte	LIB

Click to go back to instructions

← Previous Page

Click to go foward to next race

Next Page →

STEP 1  
Read Instructions

You are now on  
STEP 2  
Make your choices

STEP 3  
Review your choices

STEP 4  
Record your vote



STEP 1  
Read Instructions  
LABEL ID=L10

You are now on  
STEP 2  
Make your choices  
LABEL ID=L13

STEP 3  
Review your choices  
LABEL ID=L14

STEP 4  
Back to choices  
LABEL ID=L16

BACKGROUND  
LABEL ID=L1

LABEL ID=L51

LABEL ID=L52

To make your choice, click on the candidate's name or on the box next to his/her name. A green checkmark will appear next to your choice. If you want to change your choice, click on a different candidate or box.

President and Vice President of the United States	
(You may vote for one)	
LABEL ID=L50	
<input type="checkbox"/> Gordon Bearce Norman Maclean	REP
GROUP TOGGLE BUTTON ID=B100	
<input type="checkbox"/> Vernon Stanley Albury Richard Wright	DEM
GROUP TOGGLE BUTTON ID=B101	
<input checked="" type="checkbox"/> Janette Froman Chris Aponte	LIB
GROUP TOGGLE BUTTON ID=B102	

LABEL ID=L1002

Click to go back to instructions

← Previous Page  
PREV PG ID=L1000

LABEL ID=L1003

Click to go foward to next race

ID=L1001  
NEXT PG →

# VoteBox ballot creator

## GUI tool for creating pre-rendered ballots

this is where the complexity went

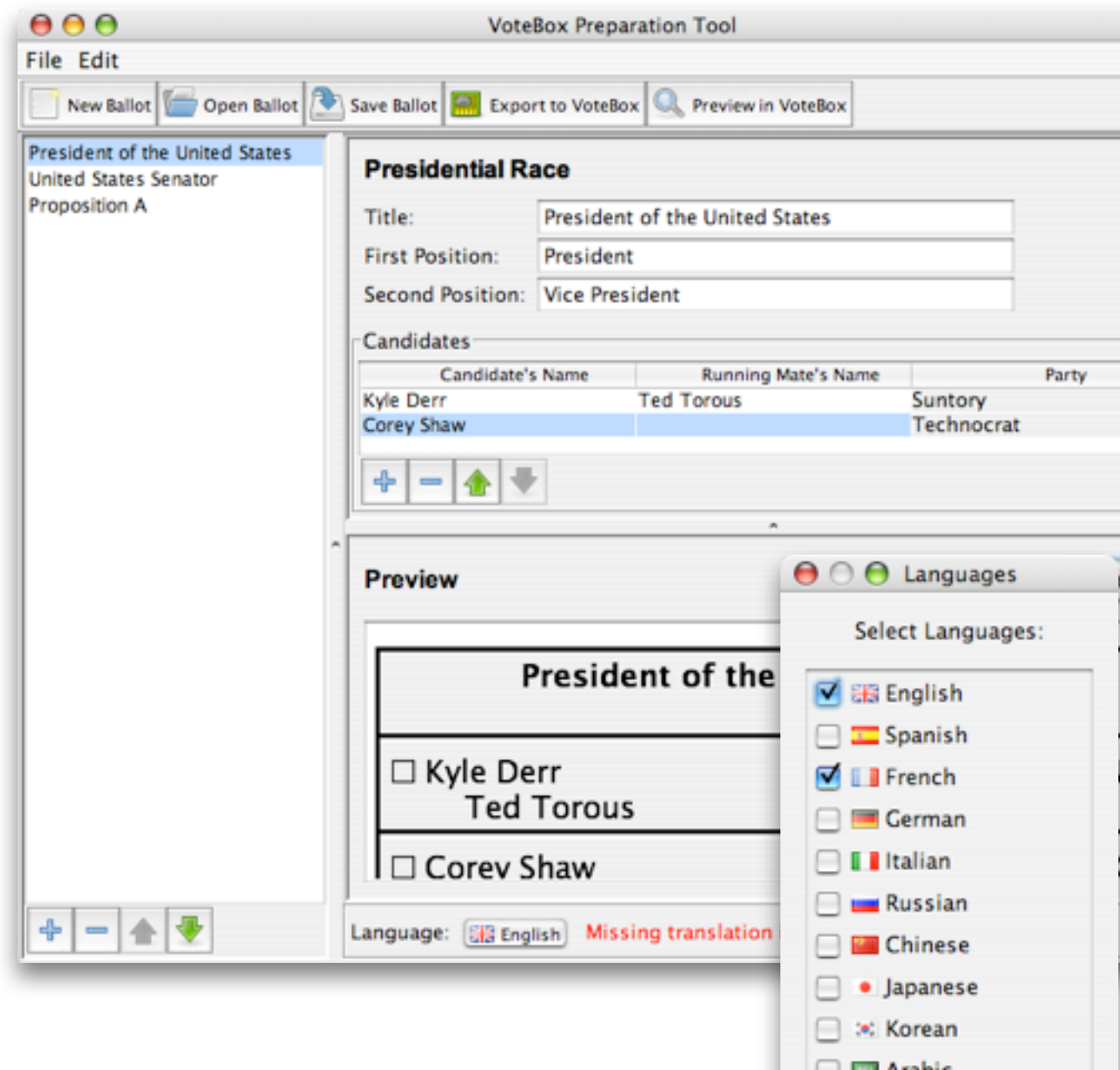
## Not in the TCB

we don't need to trust this software

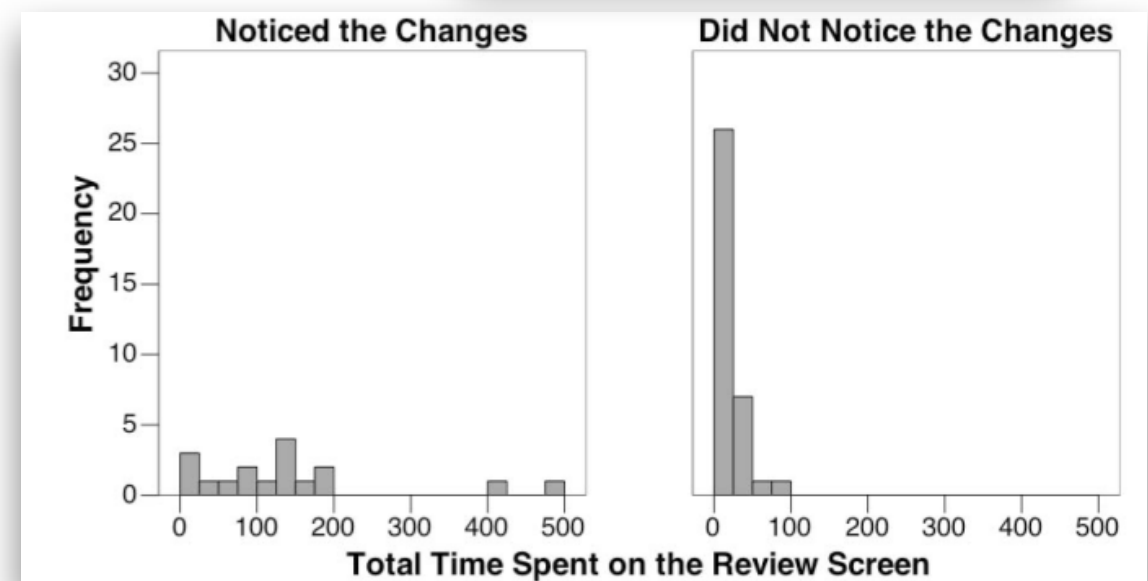
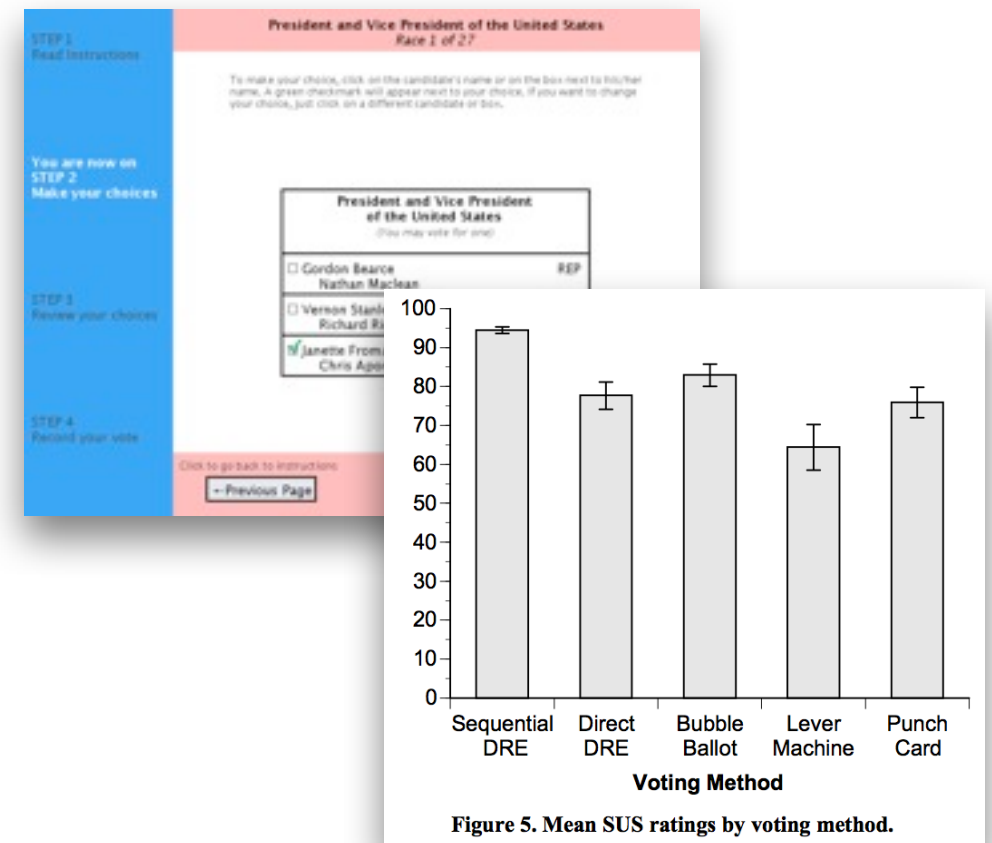
sufficient to verify that the output ballot is correct

## Flexibility

New ballot designs do not require changes to VoteBox — only the ballot creator



# HCI research

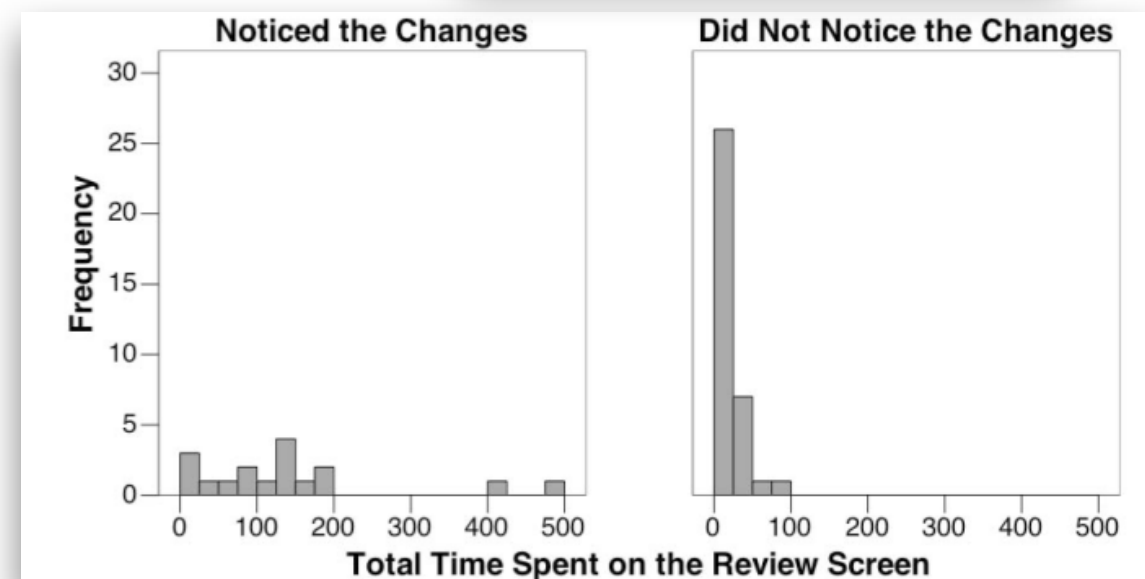
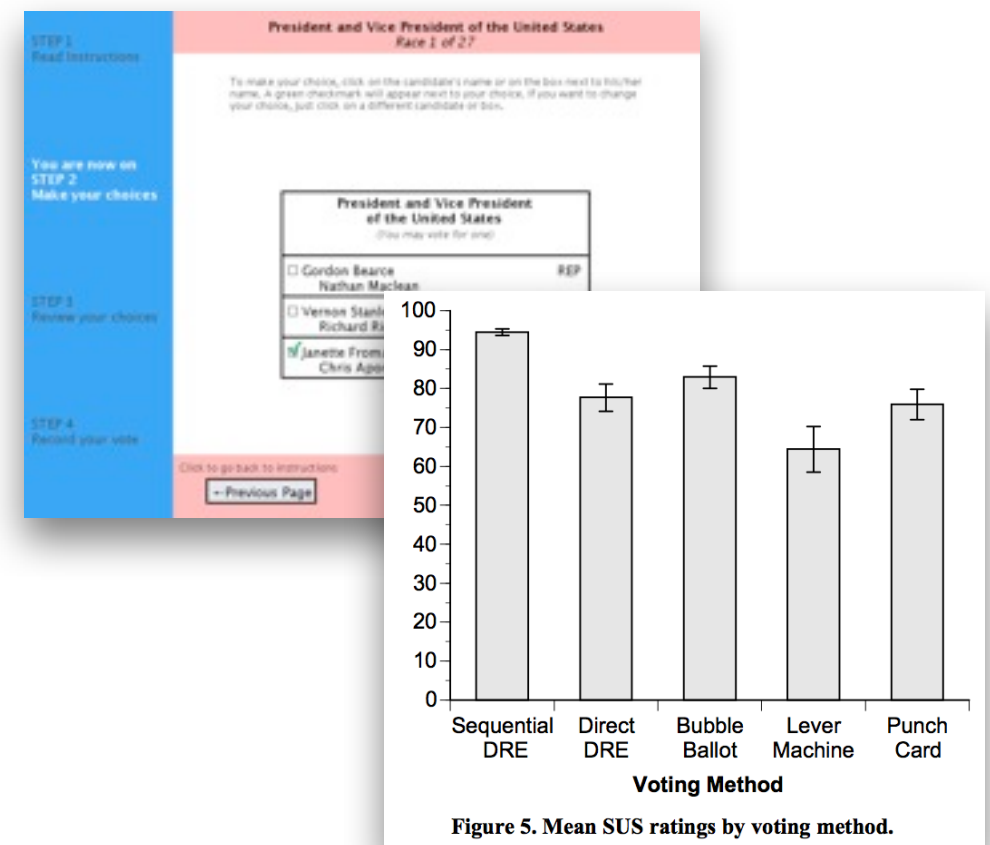


# HCI research

**VoteBox is a platform for human factors research & experimentation**

VoteBox's ballot designed jointly with Rice CHIL

special VoteBox-HF build includes extensive instrumentation for HCI work



# HCI research

**VoteBox is a platform for human factors research & experimentation**

VoteBox's ballot designed jointly with Rice CHIL

special VoteBox-HF build includes extensive instrumentation for HCI work

**Questions answered include:**

“Do users prefer DREs?”

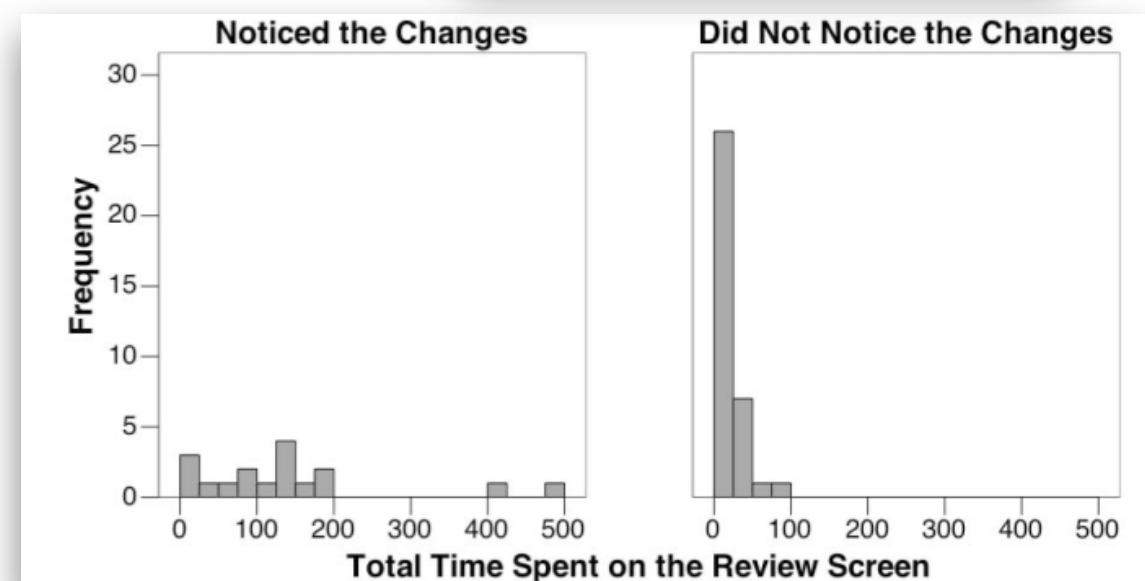
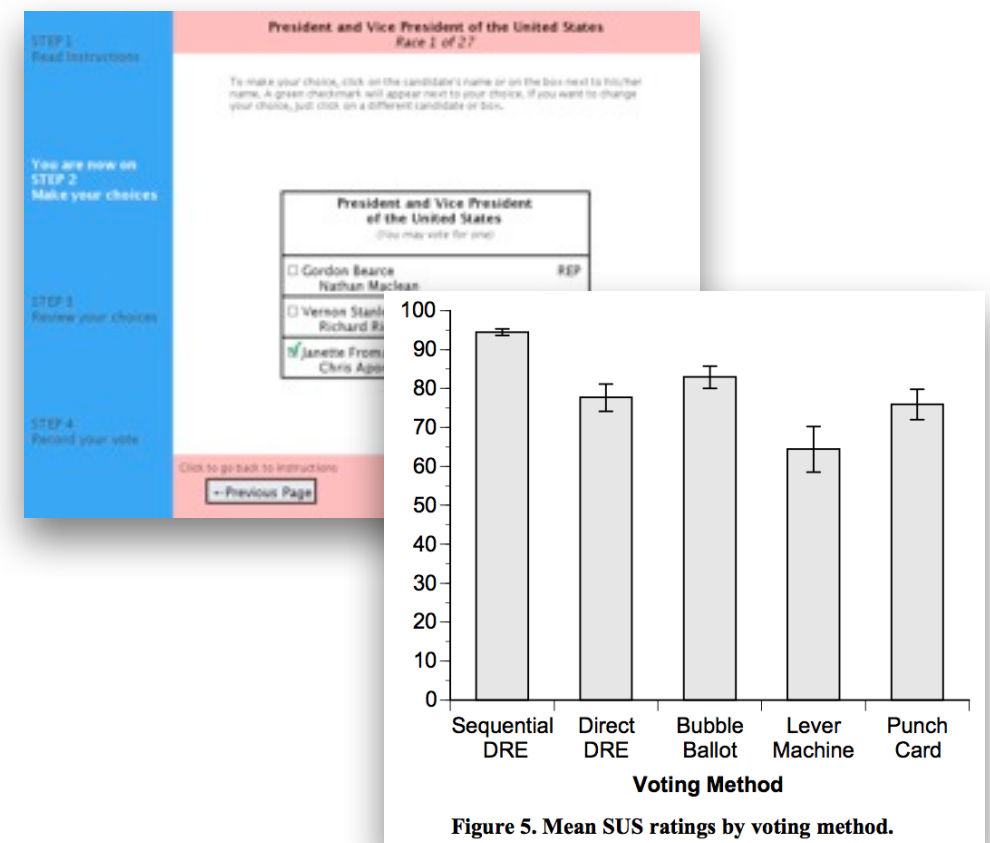
“Do DREs improve performance?”

“Do voters notice if DREs malfunction?”

**Software engineering implications**

Instrumentation is “evil” code from a security standpoint

Compile-time processing to exclude all HCI code from normal VoteBox builds



# Extensions.

internet voting  
from home is  
**a bad idea**

remote voting  
can be  
**a good idea**

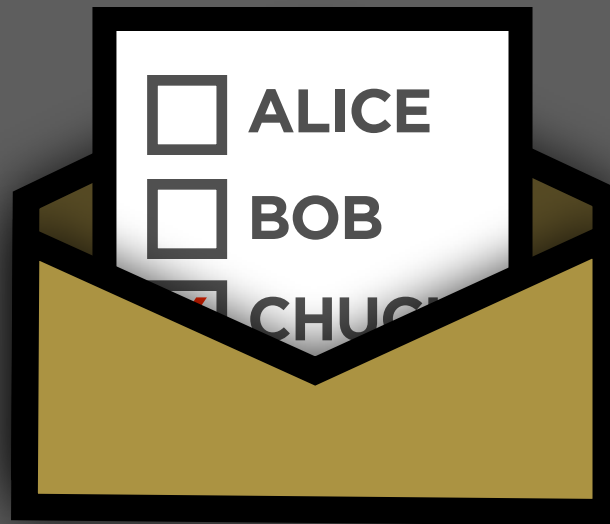
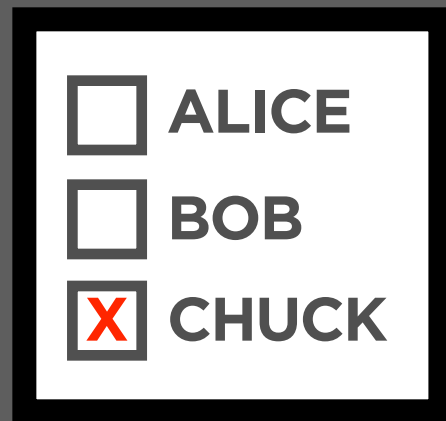


**“postal voting”**

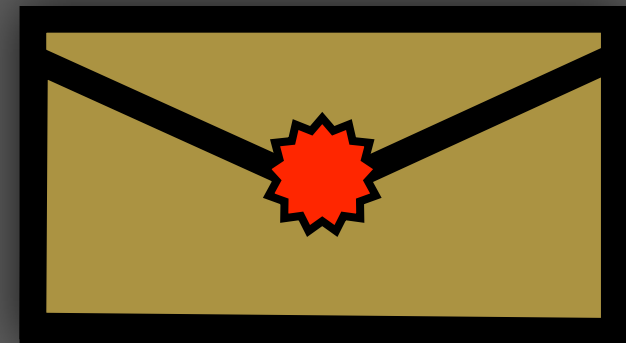
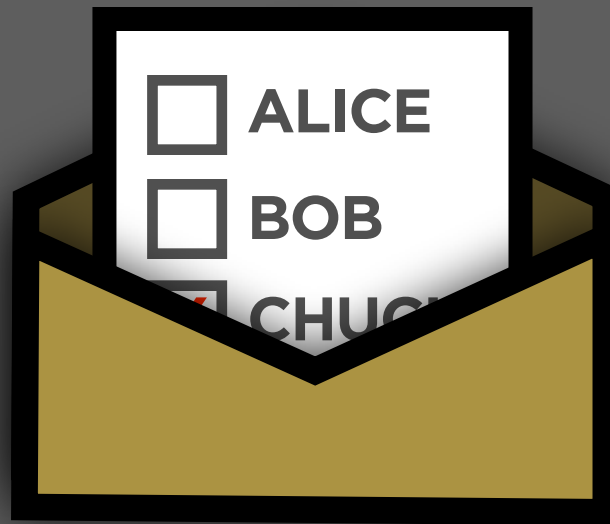
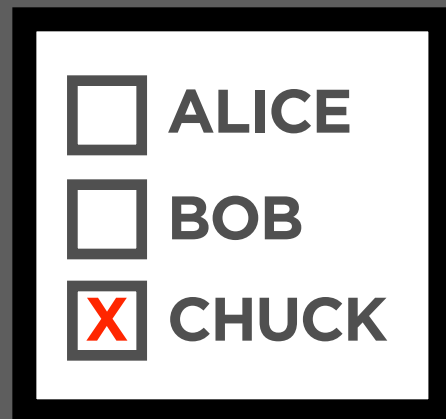
# “postal voting”

<input type="checkbox"/>	ALICE
<input type="checkbox"/>	BOB
<input checked="" type="checkbox"/>	CHUCK

# “postal voting”

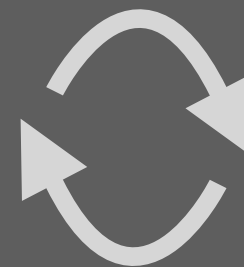
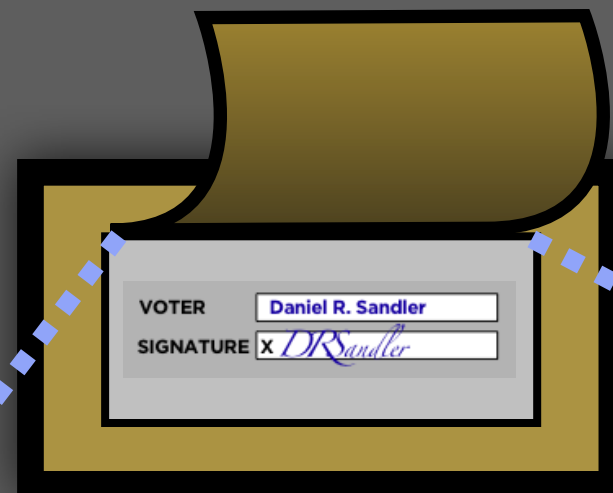
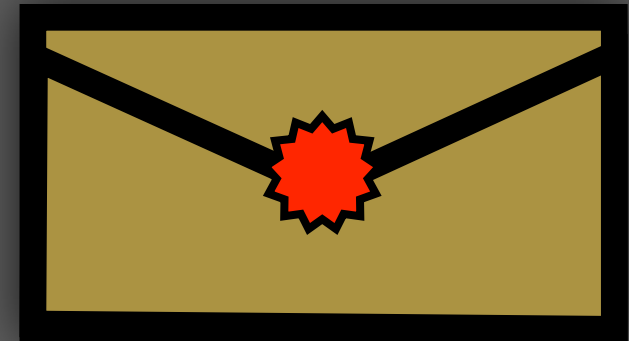
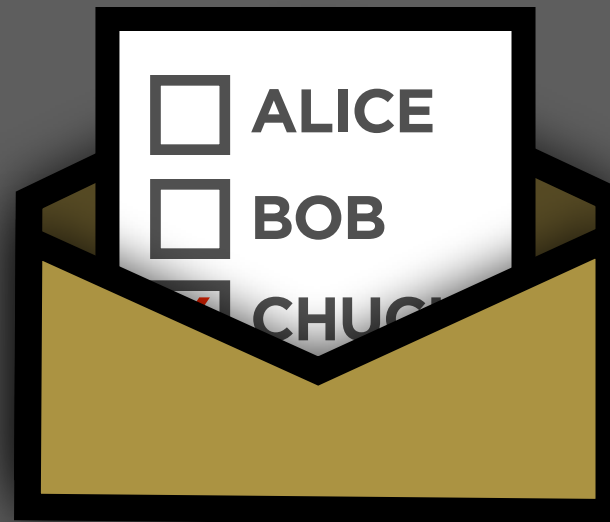


# “postal voting”



# “postal voting”

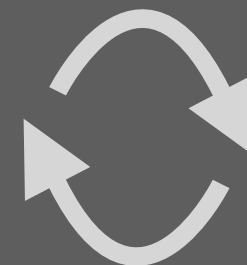
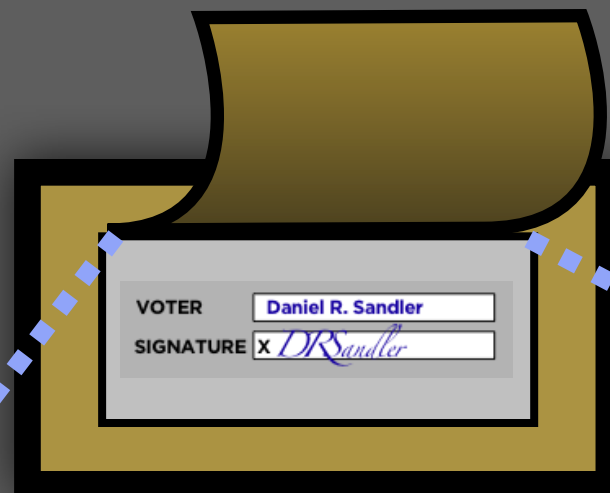
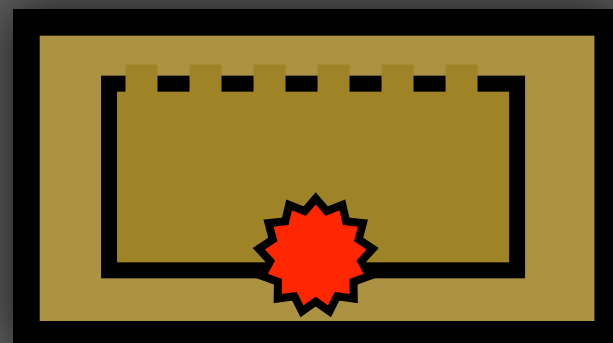
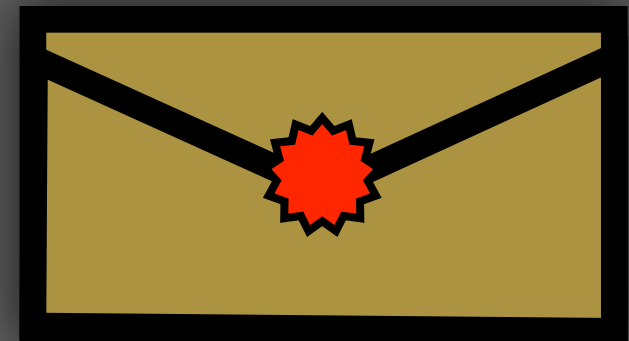
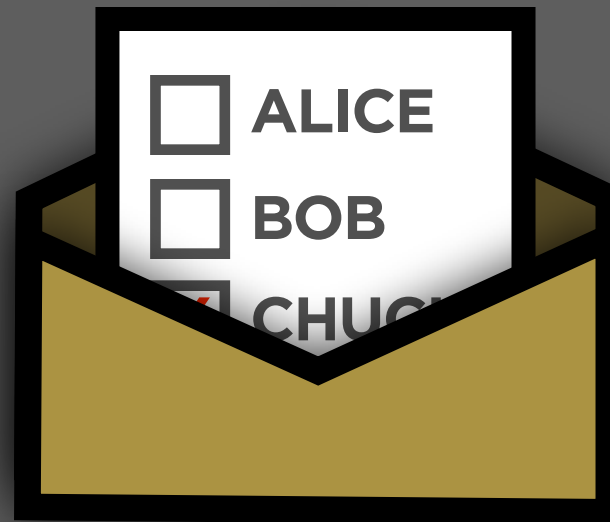
<input type="checkbox"/>	ALICE
<input type="checkbox"/>	BOB
<input checked="" type="checkbox"/>	CHUCK



VOTER	Daniel R. Sandler
SIGNATURE	X <i>DRSandler</i>

# “postal voting”

<input type="checkbox"/>	ALICE
<input type="checkbox"/>	BOB
<input checked="" type="checkbox"/>	CHUCK



VOTER	Daniel R. Sandler
SIGNATURE	X <i>DR Sandler</i>

# we can do this with VoteBox

Conventional: postal system

Replace with: Auditorium network

Conventional: sealed envelopes

Replace with: encryption





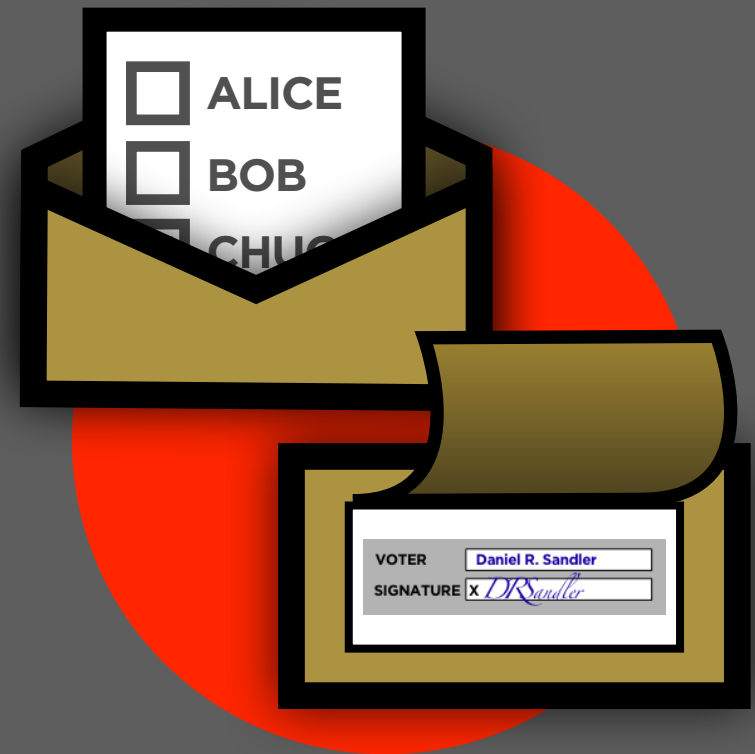


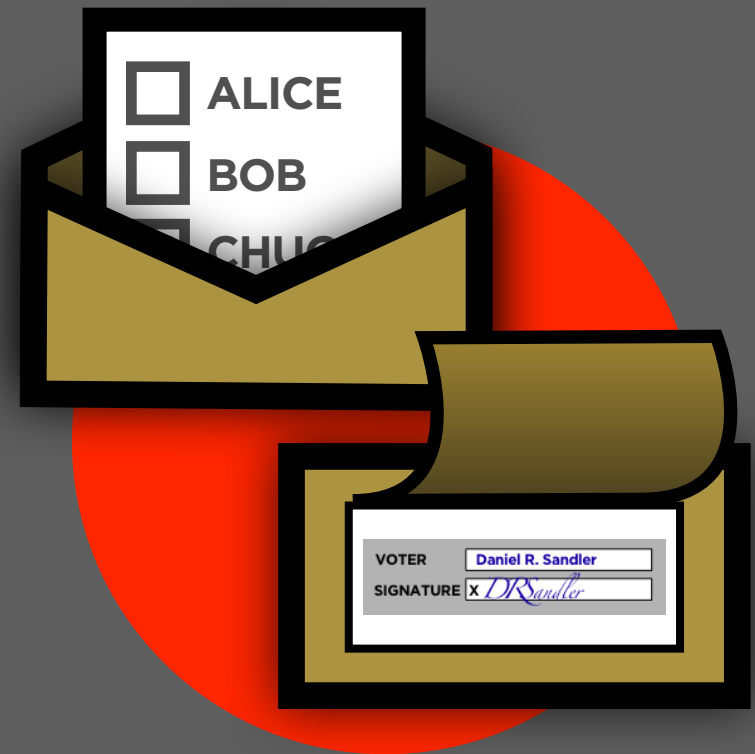


=



=





# Benefits of the networked remote polling place

## **Fast**

Ballot types from home precinct

Cast ballots back to home precinct

## **Robust**

Post and networks both lossy

...but networks can retransmit

## **More secure**

Choices cannot be observed while in transit

Crypto protects vote secrecy (even from officials)

# 3. Conclusion



why?



lots of research on  
**individual pieces**  
of the e-voting problem





**VoteBox** integrates  
these techniques in a  
**single system.**

D. R. Sandler, K. Derr, D. S. Wallach. **VoteBox: A tamper-evident, verifiable electronic voting system.** In USENIX Security 2008.



**VoteBox** integrates  
these techniques in a  
**single system.**

**Auditorium (Sandler et al.)**

robustness, tamper-evidence

D. R. Sandler, K. Derr, D. S. Wallach. **VoteBox: A tamper-evident, verifiable electronic voting system.** In USENIX Security 2008.



**VoteBox** integrates  
these techniques in a  
**single system.**

**Auditorium (Sandler et al.)**

robustness, tamper-evidence

**Ballot challenge (new adaptation of Benaloh)**

verifiability

D. R. Sandler, K. Derr, D. S. Wallach. **VoteBox: A tamper-evident, verifiable electronic voting system.** In USENIX Security 2008.



# **VoteBox** integrates these techniques in a **single system.**

## **Auditorium (Sandler et al.)**

robustness, tamper-evidence

## **Ballot challenge (new adaptation of Benaloh)**

verifiability

## **Other ingredients**

PRUI; HCI instrumentation

**D. R. Sandler, K. Derr, D. S. Wallach. VoteBox: A tamper-evident, verifiable electronic voting system. In USENIX Security 2008.**



# **VoteBox** integrates these techniques in a **single system.**

## **Auditorium (Sandler et al.)**

robustness, tamper-evidence

## **Ballot challenge (new adaptation of Benaloh)**

verifiability

## **Other ingredients**

PRUI; HCI instrumentation

## **Techniques suitable for integration with today's systems**

D. R. Sandler, K. Derr, D. S. Wallach. **VoteBox: A tamper-evident, verifiable electronic voting system.** In USENIX Security 2008.





PRIVACY, SECURITY, POLITICS AND CRIME ONLINE

« High Court Asks Obama to Weigh In on Copyright Case; Conflict of Interest Brews | Main | Video: Sneaky New ATM Skimmer Found in Pennsylvania »

## Voting Machine Audit Logs Raise More Questions about Lost Votes in CA Election

By Kim Zetter

January 13, 2009 | 12:00:00 PM

Categories: [E-Voting](#), [Election '08](#)

Computer audit logs showing what occurred on a vote tabulation system that lost ballots in the November election are raising more questions not only about how the votes were lost, but also about the general reliability of voting system audit logs to record what occurs during an election and to ensure the integrity of results.

The logs, which Threat Level obtained through a public records request from Humboldt County, California, are produced by the Global Election Management System, the tabulation software, also known as GEMS, that counts the votes cast on all voting machines -- touch-screen and optical-scan machines -- made by Premier Election Solutions (formerly called Diebold Election Systems).

The logs are at the core of an investigation that the California secretary of state's office is conducting to determine why the [GEMS tabulation system deleted 197 ballots from the tallies of one precinct](#) in Humboldt County during the November 4 general election. But instead of providing transparency into what occurred on the system, the GEMS logs have so far only baffled state investigators. Deputy Secretary of State Lowell Finley has referred to the logs as "'Greek' to anyone other than a programmer."



<http://blog.wired.com/27bstroke6/2009/01/diebold-audit-l.html>



[« High Court Asks](#)[« Pop Superstar Sting Supports Pentagon Hacker, Condemns U.S. | Main | Pirate Bay Trial Ends; Verdict Due April 17 »](#)

PRIVACY, SECURITY, POLITICS AND CRIME ONLINE

## Voting Machine Report: Diebold Voting System Has 'Delete' Button for Erasing Audit Logs

By Kim Zetter

January

By Kim Zetter

March 03, 2009 | 7:30:17 PM

Categories: [E-Voting](#)

Computer audit logs show a voting system that lost ballots in an election, raising questions not only about the general reliability of voting systems but also about the security of the system during an election and the integrity of the results.

The logs, which Threat Level reported on last week, were requested from Humboldt County by the Global Election Management System (GEMS), that company's touch-screen and optical scanning system (formerly called Premier Election Solutions).

The logs are at the core of a report released by the secretary of state's office last week. The report, titled "tabulation system deleted," says that the system in Humboldt County deleted audit logs instead of providing them. The GEMS logs have so far been reviewed by the Secretary of State Lowell P. Wehner, but no one other than a pro-

After three months of investigation, California's secretary of state has released a report examining why a voting system made by Premier Election Solutions (formerly known as Diebold) lost about 200 ballots in Humboldt County during November's presidential election.

But the most startling information in [the state's 13-page report \(.pdf\)](#) is not why the system lost votes, which [Wired.com previously covered in detail](#), but that some versions of Diebold's vote tabulation system, known as the Global Election Management System (Gems), include a button that allows someone to delete audit logs from the system.

Auditing logs are required under the federal voting-system guidelines, which are used to test and qualify voting systems for use in elections. The logs record changes and other events that occur on voting systems to ensure the integrity of elections and help determine what occurred in a system when something goes wrong.

Poster

Status

Started At

Jobs Since Start

Queued

Peak

Last

Current

Last Job

Last Alert

12/24/08 09:02:16 Poster Starting

12/24/08 09:02:56 Poster Stopped

12/24/08 09:20:20 Poster Starting

12/24/08 09:21:00 Poster Stopped

12/24/08 09:22:13 Recovering 0 job(s)

12/24/08 09:22:13 Poster Starting

12/24/08 09:22:53 Poster Stopped

12/24/08 09:46:07 Poster Starting

12/24/08 09:46:47 Poster Stopped

12/24/08 09:49:21 Poster Starting

12/24/08 09:50:01 Poster Stopped

Print

Save As...

Clear

Close

<http://blog.wired.com/27bstroke6/2009/03/ca-report-finds.html><http://blog.wired.com/27bstroke6/2009/03/ca-report-finds.html>



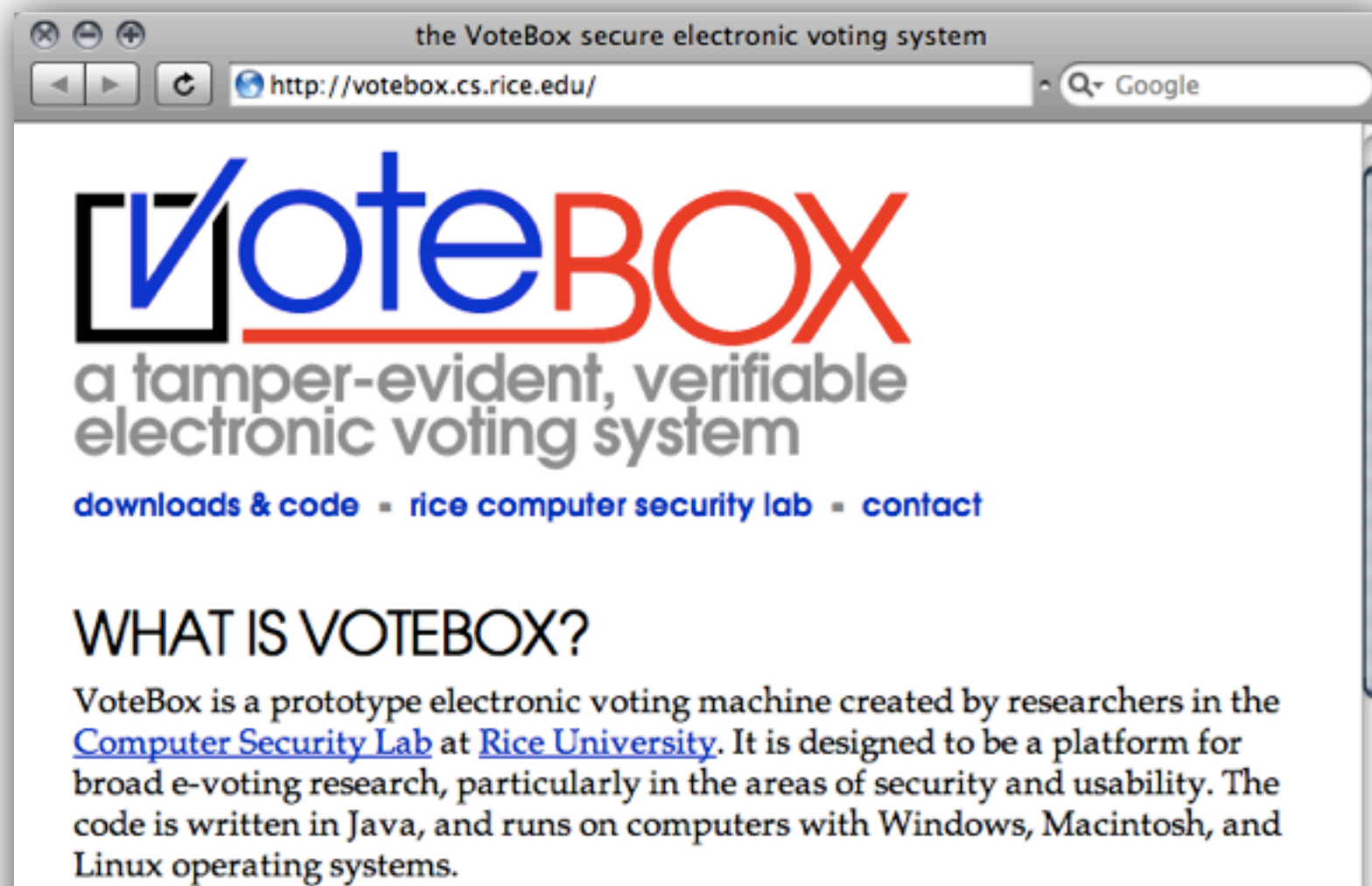
# platform



## VoteBox is open-source

[votebox.cs.rice.edu](http://votebox.cs.rice.edu) & [code.google.com/p/votebox](http://code.google.com/p/votebox)

suitable for further research, HCI experiments, class projects, security analysis





# thanks

## co-authors

Scott Crosby, Kyle Derr, Daniel Sandler,  
Ted Torous

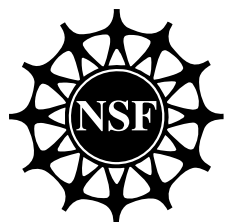
## contributors to VoteBox

Emily Fortuna, George Mastrogiannis,  
Kevin Montrose, Corey Shaw

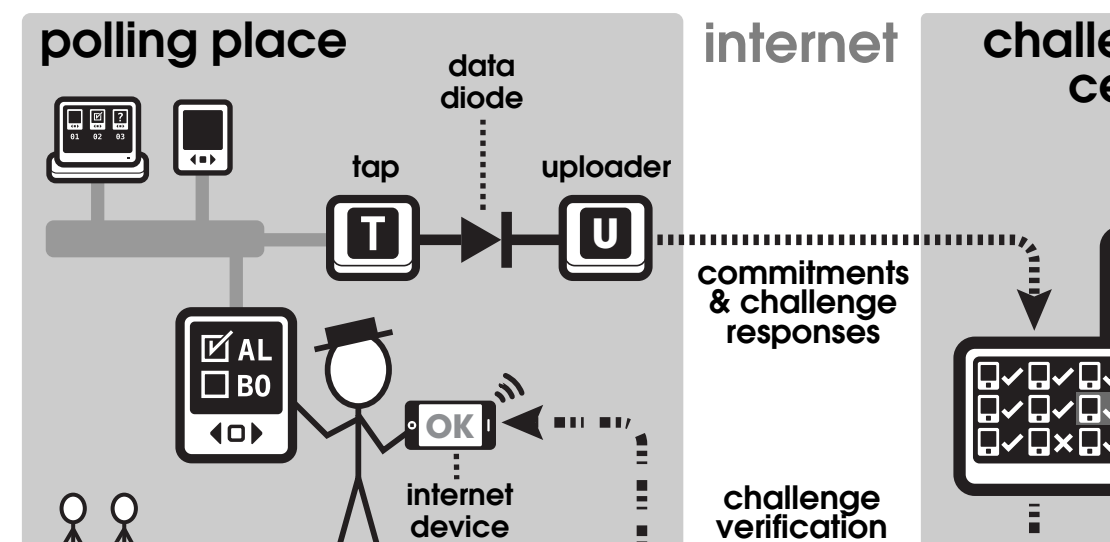
## CHIL

Mike Byrne, Sarah Everett, Kristen Greene

## NSF/ACCURATE

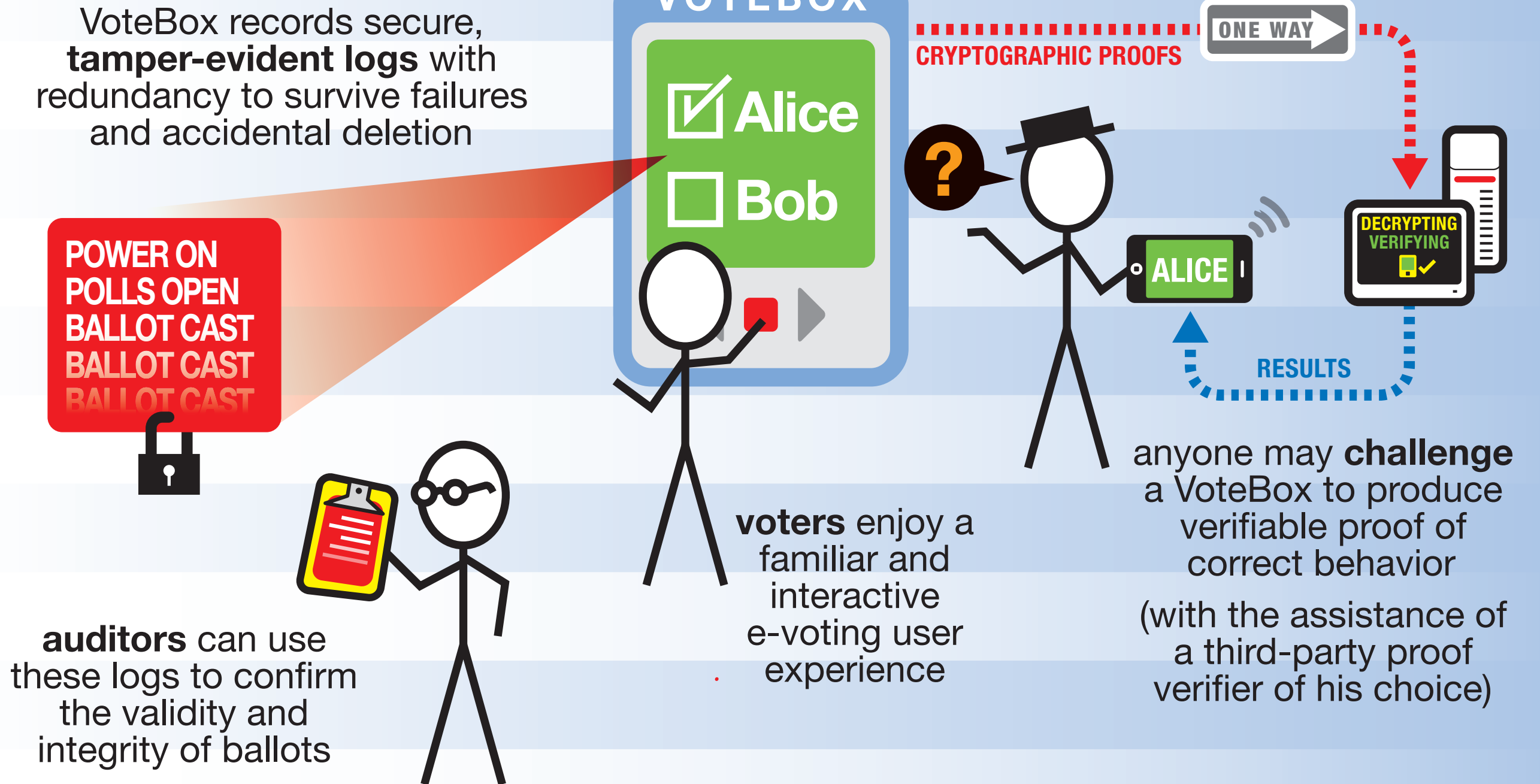


RICE





**VoteBox** is an ACCURATE research project exploring **designs for new e-voting systems** that are trustworthy, reliable, and usable.



on the web: [accurate-voting.org](http://accurate-voting.org) & [votebox.cs.rice.edu](http://votebox.cs.rice.edu)

NSF “highlights” graphic, 2009



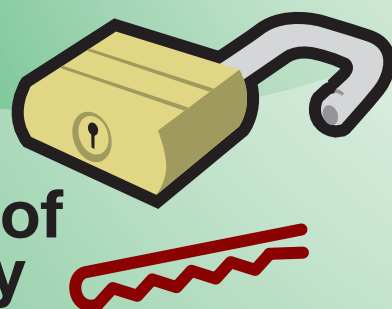


**ACCURATE center** researchers have participated in studies finding **serious flaws** in **current commercial DRE voting systems** that make them vulnerable to malfunctions or deliberate manipulation by attackers.



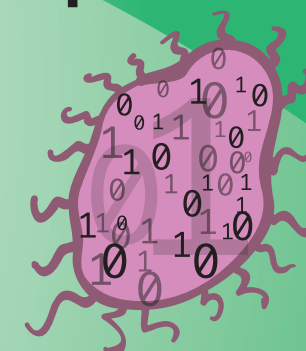
comprehensive audits  
in California and Ohio

missing or  
incorrect use of  
cryptography



malfunctions  
can destroy  
or reveal  
ballots

voting  
machine  
viruses  
possible



poor software  
engineering practices

# electronic voting in peril

NSF “highlights” graphic, 2009



**(assorted backup slides)**

**Beyond.**

# Beyond VoteBox

**Other systems need assurance, auditability, transparency**

## **Future directions**

- **email** (*auditability, document retention*)
- **web 2.0 publishing** (*reliability, openness*)
- **collaborative tools** (*event ordering, change tracking*)
- **gaming** (*ordering, cheat resistance & audit*)



# email

## **entangled mailboxes**

apply the tamper-evidence and timeline properties of auditorium to email records that must be highly auditable and recoverable

## **applications**

Sarbanes-Oxley compliance

patents/notarization

Presidential records

status: *planning*



# micropublishing

## rapid short messaging

e.g. Twitter, Facebook

opt-in/social subscription

current systems are  
centralized, isolated, and  
limited

## research opportunity

distributed, *secure*

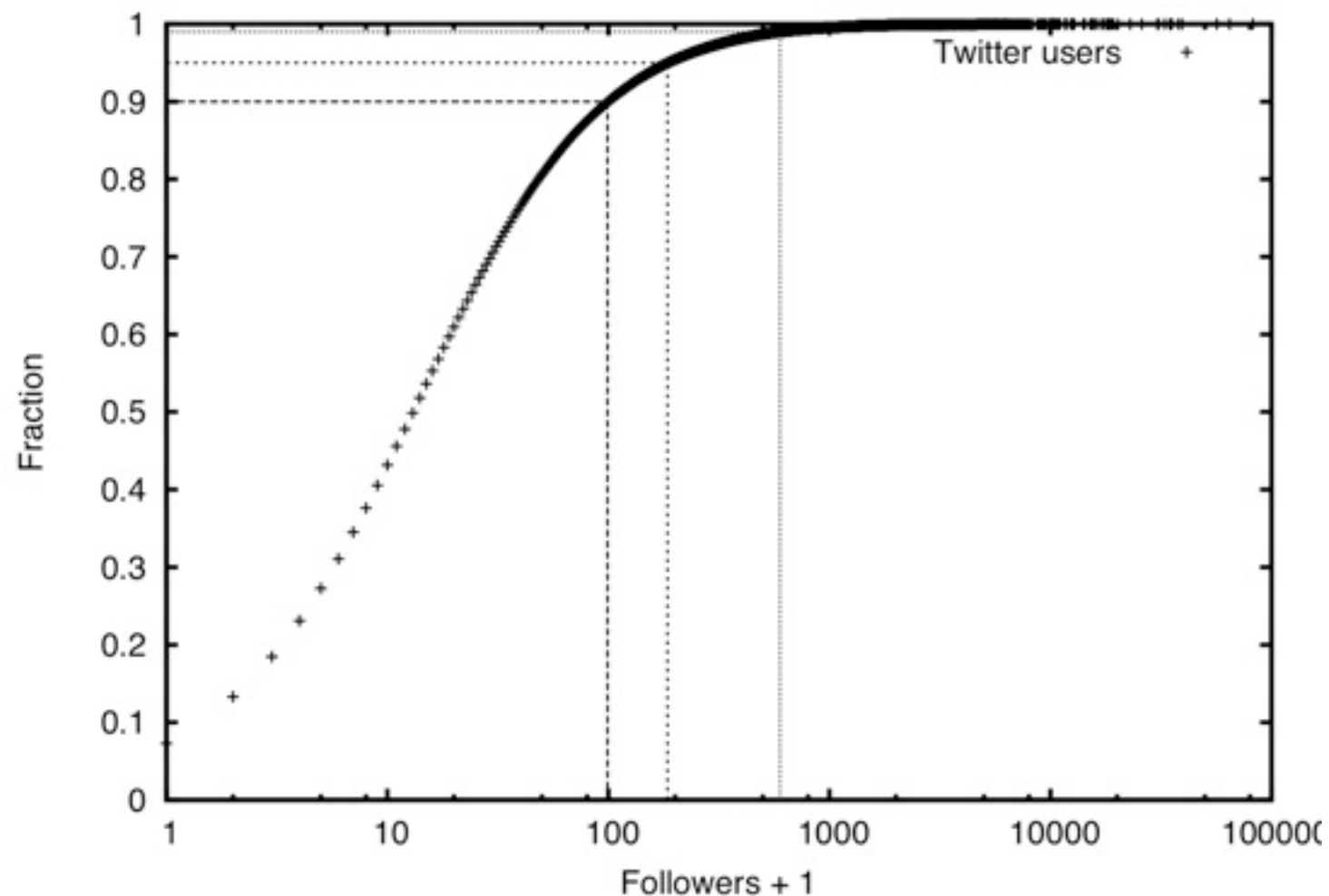
micropublishing

Auditorium-style timeline

entanglement

scaling to millions of users

continued...



(data from Twitter, collected 2008)

# micropublishing (2)

## FETHR

micropublishing API

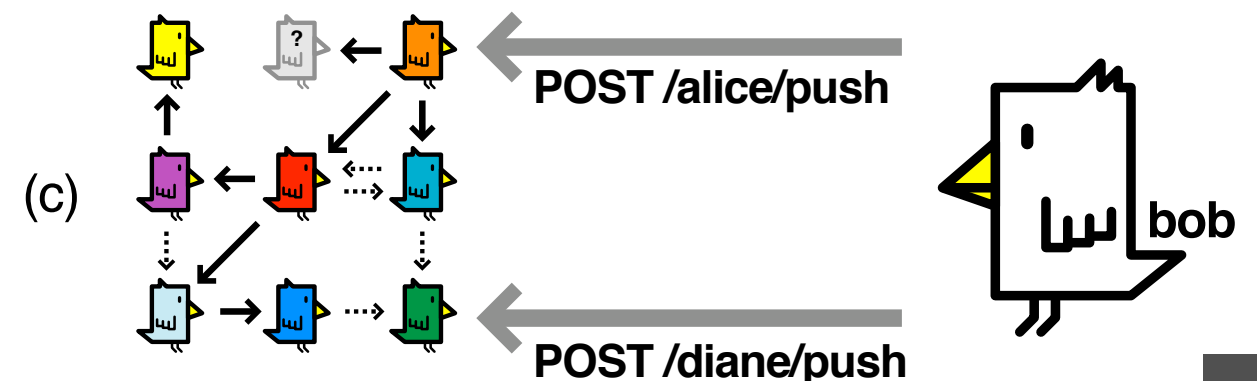
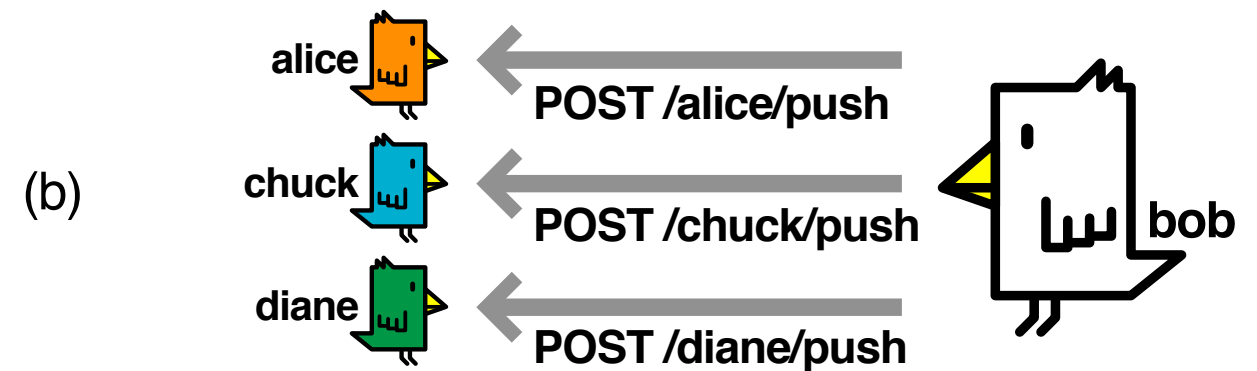
updates pushed to  
subscribers via HTTP POST

entanglement between  
publishers

gossip to assist in message  
distribution

prototype implementation:  
Birdfeeder (brdfdr.com)

status: *in progress; submitted  
(IPTPS)*

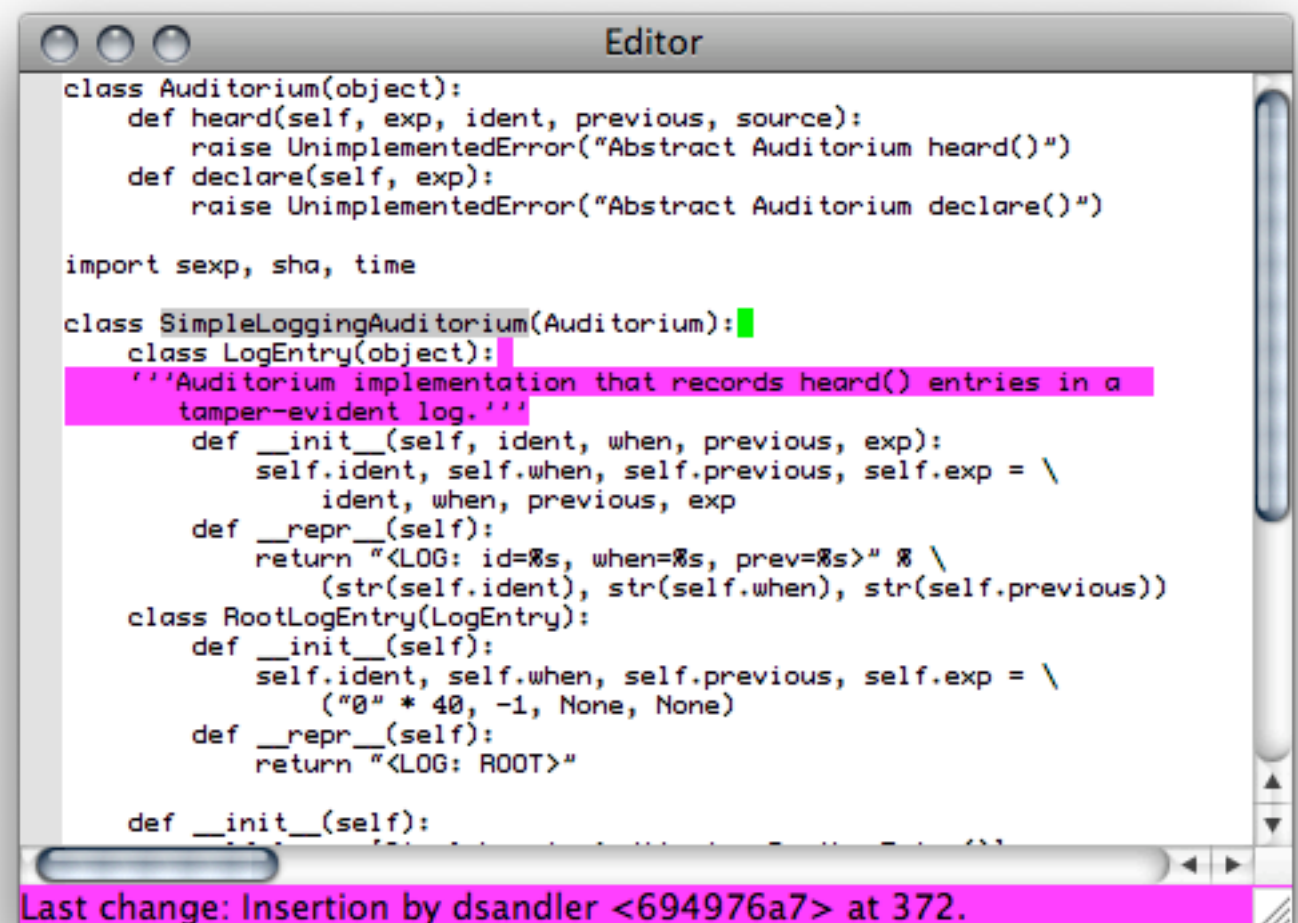


# collaborative tools

**timeline entanglement to represent sequence of edits or actions**

ordering of events corresponds neatly to causality in groupware

status: *prototyped*



```
class Auditorium(object):
    def heard(self, exp, ident, previous, source):
        raise NotImplementedError("Abstract Auditorium heard()")
    def declare(self, exp):
        raise NotImplementedError("Abstract Auditorium declare()")

import sexp, sha, time

class SimpleLoggingAuditorium(Auditorium):
    class LogEntry(object):
        '''Auditorium implementation that records heard() entries in a
        tamper-evident log.'''
        def __init__(self, ident, when, previous, exp):
            self.ident, self.when, self.previous, self.exp = \
                ident, when, previous, exp
        def __repr__(self):
            return "<LOG: id=%s, when=%s, prev=%s>" % \
                (str(self.ident), str(self.when), str(self.previous))
    class RootLogEntry(LogEntry):
        def __init__(self):
            self.ident, self.when, self.previous, self.exp = \
                ("0" * 40, -1, None, None)
        def __repr__(self):
            return "<LOG: ROOT>"

    def __init__(self):
        self.log = []
```

Last change: Insertion by dsandler <694976a7> at 372.

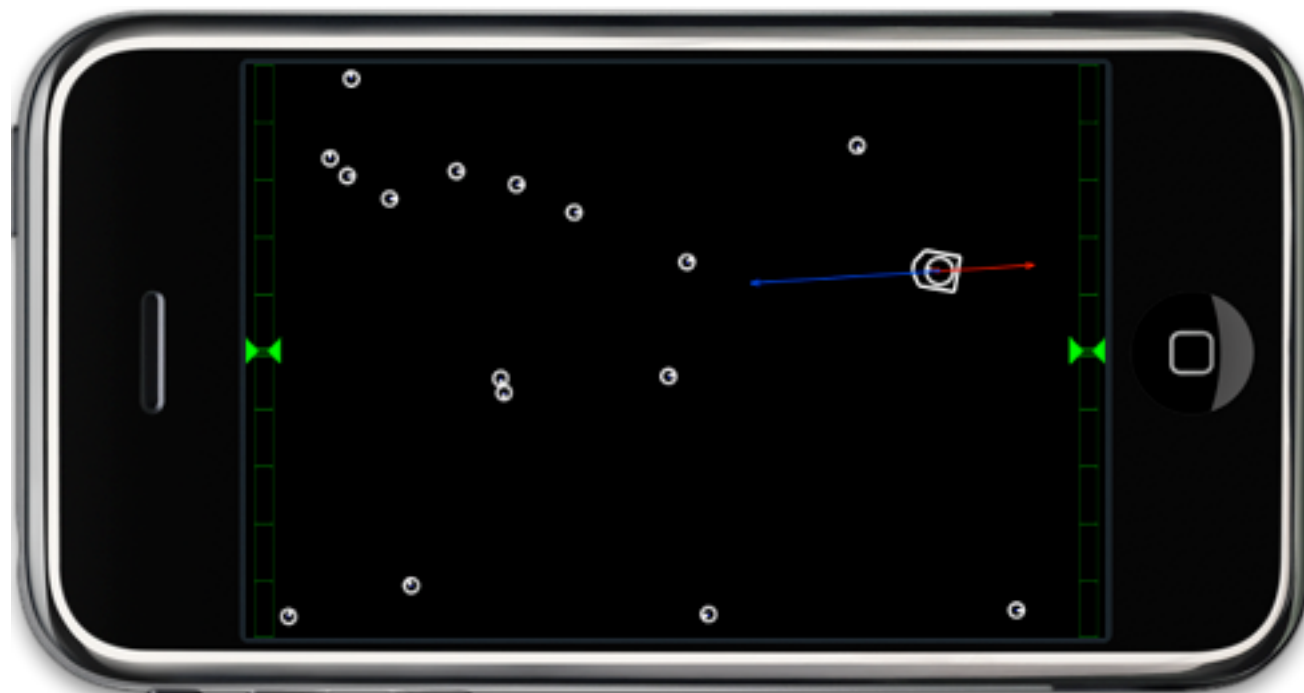
# networked games

## Auditorium-style communication for participants

gossip for decentralization, reliability

hash chains forward & backward (move commitment, history authentication)

secure logs for post-facto audit of suspected cheating



# Fancy Cryptography

# Violation of encryption semantics?

**If I know  $M_1$  and  $M_2$  and  $E(M_1) \oplus E(M_2) = E(M_1 M_2)$   
then I can find other messages where  
I know their encryption!**

# Solution: Padding

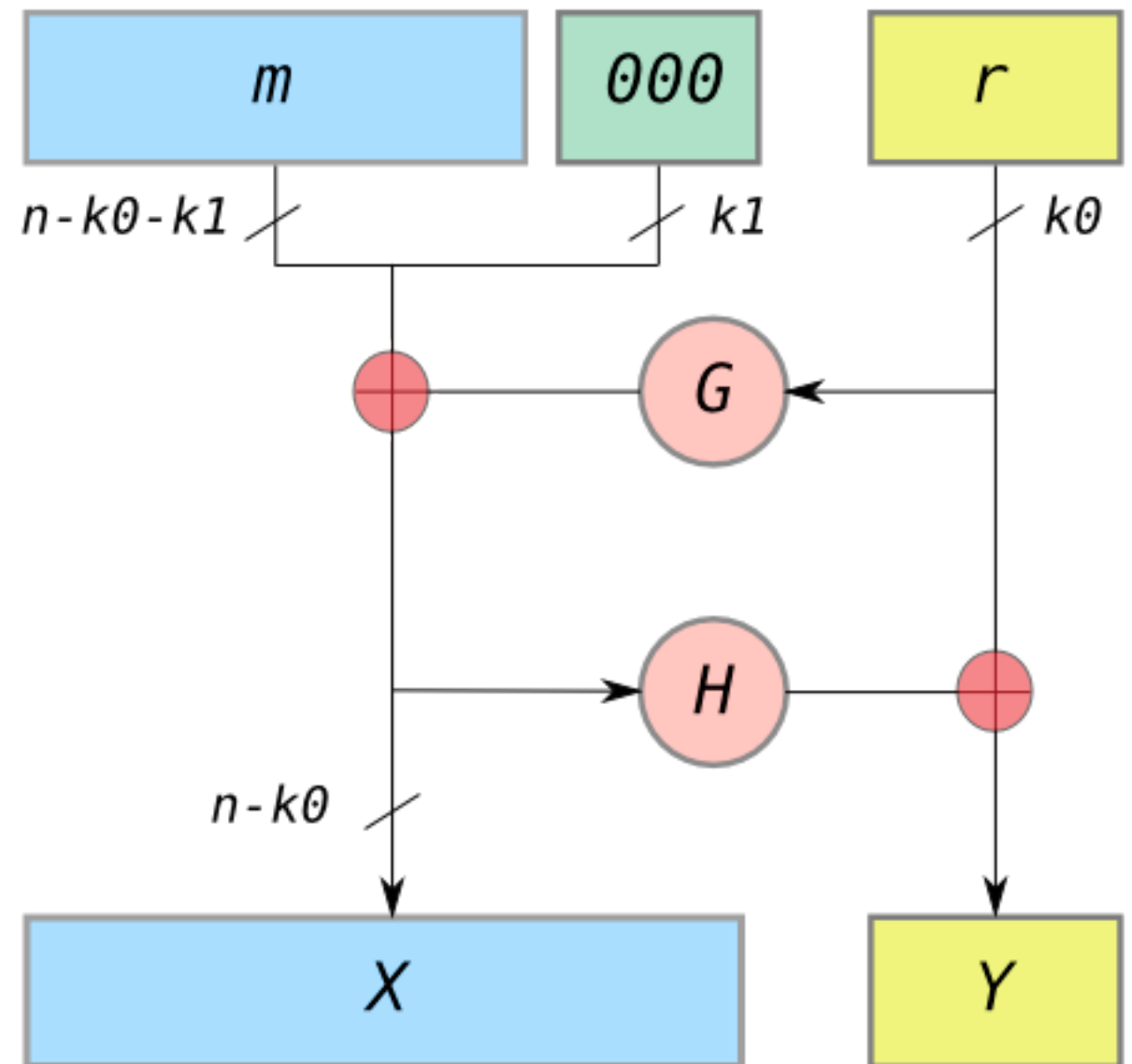
## Optimal Asymmetric Encryption Padding (OAEP) - *Belare and Rogaway (1995)*

$m$  - message (plaintext)

$r$  - random number

$G, H$  - cryptographic hash functions

$X, Y$  - the message that gets encrypted





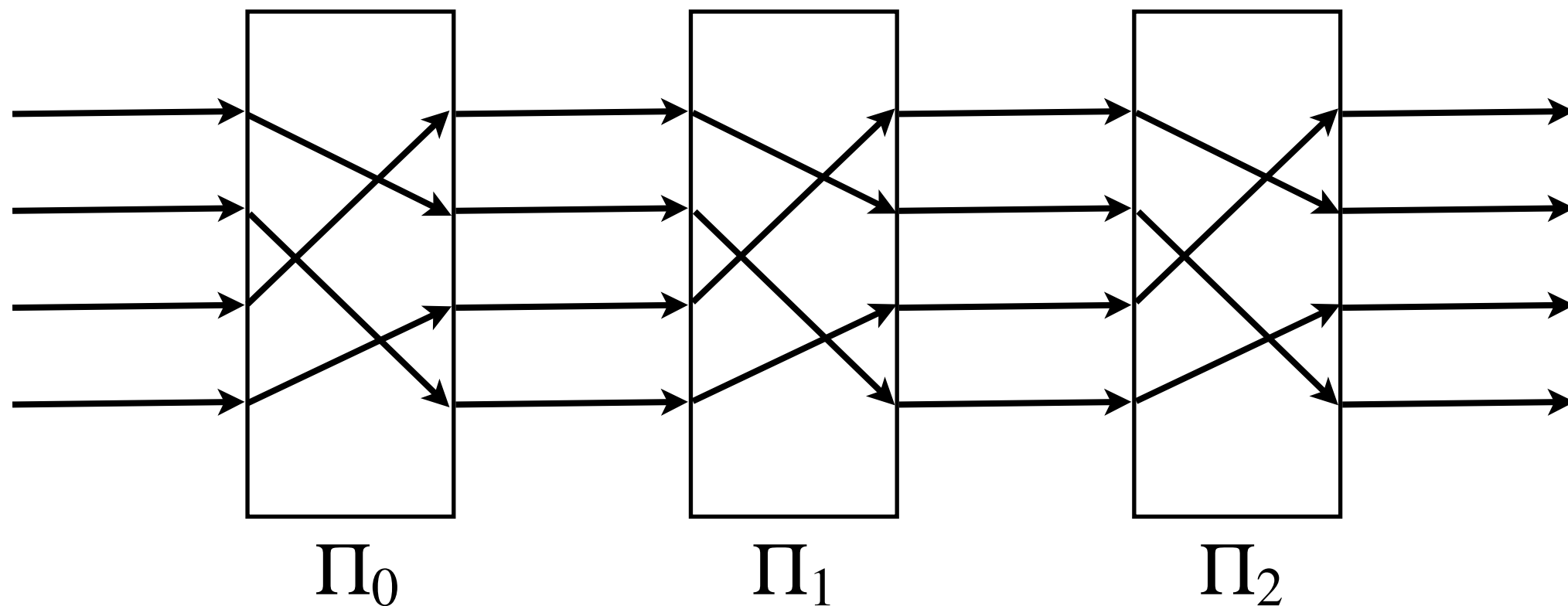
# Cool trick: reencryption

$$E(M) \oplus E(0) = E(M)^*$$

**Anybody can “reencrypt” a message.**  
(New random number introduced from  $E(0)$ .)

# Reencryption mixnets

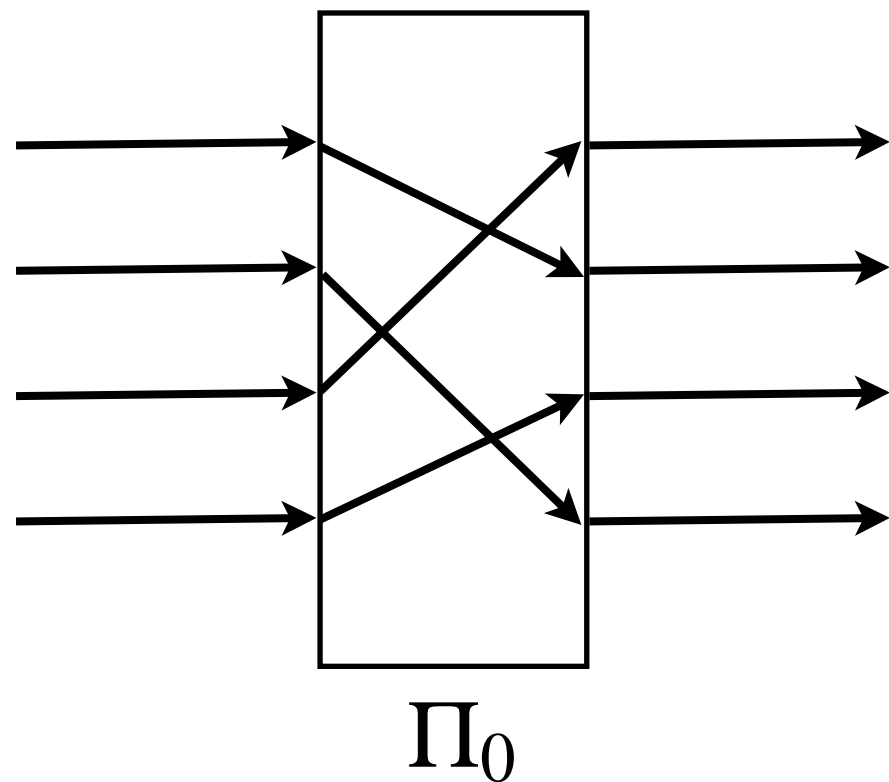
Permutations  $\Pi_i$ , where output is reencrypted.



**Each mix permutes/reencrypts.  
Must prove output corresponds to input.**

# Non-solution: reveal the mix

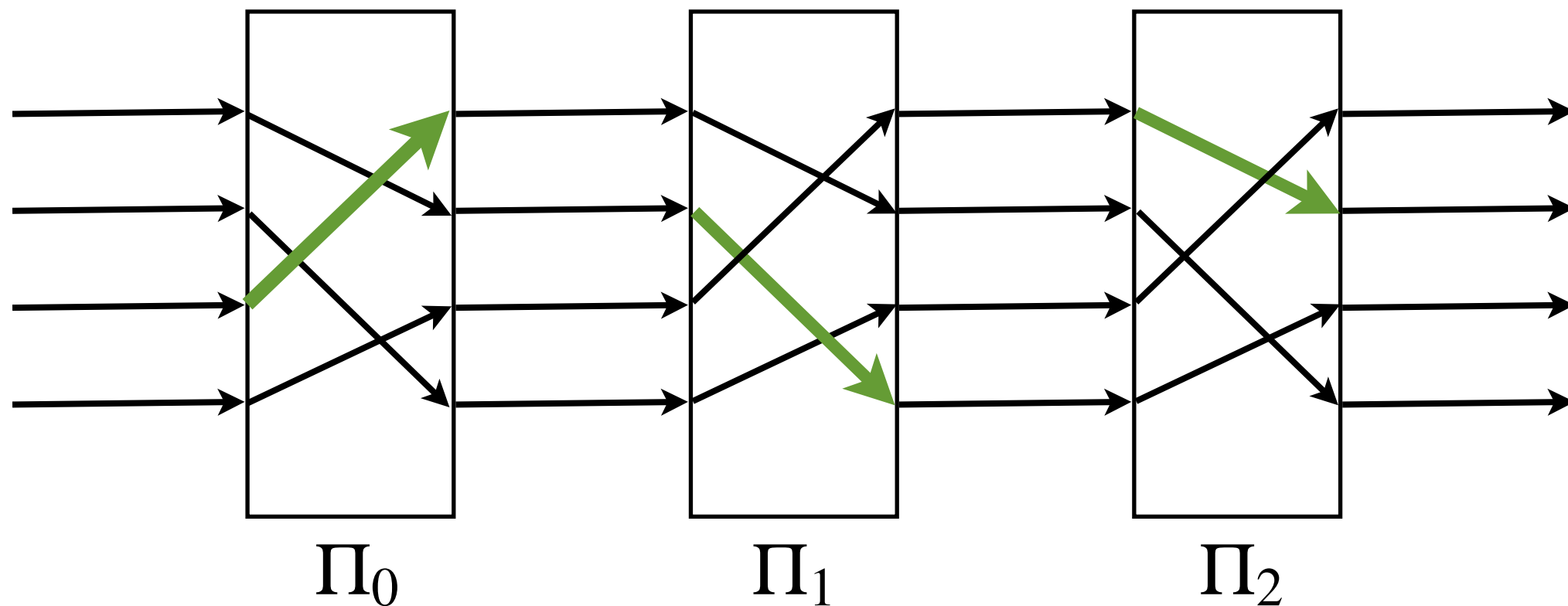
**Publish the random numbers and the permutation.**



**Eliminates benefit of randomization.**

# Randomized partial checking

**Effective across larger mixes.**  
**(Jakobsson, Jules, Rivest '02)**



Say we're mixing 1 million ballots, each mix reveals 1%. After five mixes, 99.99% chance that all ballots reencrypted at least once.

# Zero-knowledge proofs (ZKP)

**want to prove you know something**

while revealing nothing

**generalized format**

prover: commit to something (e.g., reencryption mix output)

verifier: *challenge* the prover

prover: respond to the challenge

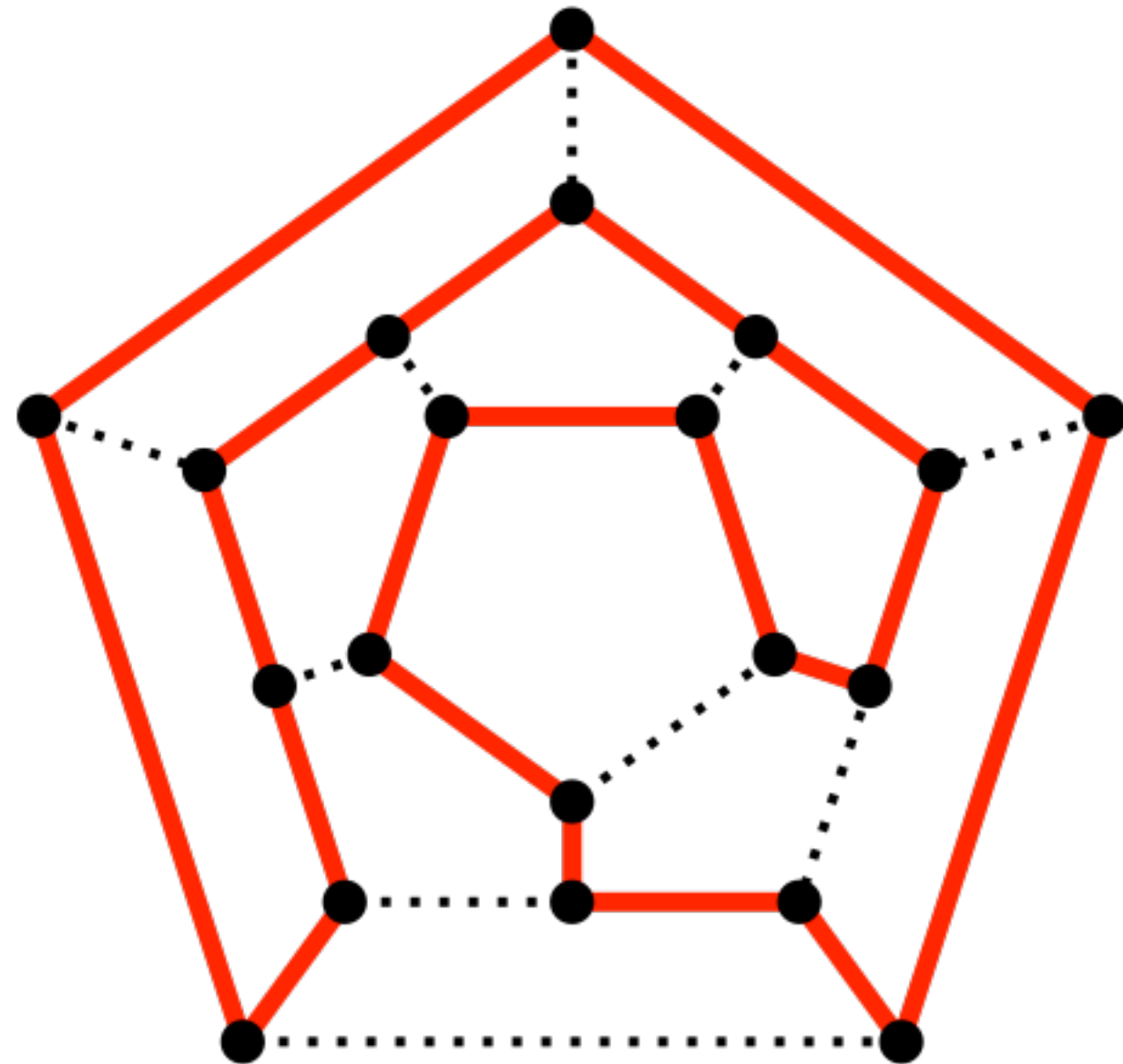
# Example: Hamiltonian paths

**Prover:** “I know a HP over graph  $G$ .” Compute graph isomorphism  $H$ . Publish  $G$ ,  $H$ .

**Verifier:** Coin toss. Heads: tell me HP over  $H$ . Tails: tell me isomorphism  $G$  to  $H$ .

(Repeat  $N$  times.)

If prover doesn't know HP, verifier catches with high probability.

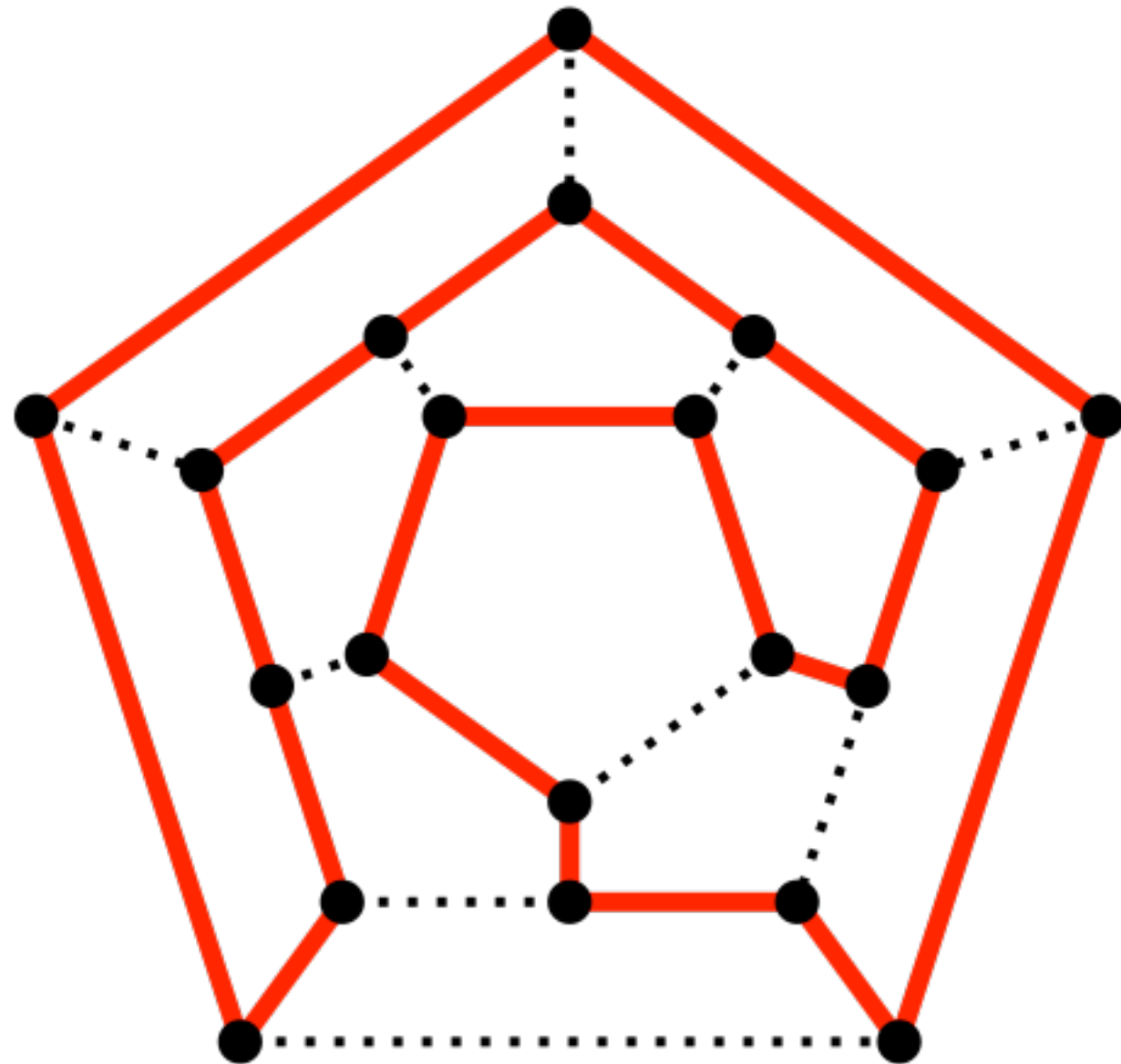


# Non-interactive ZK proofs

**Prover:** Precompute  $N$  isomorphisms ( $H_1$  to  $H_N$ ) and hash them. Hash function yields coin tosses for virtual challenger. Then output the results.

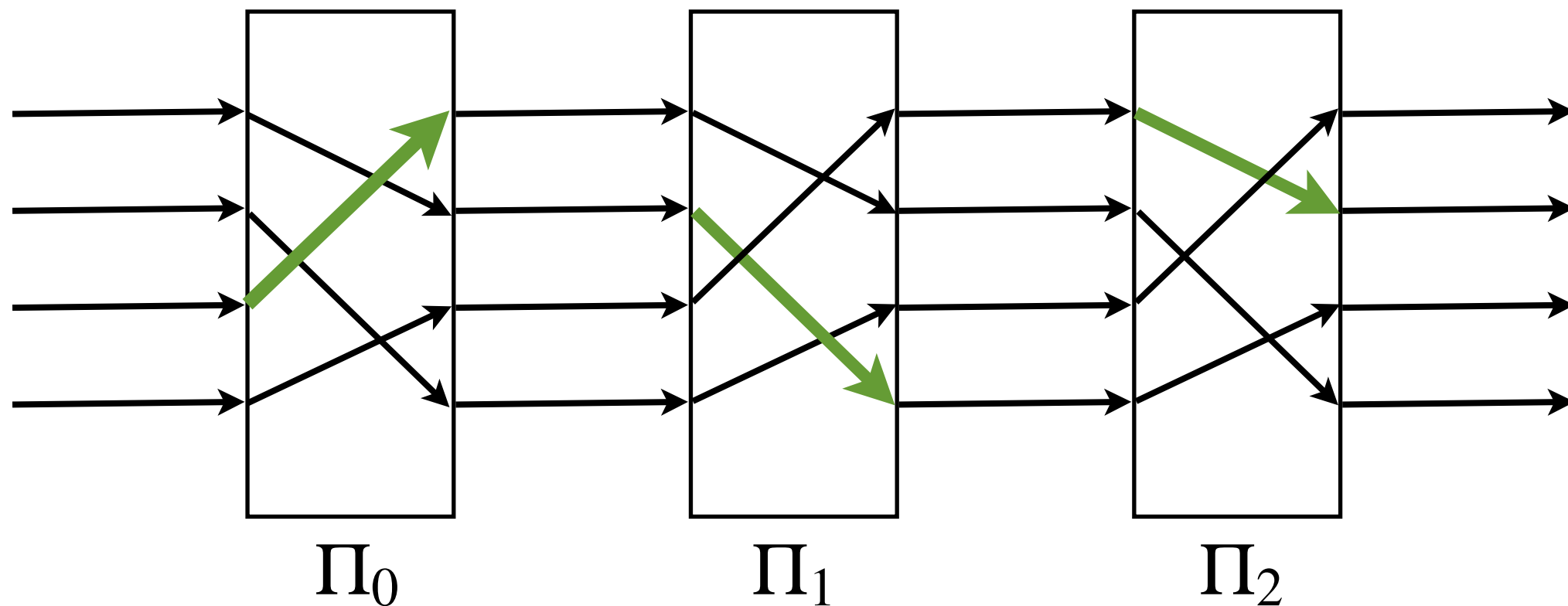
(Assumes good hash functions.)

This is an example of the *Fiat-Shamir heuristic* (1986).



# NIZK variant for mixes

**Hash the output of the permutation/reencryption. Use those bits to select which edges get revealed.**



Say we're mixing 1 million ballots, each mix reveals 1%. After five mixes, 99.99% chance that all ballots reencrypted at least once.



# Evil machine: $E(\text{bignum})$ ?

Must prove ciphertext corresponds to well-formed plaintext. (Example, prove counters are zero or one.)

We need another ZK tool: Chaum-Pedersen proofs.

Prover knows:  $(g, g^x), (h, h^x)$

Wants to prove that these two tuples share  $x$

# Chaum-Pedersen proofs (1992)

*Goal: demonstrate  $(g, g^x), (h, h^x)$*

**P**: choose random  $w \in \mathbb{Z}_p^*$ , compute  $(A = g^w, B = h^w)$

Send  $(A, B)$  to  $V$

**V**: pick a random number  $c$  (challenge), send to  $P$

**P**: compute  $R = w + xc$

send  $R$  to  $V$

**V**: Compute

$$\begin{aligned} A(g^x)^c &= g^w g^{xc} \\ &= g^{w+xc} \\ &= g^R \end{aligned}$$

$$\begin{aligned} B(h^x)^c &= h^w h^{xc} \\ &= h^{w+xc} \\ &= h^R \end{aligned}$$

# Fake C-P proofs?

*Goal: demonstrate  $(g, g^x), (h, h^x)$*

**P**: choose random  $w \in \mathbb{Z}_p^*$ , compute  $(A = g^w, B = h^w)$

Send  $(A, B)$  to  $V$

**V**: pick a random number  $c$  (challenge), send to  $P$

**P**: compute  $R = w + xc$

send  $R$  to  $V$

**V**: Compute

$$\begin{aligned} A(g^x)^c &= g^w g^{xc} \\ &= g^{w+xc} \\ &= g^R \end{aligned}$$

$$\begin{aligned} B(h^x)^c &= h^w h^{xc} \\ &= h^{w+xc} \\ &= h^R \end{aligned}$$

# Fake C-P proofs?

*Goal: demonstrate  $(g, g^x), (h, h^x)$*

**P:** choose random  $w \in \mathbb{Z}_p^*$ , compute  $(A = \cancel{g^w}, B = \cancel{h^w})$

Send  $(A, B)$  to  $V$

**V:** pick a random number  $c$  (challenge), send to  $P$

**P:** compute  $R = w + xc$

send  $R$  to  $V$

**V:** Compute

$$\begin{aligned} A(g^x)^c &= g^w g^{xc} \\ &= g^{w+xc} \\ &= g^R \end{aligned}$$

$$\begin{aligned} B(h^x)^c &= h^w h^{xc} \\ &= h^{w+xc} \\ &= h^R \end{aligned}$$

# Fake C-P proofs?

Goal: demonstrate  $(g, g^x), (h, h^x)$

**P**: choose random  $w \in \mathbb{Z}_n^*$ , compute  $(A = g^w, B = h^w)$

Send  $(A, B)$  to **V**. **P** chooses fake  $c$ , **R**: then  $A = g^R (g^{xc})^{-1}$ .

**V**: pick a random number  $c$  (challenge), send to **P**

**P**: compute  $R = w + xc$   
send  $R$  to **V**

**V**: Compute

$$\begin{aligned} A(g^x)^c &= g^w g^{xc} \\ &= g^{w+xc} \\ &= g^R \end{aligned}$$

$$\begin{aligned} B(h^x)^c &= h^w h^{xc} \\ &= h^{w+xc} \\ &= h^R \end{aligned}$$

$$A(g^x)^c$$

# Fake C-P proofs?

Goal: demonstrate  $(g, g^x), (h, h^x)$

**P**: choose random  $w \in \mathbb{Z}_n^*$ , compute  $(A = g^w, B = h^w)$

Send  $(A, B)$  to **V**. **P** chooses fake  $c$ , **R**: then  $A = g^R (g^{xc})^{-1}$ .

**V**: pick a random number  $c$  (challenge), send to **P**

**P**: compute  $R = w + xc$

send  $R$  to **V**

Observer can compute  $A(g^x)^c \dots$

**V**: Compute

$$\begin{aligned} A(g^x)^c &= g^w g^{xc} \\ &= g^{w+xc} \\ &= g^R \end{aligned}$$

$$\begin{aligned} B(h^x)^c &= h^w h^{xc} \\ &= h^{w+xc} \\ &= h^R \end{aligned}$$

# Fake C-P proofs?

*Goal: demonstrate  $(g, g^x), (h, h^x)$*

**P**: choose random  $w \in \mathbb{Z}_n^*$ , compute  $(A = g^w, B = h^w)$

Send  $(A, B)$  to **V**     **P** chooses fake  $c$ , **R**: then  $A = g^R (g^{xc})^{-1}$ .

**V**: pick a random number  $c$  (challenge), send to **P**

**P**: compute  $R = w + xc$

send  $R$  to **V**

Observer can compute  $A(g^x)^c \dots$

**V**: Compute

$$\begin{aligned} A(g^x)^c &= g^w g^{xc} \\ &= g^{w+xc} \\ &= g^R \end{aligned}$$

$$\begin{aligned} B(h^x)^c &= h^w h^{xc} \\ &= h^{w+xc} \\ &= h^R \end{aligned}$$

*ZK protocols only work when “live” (or use Fiat-Shamir heuristic for non-interactive)*

# C-P for vote testing

Can I prove a vote is zero or one? First, how about proving it's zero using C-P.

Want to verify  $\langle g^r, g^{ar} g^v \rangle$  for a specific value of  $v$ ?

Do C-P protocol where  $(g, g^x), (h, h^x)$  becomes

$$(g, g^r), \left( g^a, \frac{g^{ar} g^v}{g^v} \right)$$

We could do this for any value of  $v$

Challenge is to do  $v = 0$  and  $v = 1$  at the same time.



# Cramer-Damgård-Schoenmakers (1996)

Can run two Chaum-Pedersen (or any two ZK proofs like this) simultaneously, one “real” and one “simulated”.

First, fake a proof (e.g., for  $v = 1$ ) in advance.

Then, announce the first message for both protocols. Challenger sends  $c$ , prover announced a split  $c_0, c_1$  where  $c_0 + c_1 = c$ , then executes both ZK protocols.

Verifier cannot tell which one was real vs. simulated, but knows that **one** of them was real.

# Crypto summary

At the end of the day, **any** election observer can now:

- verify every single ballot for being “well-formed”  
(valid Elgamal tuple, encrypted zero-or-one, etc.)
- add together all the ballots (homomorphically)
- verify a proof of the tally (Chaum-Pedersen again)  
(only the election authority can generate this)

But we have no idea if the original ciphertext corresponded to the **intent of the voter** (versus evil machine flipping votes).